

The Dilaton and its many Faces

Javi Serra



with B.Bellazzini, C.Csaki, J.Hubisz, J.Terning

arXiv:1209.3299

arXiv:1305.3919

arXiv:1312.0259

arXiv:14xx.xxxx

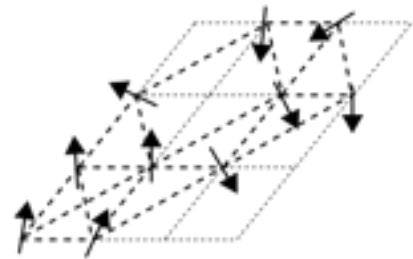
UC Irvine Joint Particle Physics Seminar
April 9, 2014

Quantum field theory of order parameter describes many physical systems with phase transitions

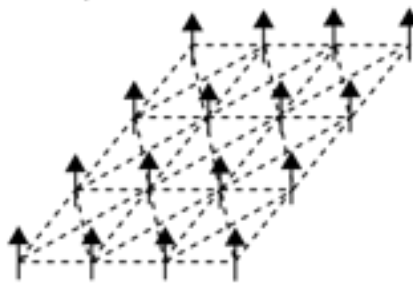
Ferromagnetism

temperature

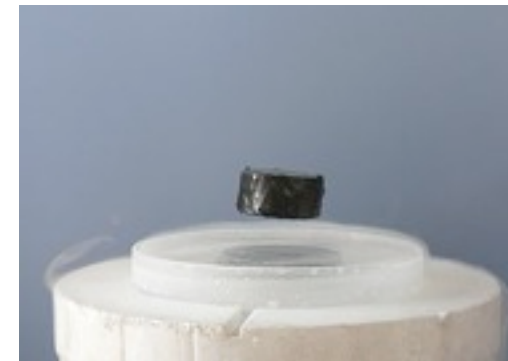
$$T > T_C$$



$$T < T_C$$

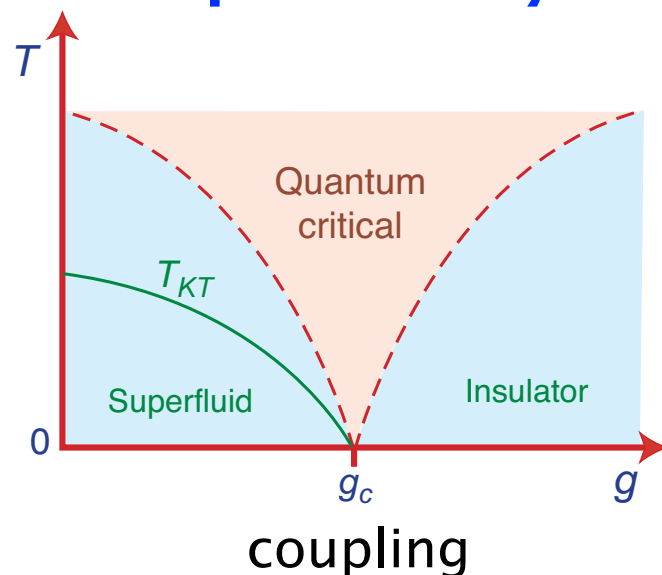


Superconductivity

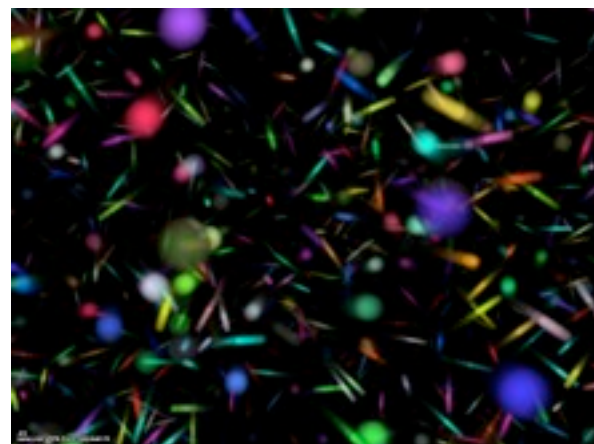


$$T < T_C$$

Superfluidity



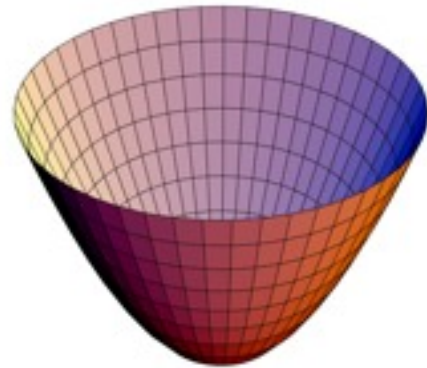
Vacuum State of Nature



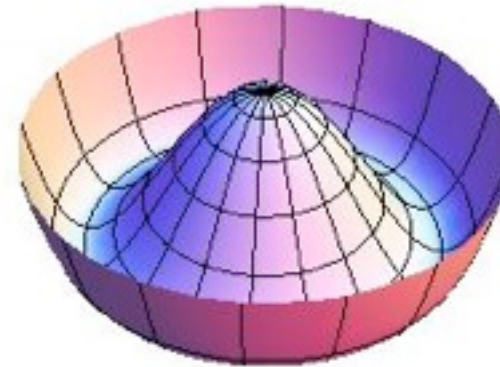
Inflation
ElectroWeak Symmetry Breaking
Quantum Chromodynamics

$$\mathcal{L} = (\partial\phi^\dagger)(\partial\phi) + m^2\phi^\dagger\phi - \lambda(\phi^\dagger\phi)^2$$

Unbroken phase



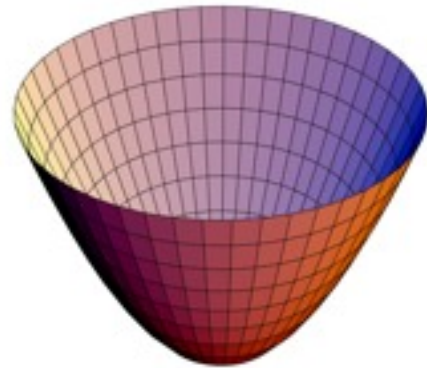
Broken phase



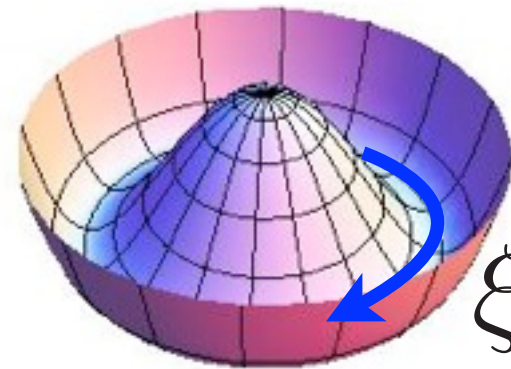
Spontaneous Symmetry Breaking: $G \rightarrow H$

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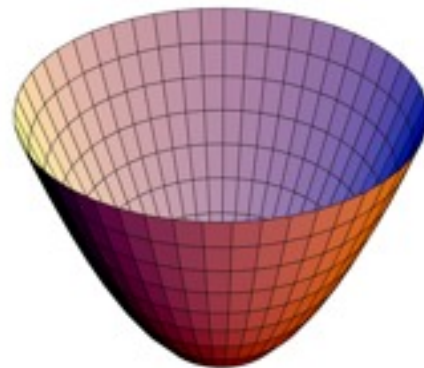
Spontaneous Symmetry Breaking: $G \rightarrow H$

(approximately) Massless Goldstone modes appear = phases

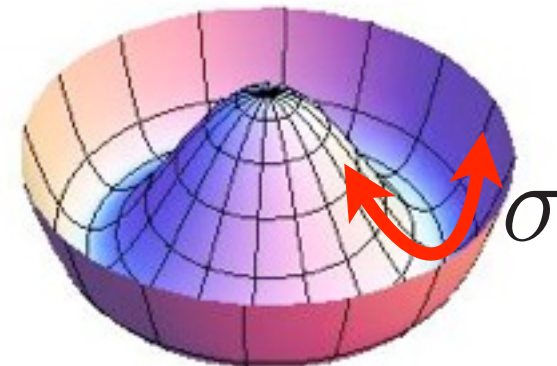
$$\phi = e^{i\xi}(\langle\phi\rangle + \sigma)$$

$$\mathcal{L} = (\partial\phi^\dagger)(\partial\phi) + m^2\phi^\dagger\phi - \lambda(\phi^\dagger\phi)^2$$

Unbroken phase



Broken phase



Spontaneous Symmetry Breaking: $G \rightarrow H$

No amplitude mode without adjusting parameters = TUNING

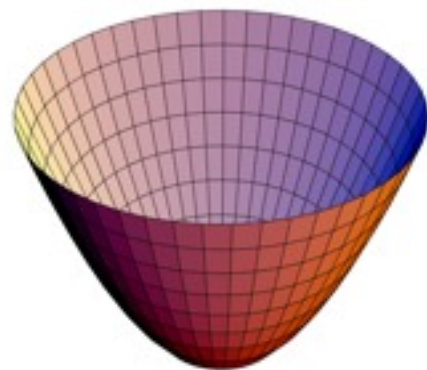
$$\phi = e^{i\xi}(\langle\phi\rangle + \sigma)$$

$$m \sim (T - T_C), (j - j_C), (\Lambda - \Lambda_Q)$$

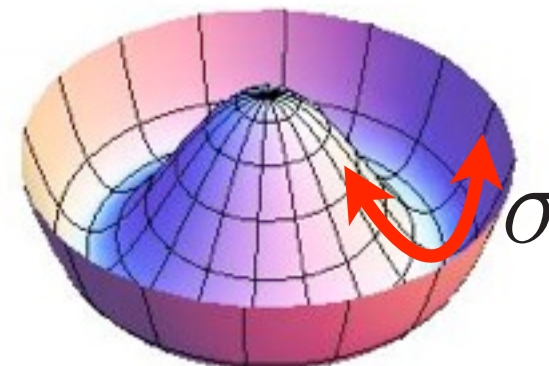
Fundamental scalars are unnatural

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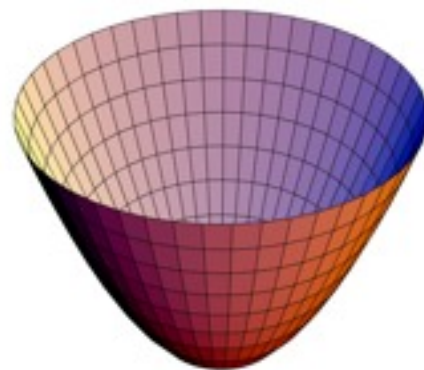


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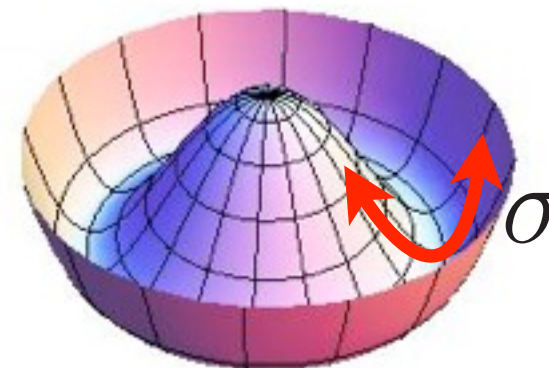
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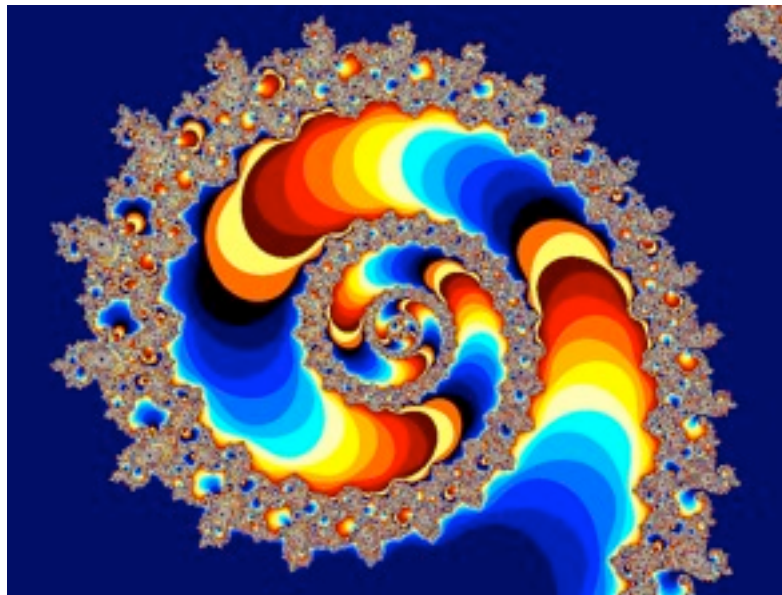


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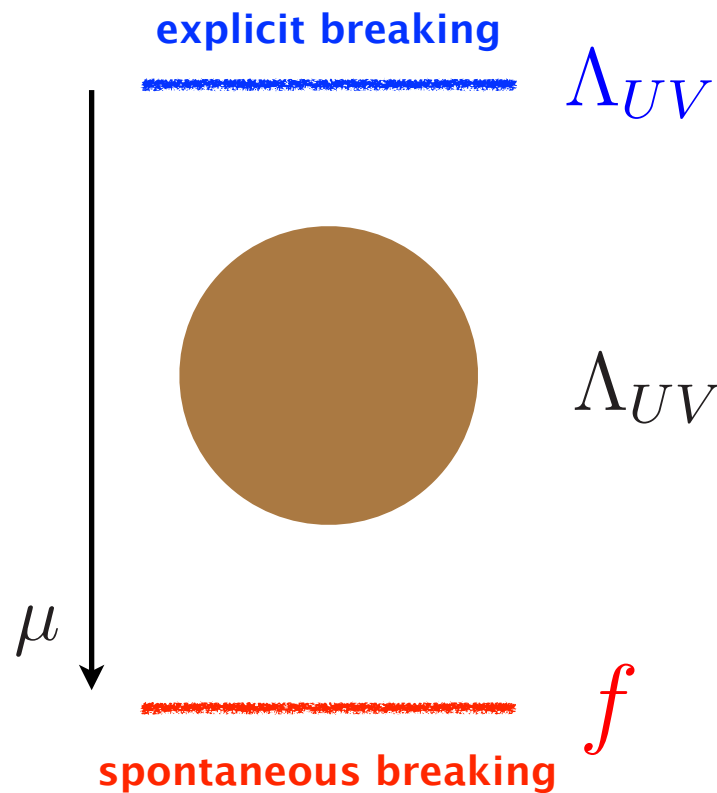
Fundamental scalars are unnatural



The Dilaton



What is the dilaton?



Scale (conformal) invariant sector

$$x \rightarrow e^\alpha x, \quad \Phi(x) \rightarrow e^{d_\Phi \alpha} \Phi(e^\alpha x)$$

$$\mathcal{S}_{CFT} = \sum_{\mathcal{O}} \int d^4x \mathcal{O}, \quad d_{\mathcal{O}} = 4$$

- Irrelevant operators are unimportant at low energies.
- No relevant operators can be present.

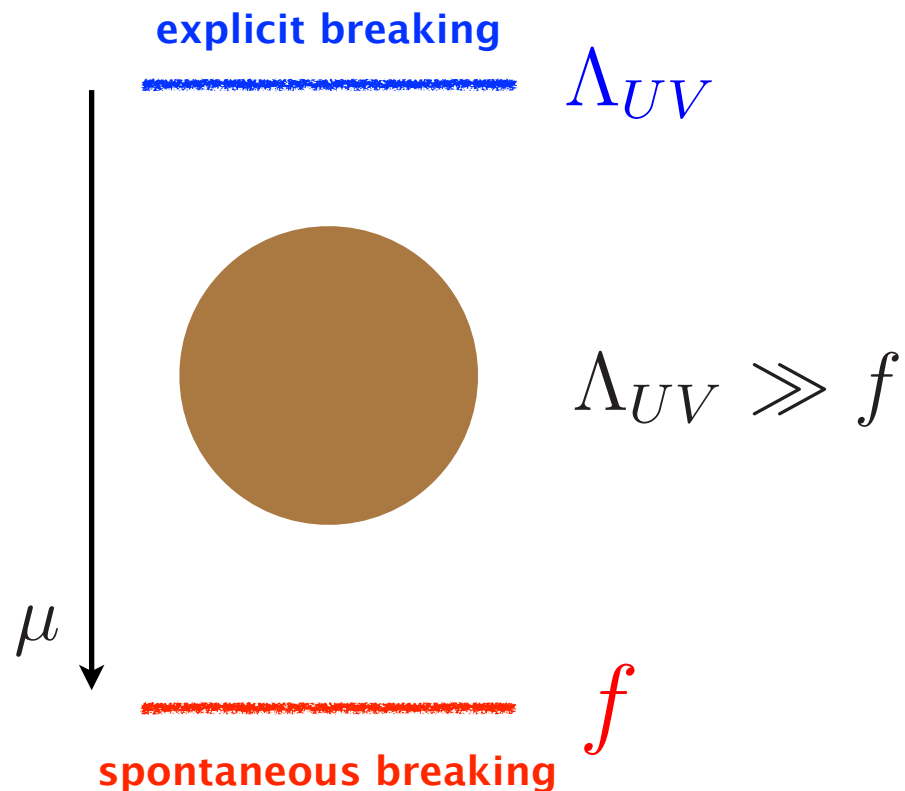
Spontaneous breaking of scale invariance

$$\langle \mathcal{O}(x) \rangle = f^{d_{\mathcal{O}}}$$

1 GB (enough): $\text{SO}(4, 2)/\text{SO}(3, 1)$

$$\chi \equiv f e^{\sigma/f} \rightarrow e^\alpha \chi$$
$$\sigma \rightarrow \sigma + \alpha f$$

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Compositeness

$$\mathcal{O} = \bar{\psi}\psi$$

Chiral symmetry is crucial in both cases

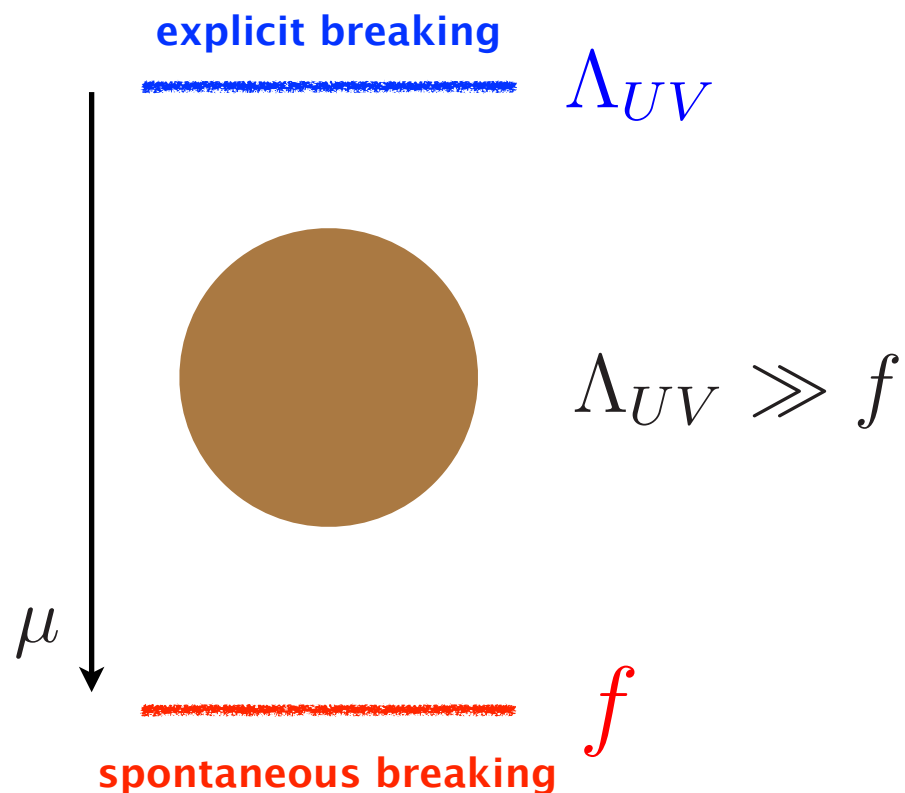
new states at
 $\Lambda_{IR} \sim 4\pi f$

Supersymmetry

$$\mathcal{O} = (\phi, \psi)$$

new states at
 gf

What is the dilaton?



Scale (conformal) invariant sector

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Effective theory for CFT spontaneous breaking

The point is if there is a light amplitude mode when scale generates

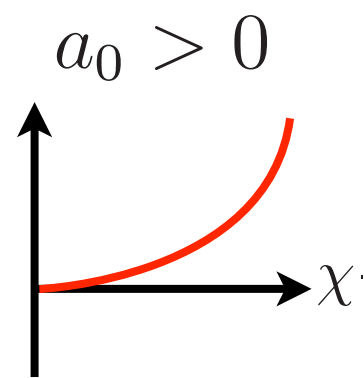
$$\mathcal{L}_{eff} = \frac{1}{2}(\partial\chi)^2 - a_0\chi^4 + \frac{a_{2,4}}{\chi^4}(\partial\chi)^4 + \dots$$

Non-zero potential allowed

Fubini '76

standard GB:

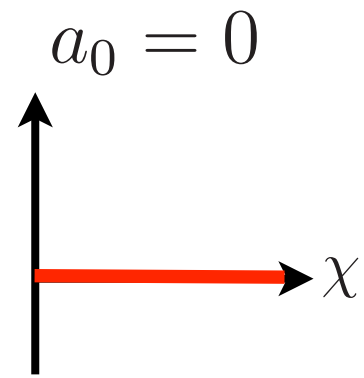
$$V(\pi) = 0$$



$$\langle\chi\rangle \rightarrow 0$$

CFT/AdS4

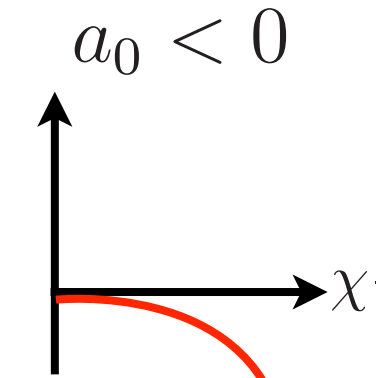
runaway



$$\langle\chi\rangle = f = ?$$

CFT/Poincare4

flat direction



$$\langle\chi\rangle \rightarrow \infty$$

CFT/dS4

runaway

Effective theory for CFT spontaneous breaking

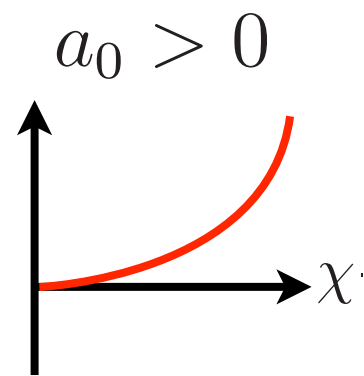
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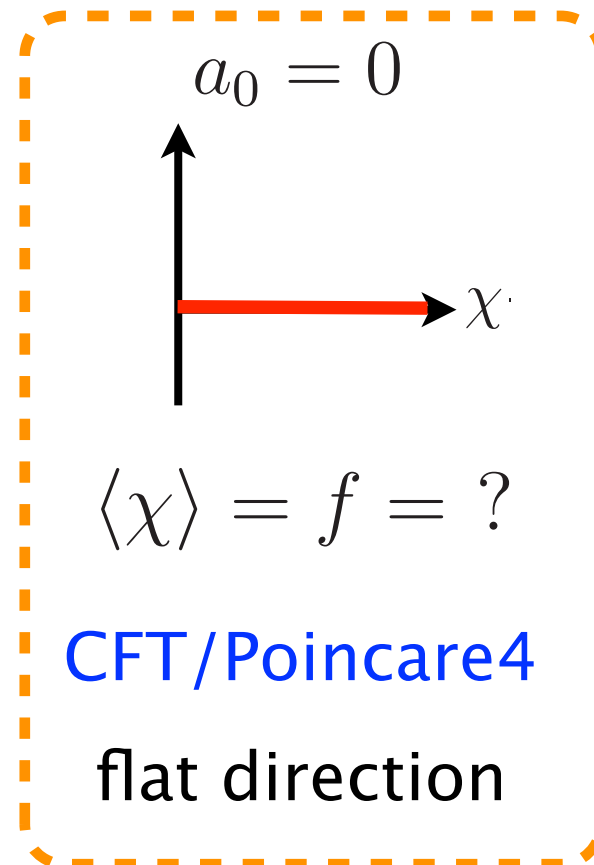
standard GB:
 $V(\pi) = 0$



$$\langle\chi\rangle \rightarrow 0$$

CFT/AdS4

runaway

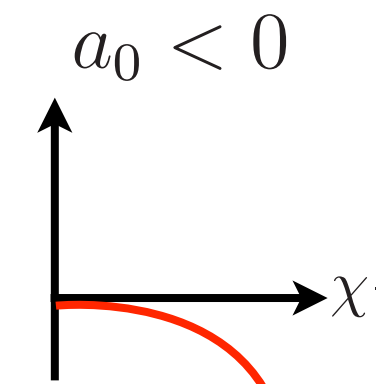


$$\langle\chi\rangle = f = ?$$

CFT/Poincare4

flat direction

TUNING



$$\langle\chi\rangle \rightarrow \infty$$

CFT/dS4

runaway

Flat directions are only natural in SUSY.

Effective theory for CFT spontaneous breaking

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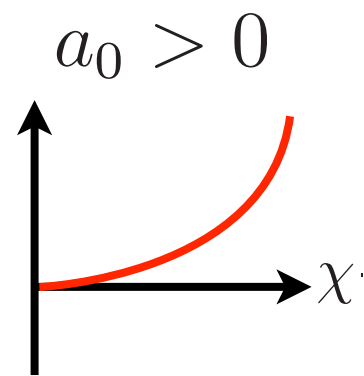
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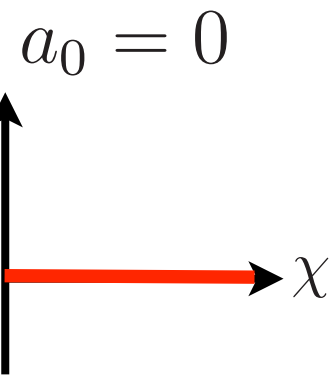
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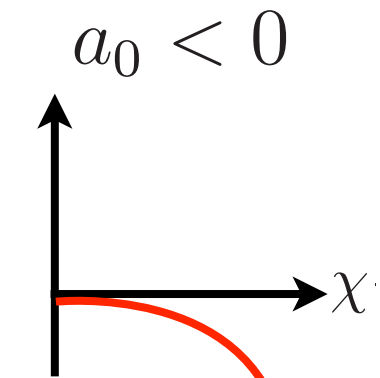
runaway



$$\langle\chi\rangle = f = ?$$

CFT/Poincare4

flat direction



$$\langle\chi\rangle \rightarrow \infty$$

CFT/dS4

runaway

WE WISH

We need to add a perturbation (explicit breaking)

$$\mathcal{L} = \mathcal{L}_{CFT} + \lambda \mathcal{O} \quad [\mathcal{O}] = 4 - \beta/\lambda \quad \frac{d\lambda(\mu)}{d \log \mu} = \frac{\beta(\lambda)}{\lambda} \neq 0$$

$$\downarrow \mu \rightarrow \chi$$

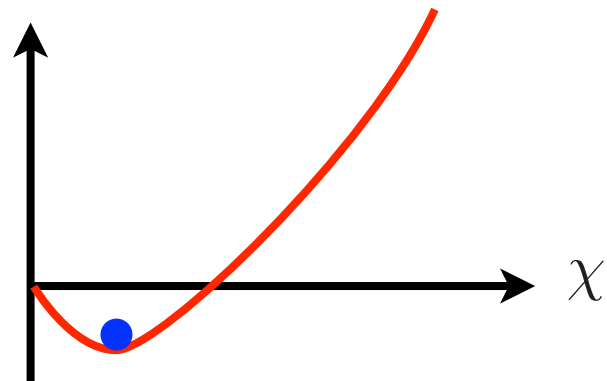
$$V(\chi) = \chi^4 F(\lambda(\chi))$$

$$F(\lambda(\chi)) = a_0 + \sum_n a_n \lambda^n(\chi)$$

Quartic gets dependence on running coupling.

“Running” potential

Coleman, Weinberg '73



The dilaton effectively scans the landscape of quartics.

Minimum and dilaton mass

$$\langle \chi \rangle = f$$

$$V' = f^3 [4F(\lambda(f)) + \beta F'(\lambda(f))] = 0$$

$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f))$$

Minimum and dilaton mass

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Dimensional Transmutation

$$\lambda(\mu) = \lambda_0 \left(\frac{\mu_0}{\mu} \right)^{\beta/\lambda} \quad \mu \rightarrow \chi$$

$$\lambda(f) \sim \sqrt{a_0}$$

$$f \sim \mu_0 \left(\frac{\lambda_0}{\sqrt{a_0}} \right)^{\lambda/\beta}$$

*A large hierarchy
has been generated!*

a_0 still matters for the dilaton mass

$$V' = f^3[4F(\lambda(f)) + \beta F'(\lambda(f))] = 0$$

$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f)) \stackrel{\downarrow}{=} -16f^2 F(\lambda(f))$$

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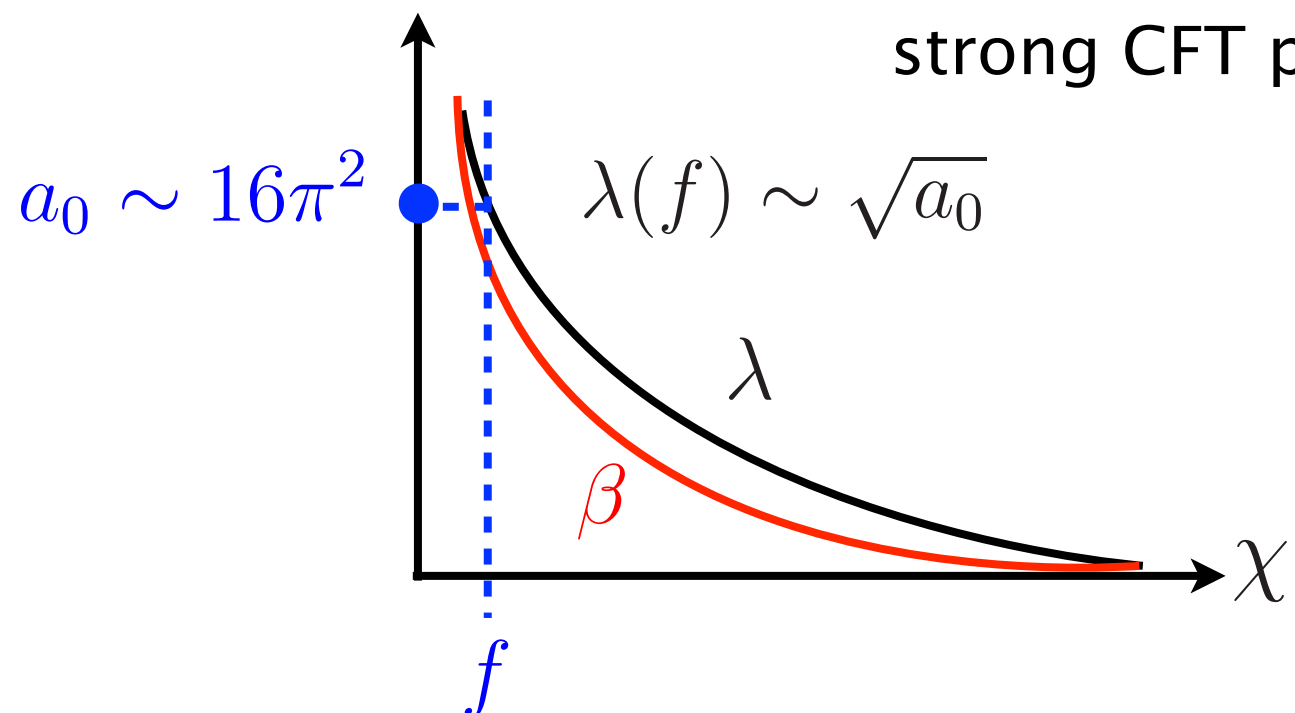
$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f)) \stackrel{\downarrow}{=} -16f^2 F(\lambda(f))$$

Generically there is NO small explicit breaking at f !

F is the vacuum energy (CC) in units of f : $F(f) \sim a_0 \sim \frac{\Lambda_{IR}^4}{16\pi^2 f^4} \sim 16\pi^2$

QCD-like

strong CFT perturbation



$m_d^2 \sim 16\pi^2 f^2 \sim \Lambda_{IR}^2$
NO remnant of scaling symmetry
NO dilaton in QCD-like theories

Holdom, Terning '88

a_0 still matters for the dilaton mass

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We can get small explicit breaking at f by tuning

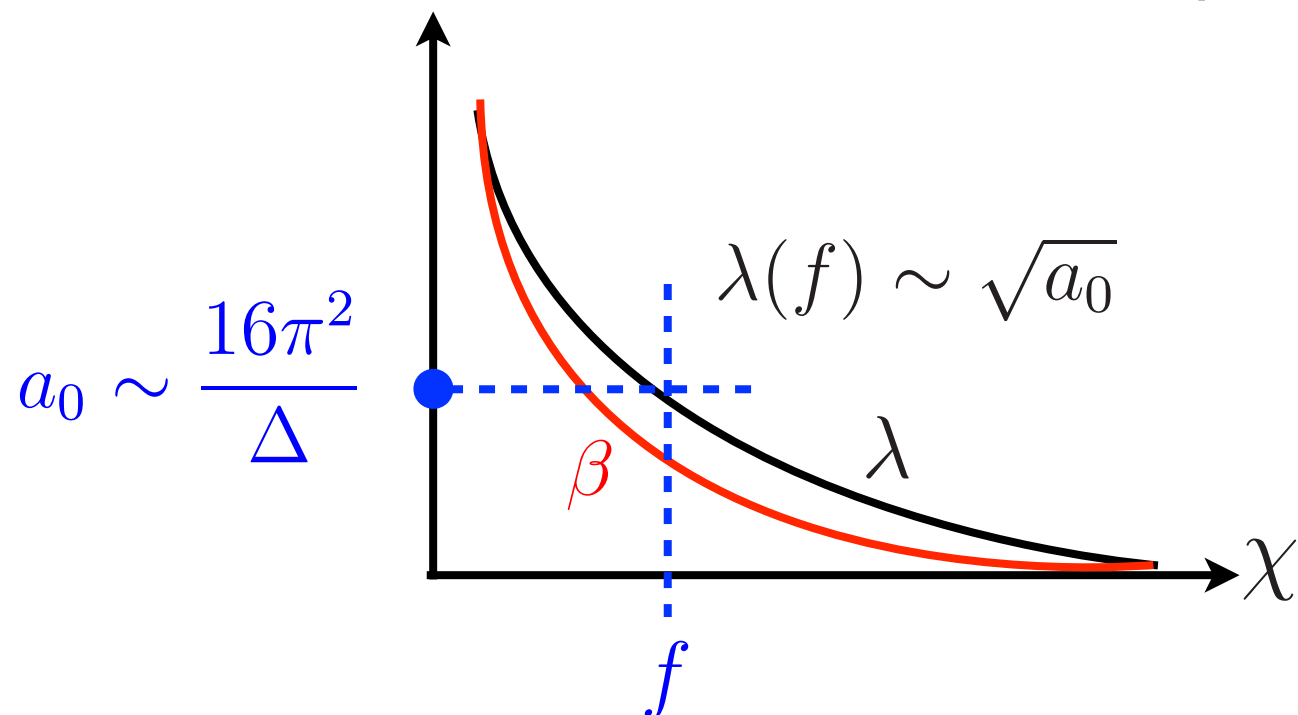
Start with small vacuum energy $\sim$ flat direction.

tuned-QCD-like

weak CFT perturbation

Randall, Sundrum '99

Goldberger, Wise '99



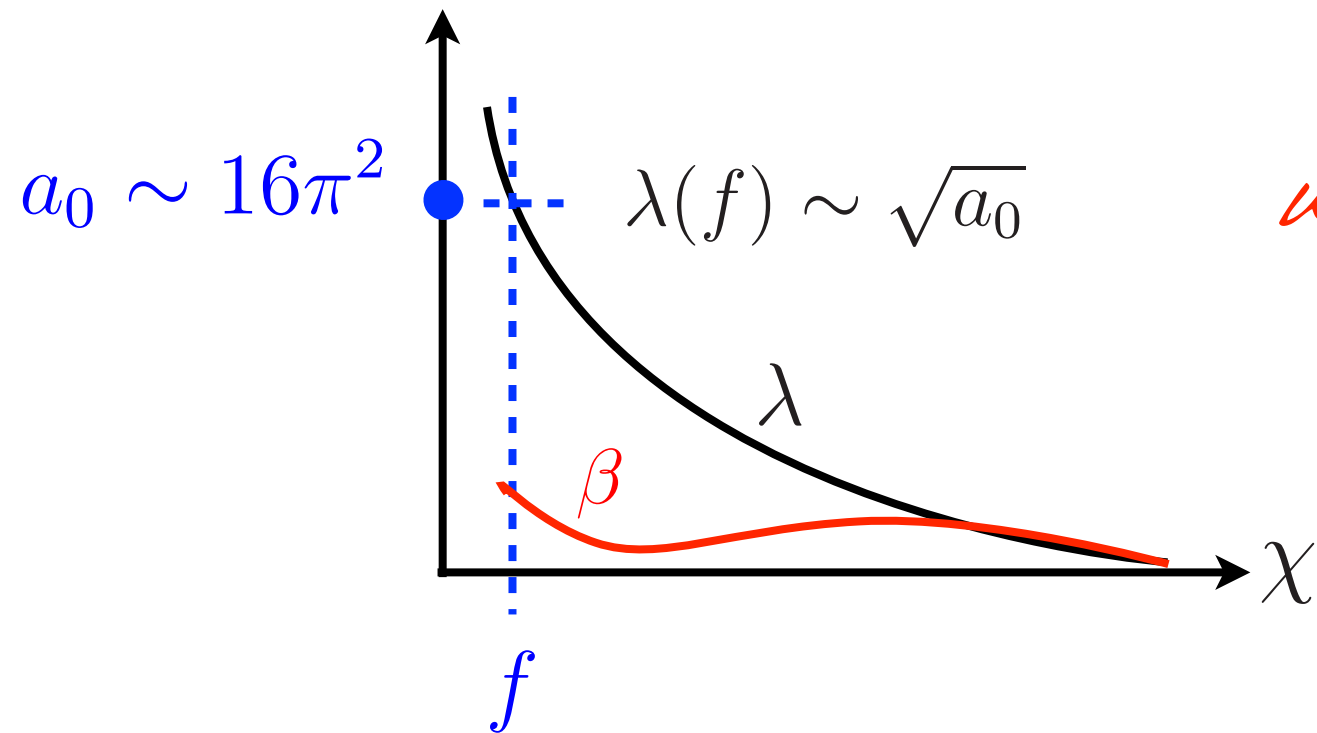
With TUNING: $\Delta \gtrsim \frac{\Lambda_{IR}}{m_d}$

But there is an unorthodox way out

CPR construction

Strong CFT perturbation but small breaking

$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f)) = -16f^2 F(\lambda(f)) = -16V(f)/f^2$$



Without "TUNING"

$$m_d^2 \ll \Lambda_{IR}^2$$

Let the dilaton scan the landscape of quartics but keep the slow running always.

Contino, Pomarol, Rattazzi, '10

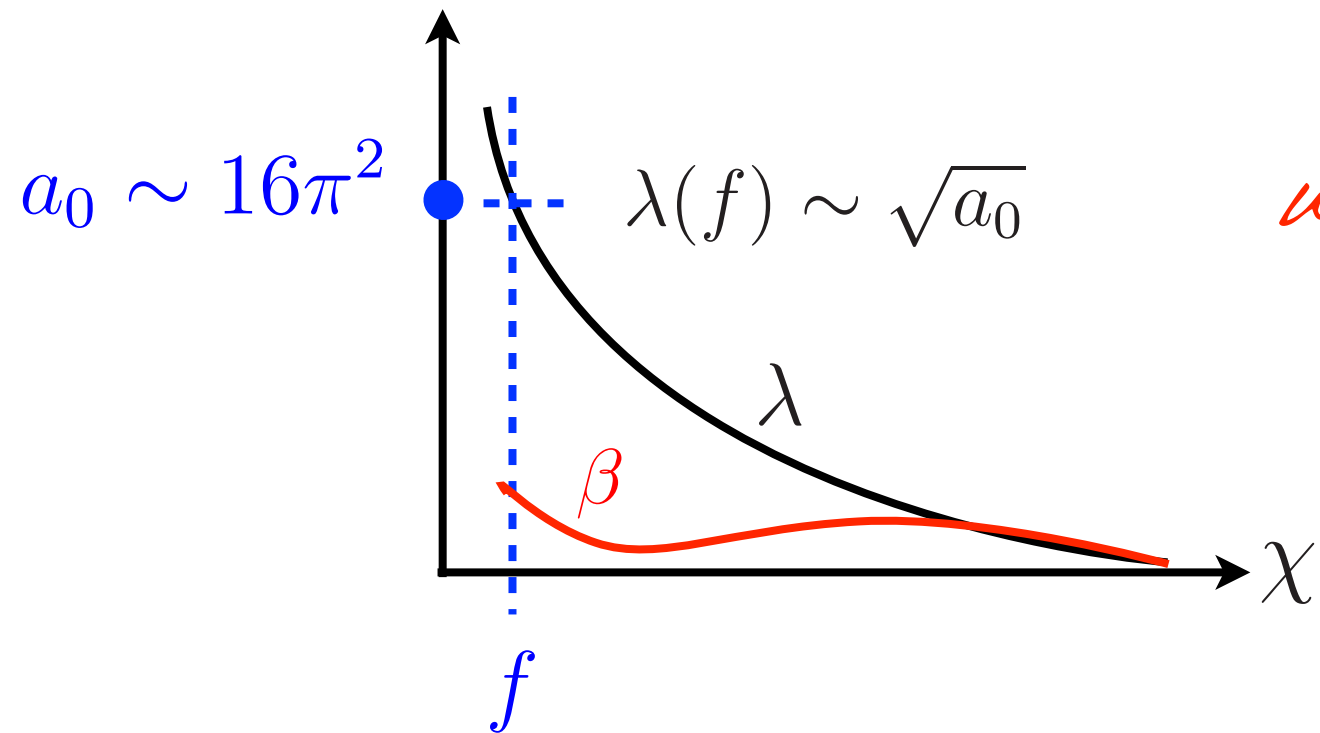
Bellazzini, Csaki, Hubisz, Terning, JS, '13

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Contino, Pomarol, Rattazzi, '10

Bellazzini, Csaki, Hubisz, Terning, JS, '13

An Extra-D Computable Example

An amazing conjecture

type IIB string theory
on $\text{AdS}_5 \times S^5$ $\longleftrightarrow$ $\mathcal{N} = 4$ SU(N) 4D gauge theory

Maldacena '97

$$\frac{R_{\text{AdS}}^4}{l_s^4} = 4\pi g_{\text{YM}}^2 N$$

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Maldacena '97

$$\frac{R_{\text{AdS}}^4}{l_s^4} = 4\pi g_{YM}^2 N$$

*Serves as a computational tool to describe systems that are
strongly coupled.*

$$g_{YM}^2 N \gg 1$$

$$N \gg 1$$

**weakly coupled
5-dimensional gravity**

AdS_5



**strongly coupled
4-dimensional CFT**

CFT_4

$$\text{AdS}_5 \longleftrightarrow \text{CFT}_4$$

5D field – 4D operator connection

$$\phi(x^\mu, y) \longleftrightarrow \mathcal{O}$$

$$\phi_0 = \phi(x^\mu, y)|_{\text{AdS boundary}} \longleftrightarrow \lambda_0$$

Generating functional

$$Z[\phi_0] = \int \mathcal{D}\phi_{\text{CFT}} e^{-S_{\text{CFT}}[\phi_{\text{CFT}}] - \int d^4x \phi_0 \mathcal{O}} = \int_{\phi_0} \mathcal{D}\phi e^{-S_{\text{bulk}}[\phi]} \equiv e^{iS_{\text{eff}}[\phi_0]}$$

$$\langle \mathcal{O} \dots \mathcal{O} \rangle = \frac{\delta^n S_{\text{eff}}}{\delta \phi_0 \dots \delta \phi_0}$$

$$\text{AdS}_5 \longleftrightarrow \text{CFT}_4$$

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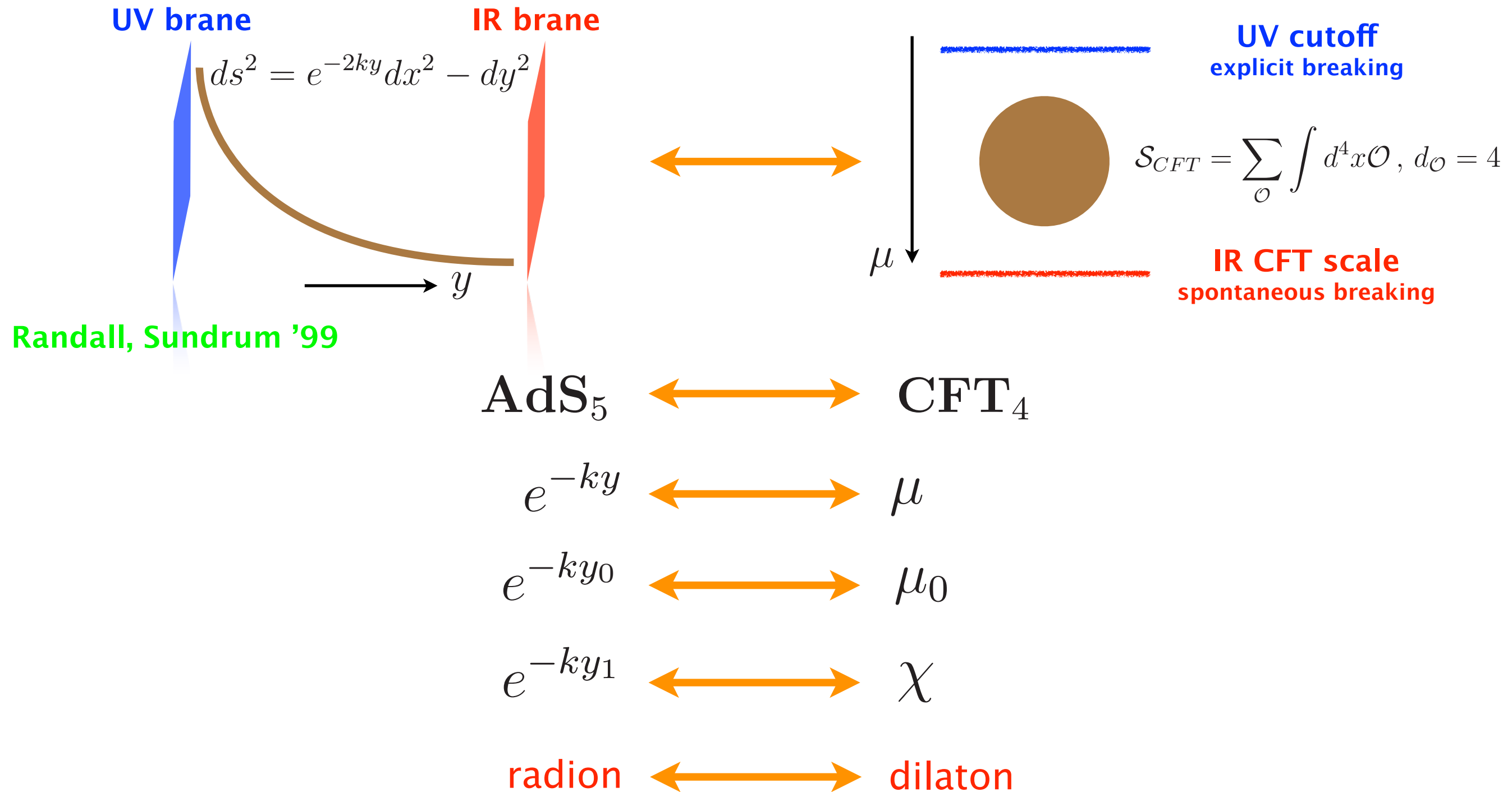
$$\langle \mathcal{O} \dots \mathcal{O} \rangle = \frac{\delta^n S_{\text{eff}}}{\delta \phi_0 \dots \delta \phi_0}$$

This correspondence has found many applications:

- ♦ Quantum gravity
- ♦ Electroweak hierarchy problem
- ♦ Quark–gluon plasma
- ♦ Superconductors, superfluids

and still offers many avenues for investigation.

Randall & Sundrum solved a hierarchy problem with a slice of AdS



The brane separation (hierarchy of scales) is fixed by χ .

5D gravitational action

$$S = - \int_{y=y_0} dx^4 \sqrt{g_0} \Lambda_0 - \int \sqrt{g} \left(\frac{1}{2\kappa^2} \mathcal{R} + \Lambda_{(5)} \right) - \int_{y=y_1} dx^4 \sqrt{g_1} \Lambda_1$$

Effective potential

$$V(\chi) = \left(\Lambda_0 + \Lambda_{(5)}/k \right) \mu_0^4/k^4 + \left(\Lambda_1 - \Lambda_{(5)}/k \right) \chi^4$$

$$k = \sqrt{\frac{-\Lambda_{(5)}\kappa^2}{6}}$$

5D gravitational action

$$S = - \int_{y=y_0} dx^4 \sqrt{g_0} \Lambda_0 - \int \sqrt{g} \left(\frac{1}{2\kappa^2} \mathcal{R} + \Lambda_{(5)} \right) - \int_{y=y_1} dx^4 \sqrt{g_1} \Lambda_1$$

Effective potential

$$k = \sqrt{\frac{-\Lambda_{(5)} \kappa^2}{6}}$$

$$V(\chi) = \underbrace{(\Lambda_0 + \Lambda_{(5)}/k)}_{\Lambda_{(4)} = 0} \mu_0^4/k^4 + \underbrace{(\Lambda_1 - \Lambda_{(5)}/k)}_{a_0 = 0} \chi^4$$

2 TUNINGS! Vanishing cosmological constant and dilaton flat direction.

Randall-Sundrum and followers tuned brane tension.

Brane distance is free.

This solution is not stable under perturbations.

Csaki, Graesser, Kolda, Terning '99

Explicit breaking perturbation in AdS/CFT

$$S = \int d^5x \sqrt{g} \left(-\frac{1}{2\kappa^2} \mathcal{R} + \frac{1}{2} g^{MN} \partial_M \phi \partial_N \phi - V(\phi) \right) - \int d^4x \sqrt{g_0} V_0(\phi) - \int d^4x \sqrt{g_1} V_1(\phi)$$

$$\text{AdS}_5 \longleftrightarrow \text{CFT}_4$$

$$\text{radion} \longleftrightarrow \text{dilaton}$$

$$V(\phi) = \Lambda_{(5)} \quad \phi \longleftrightarrow \mathcal{O} \quad \text{exactly marginal}$$

$$V'(\phi) = dV/d\phi \longleftrightarrow \beta(\lambda) = d\lambda/d \log \mu \quad \text{running}$$

$$(\partial\phi)|_{y=y_0} = 0 \quad \phi|_{y=y_0} \longleftrightarrow \lambda_0$$

$$\mathcal{L} = \mathcal{L}_{CFT} + \lambda \mathcal{O}$$

A simple example, scalar with bulk mass

$$V(\phi) = \Lambda_{(5)} + m^2 \phi^2$$

Scaling dimension of operator:

$$d_{\mathcal{O}} = 2 + \sqrt{4 + m^2/k^2}$$

Scalar solution of E.O.M. in RS:

$$\phi(y) = \underbrace{\phi_0 e^{-ky(4-d_{\mathcal{O}})}}_{\text{running}} + \underbrace{\phi_1 e^{-kyd_{\mathcal{O}}}}_{\text{condensate}}$$

$$\frac{d\lambda}{d \log \mu} \equiv \beta(\lambda) = (4 - d_{\mathcal{O}})\lambda$$

$$\phi_0 = \lim_{\mu_0 \rightarrow \infty} \mu_0^{4-d_{\mathcal{O}}} \lambda_0$$

$$\phi_1 = \frac{\langle \mathcal{O} \rangle}{2d_{\mathcal{O}} - 4}$$

The general stabilized RS is this:

$$S = \int d^5x \sqrt{g} \left(-\frac{1}{2\kappa^2} \mathcal{R} + \frac{1}{2} g^{MN} \partial_M \phi \partial_N \phi - V(\phi) \right) - \int d^4x \sqrt{g_0} V_0(\phi) - \int d^4x \sqrt{g_1} V_1(\phi)$$

Bellazzini, Csaki, Hubisz, Terning, JS, '13

UV brane

$$ds^2 = e^{-2A(y)} dx^2 - dy^2$$

IR brane

→ y

flat metric ansatz

good approximation

bulk E.O.M.

$$\begin{aligned} 4A'^2 - A'' &= -\frac{2\kappa^2}{3} V(\phi) \\ A'^2 &= \frac{\kappa^2 \phi'^2}{12} - \frac{\kappa^2}{6} V(\phi) \\ \phi'' &= 4A' \phi' + \frac{\partial V}{\partial \phi}. \end{aligned}$$

boundary conditions

$$\begin{aligned} 2A'|_{y=y_0, y_1} &= \pm \frac{\kappa^2}{3} V_{0,1}(\phi)|_{y=y_0, y_1} \\ 2\phi'|_{y=y_0, y_1} &= \pm \frac{\partial V_{0,1}}{\partial \phi} |_{y=y_0, y_1}, \end{aligned}$$

We derived the effective potential integrating over the extra-d

$$\int_{y_0}^{y_1} dy \mathcal{L}_{bulk} + \mathcal{L}_{boundary}(y_{0,1})$$



$$V_{eff} = V_{UV} + V_{IR}$$

$$V_{UV/IR} = e^{-4A(y_{0,1})} \left[V_{0,1}(\phi(y_{0,1})) \mp \frac{6}{\kappa^2} A'(y_{0,1}) \right]$$

Useful identification:

$$e^{-A(y_0)} \longleftrightarrow \mu_0$$
$$e^{-A(y_1)} \longleftrightarrow \chi$$

We obtain just what we expected, again.

$$V_{UV} = \mu_0^4 F(\lambda(\mu_0)) \qquad V_{IR} = \chi^4 F(\lambda(\chi))$$

UV vacuum energy

$$V_{UV} = \mu_0^4 \left[\Lambda_0 + \frac{\Lambda_{(5)}}{k} \right]$$

Modulated, slowly running, dilaton quartic, *with no TUNING!*

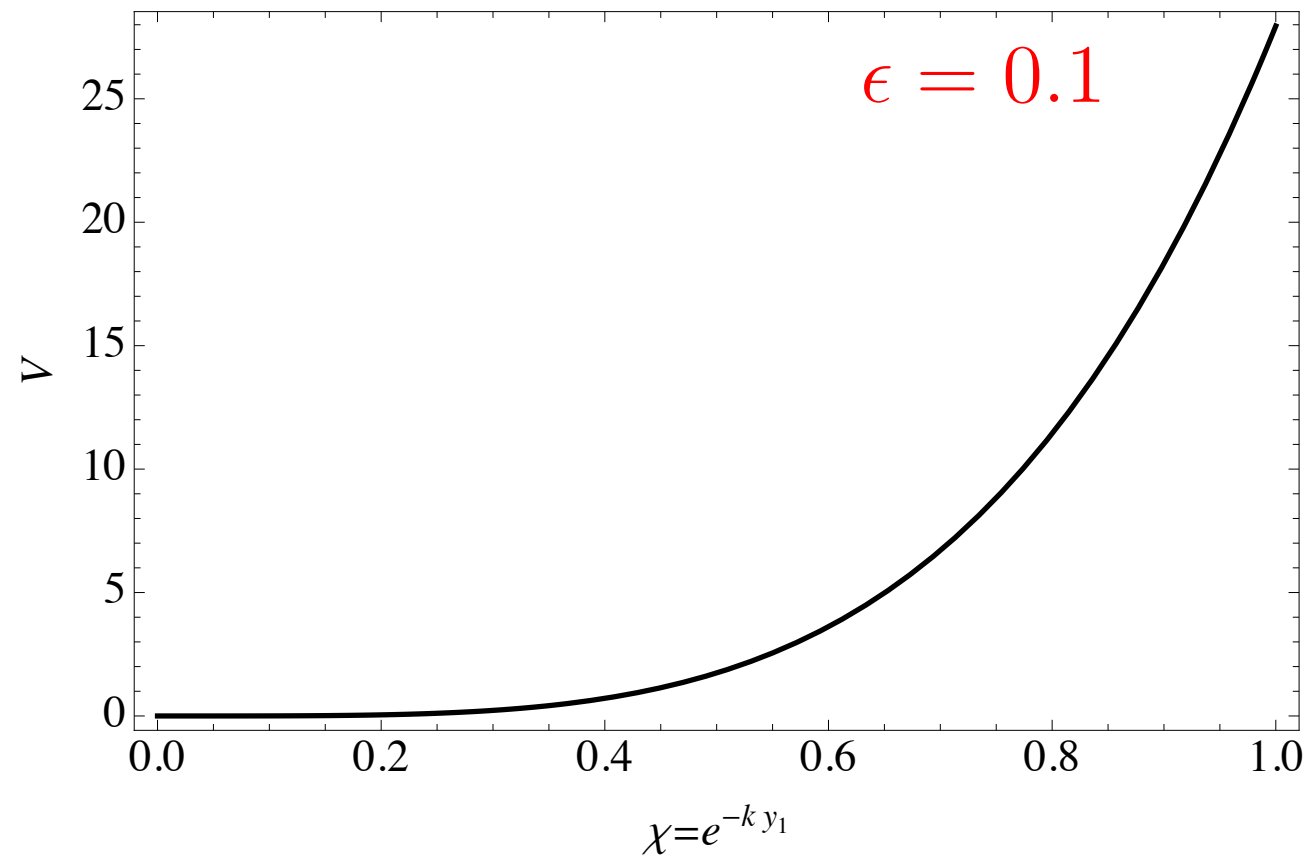
$$V_{IR} = \chi^4 \left[\Lambda_1 - \frac{\Lambda_{(5)}}{k} \cosh \left(\frac{2\kappa}{\sqrt{3}} (v_1 - v_0 (\mu_0/\chi)^\epsilon) \right) \right]$$

$$m^2 = -2\epsilon k^2 \quad \epsilon \ll 1 \quad d_{\mathcal{O}} \approx 4 - \epsilon$$

*As announced in the 4D effective Lagrangian analysis,
this potential yields a large hierarchy, a light dilaton, and
a small cosmological constant*

NATURAL & CORRELATED

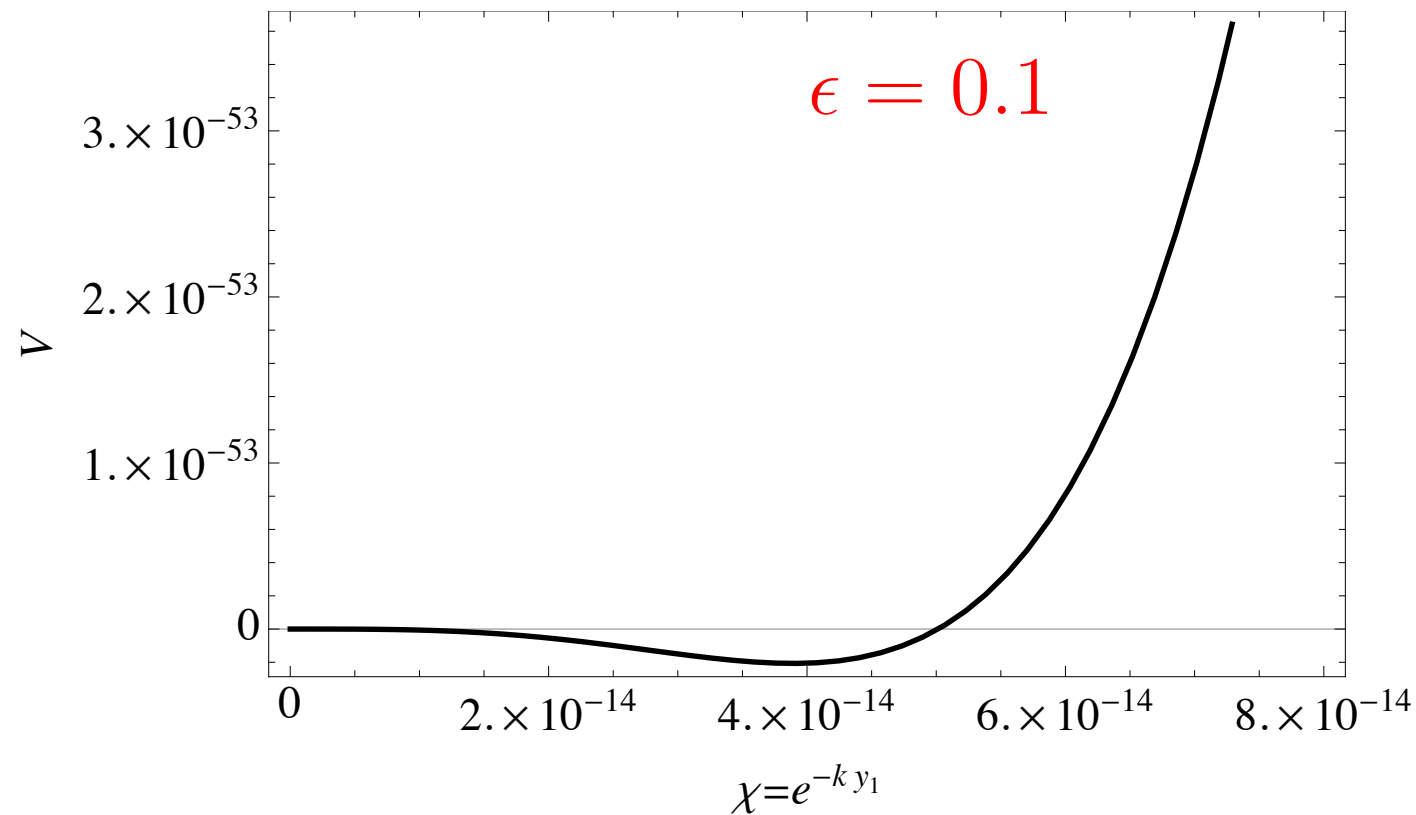
The large hierarchy



$$\langle \chi \rangle = f \quad \frac{f}{\mu_0} = \left(\frac{v_0}{v_1 - \text{sign}(\epsilon) \frac{\sqrt{3}}{2\kappa} \text{arcsech}(\Lambda_{(5)}/k\Lambda_1)} \right)^{1/\epsilon}$$

Thanks to slow running for long time.

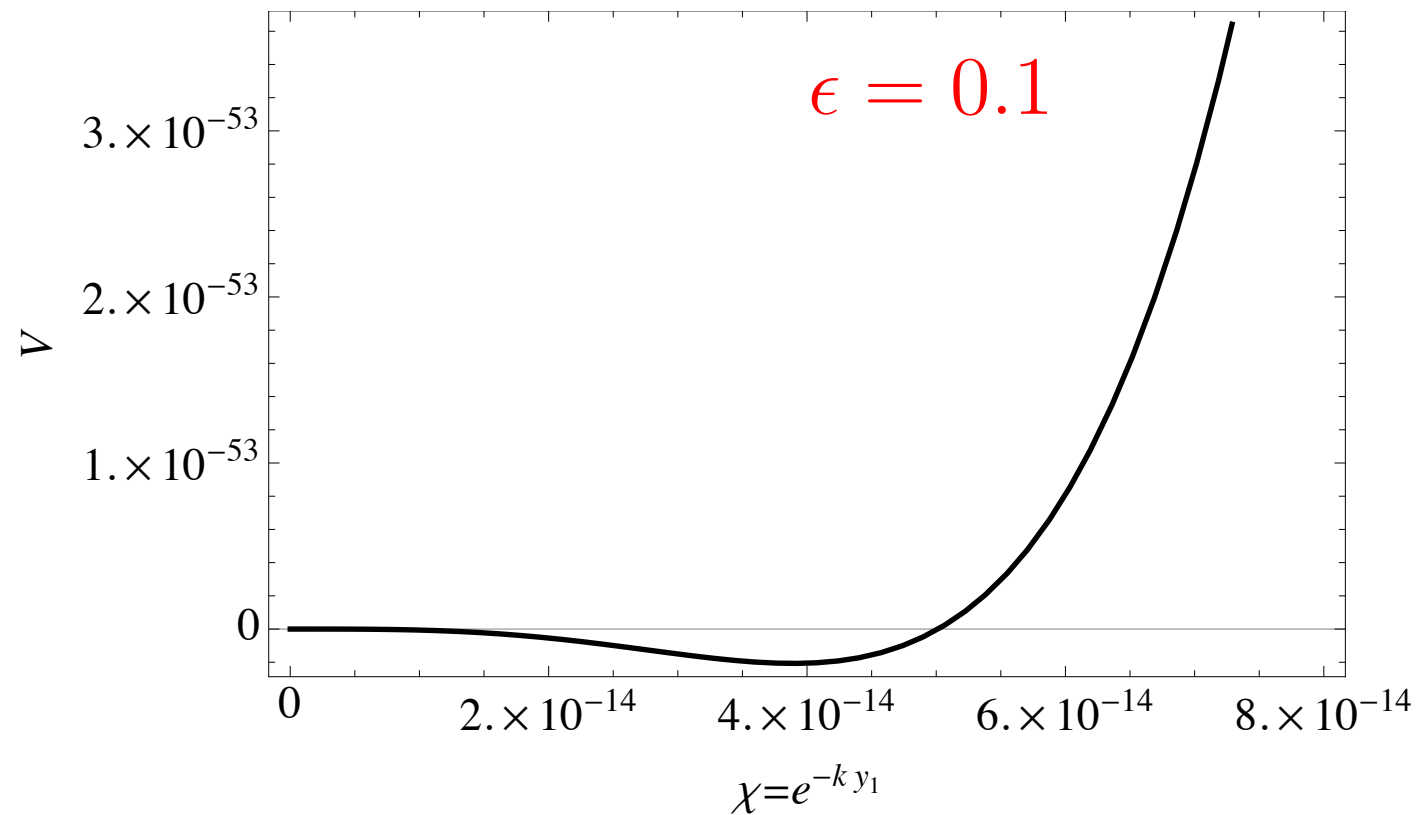
The light dilaton



$$m_{\chi}^2 \sim \epsilon \frac{32\sqrt{3}k v_0}{\kappa} \tanh \left(\frac{\kappa}{\sqrt{3}} (v_1 - v_0 (\mu_0/f)^\epsilon) \right) f^2 (\mu_0/f)^\epsilon$$

Thanks to slow running at the minimum.

The small cosmological constant



$$V_{IR}^{min} = -\epsilon \frac{2\sqrt{3}k v_0}{\kappa} \tanh \left(\frac{\kappa}{\sqrt{3}} (v_1 - v_0 (\mu_0/f)^\epsilon) \right) f^4 (\mu_0/f)^\epsilon$$

Thanks to slow running at the minimum.

1) Small CC and light dilaton signal the **approximate scale invariance** at the condensation scale:

$$V'(\phi) = dV/d\phi \longleftrightarrow \beta(\lambda) = d\lambda/d\log\mu$$

Change the bulk potential, change the running.

Chacko, Mishra, Stolarski '13

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Chacko, Mishra, Stolarski '13

2) The suppression is parametrically better than in **SUSY**:

SUSY

$$\Lambda_{(4)} = c(m_b^4 - m_f^4) \simeq c(m_b^2 + m_f^2)g_s^2 F_s^2$$

CFT

$$\Lambda_{(4)} = \tilde{c} \epsilon (4\pi)^2 f^4 \simeq \tilde{c} \epsilon \Lambda^2 f^2$$

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3) Our result is consistent with **Weinberg's no-go theorem**:

$\epsilon = 0$ can remove the CC, but $\epsilon \neq 0$ is required for a unique vacuum

The requirement is that a very light state must be in the spectrum!

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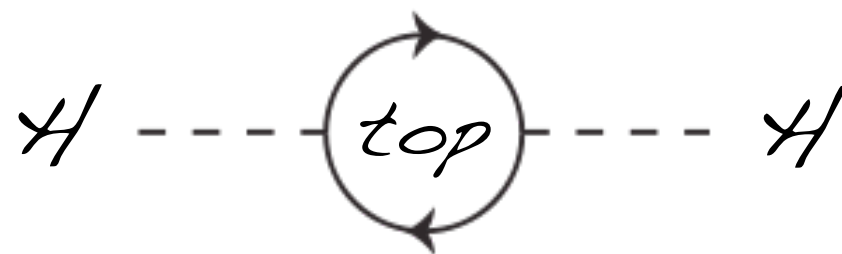
4) **UV contribution** to the CC?

Phenomenological Applications

1) A Higgs-like Dilaton

Why are particles (nearly) massless relative to Planckian scales? $v \ll M_p$

What protects the Higgs from getting a huge mass from quantum effects?

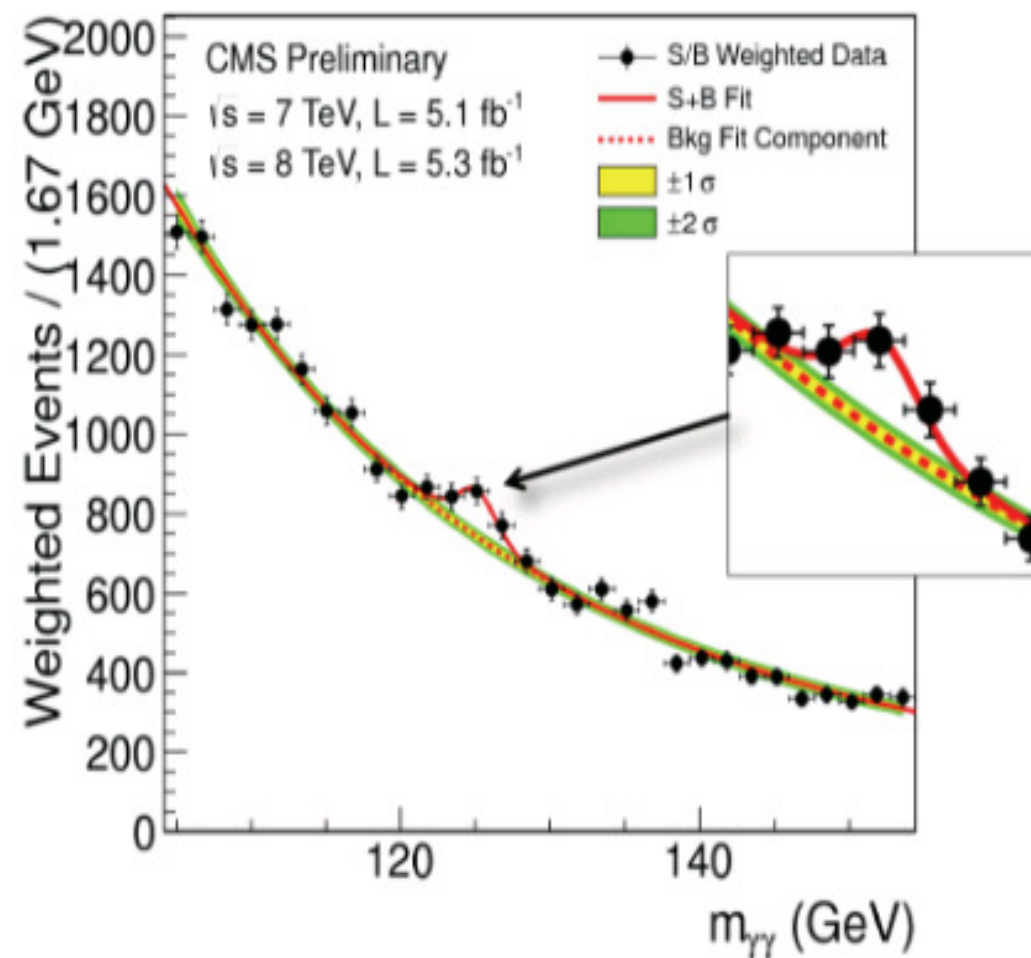


The answer pursued in this talk is

COMPOSITENESS

*We observed the 3 phase modes long ago =
longitudinal polarizations of W and Z gauge bosons*

But now we have observed the amplitude mode!

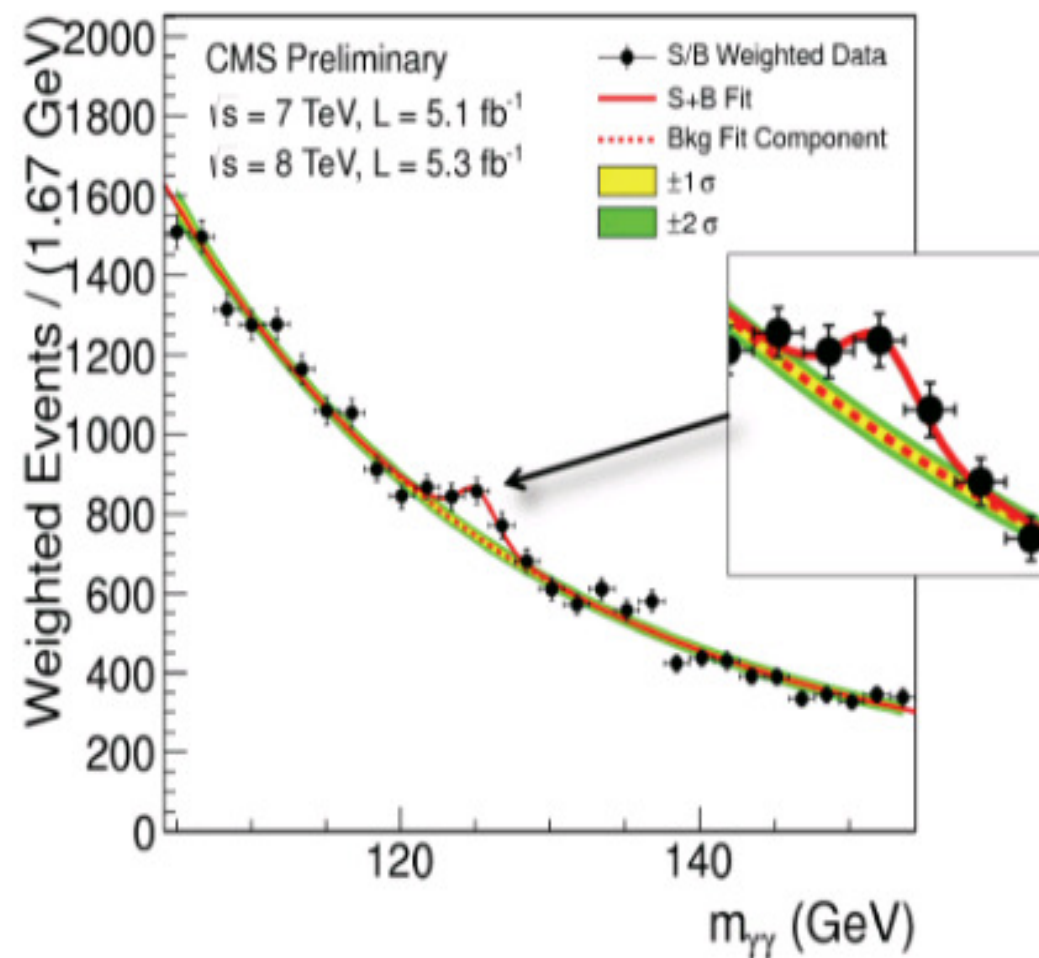


and nothing else!

*We have never encountered something like this in
particle physics*

*We observed the 3 phase modes long ago =
longitudinal polarizations of W and Z gauge bosons*

But now we have observed the amplitude mode!



Dilaton?

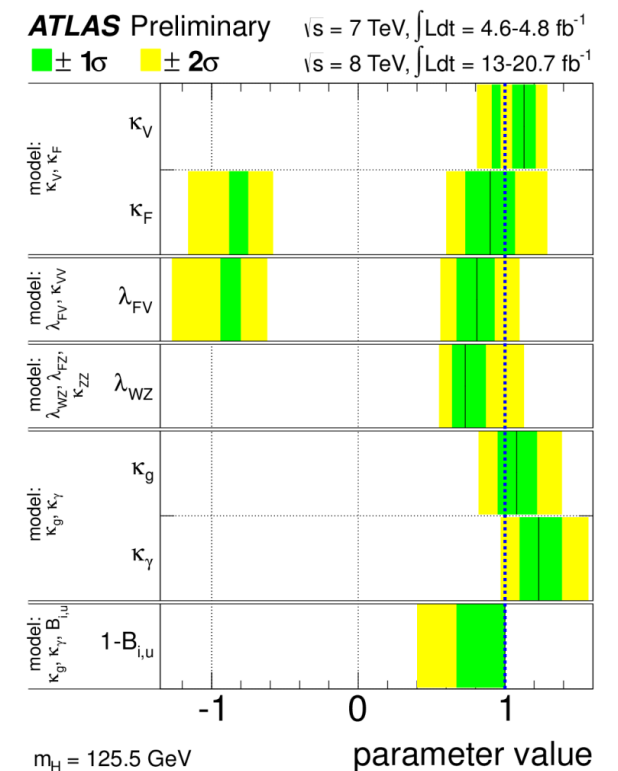
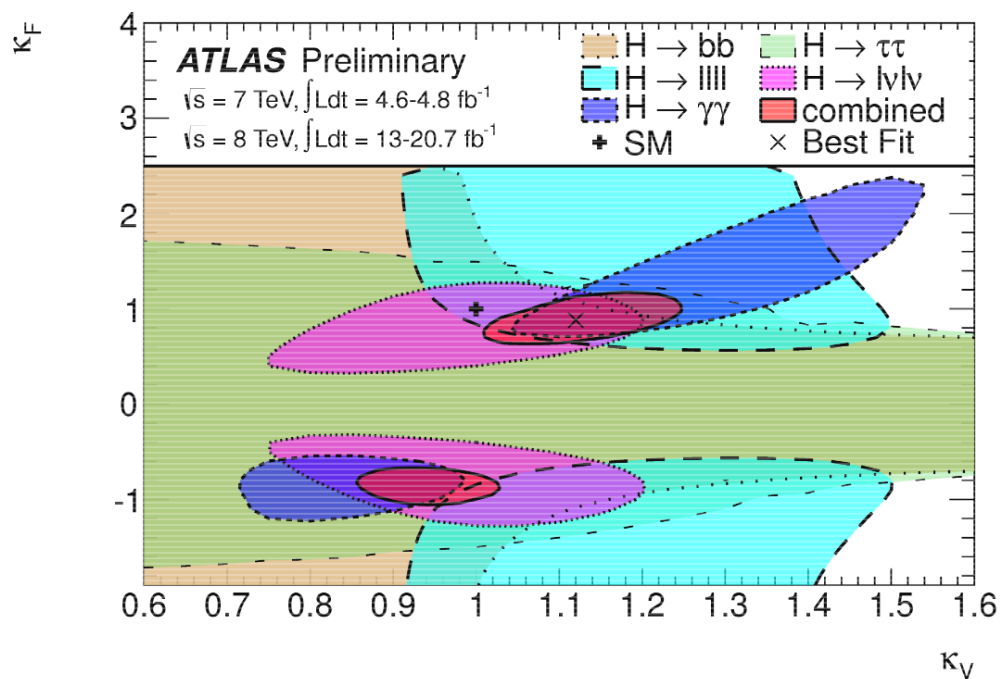
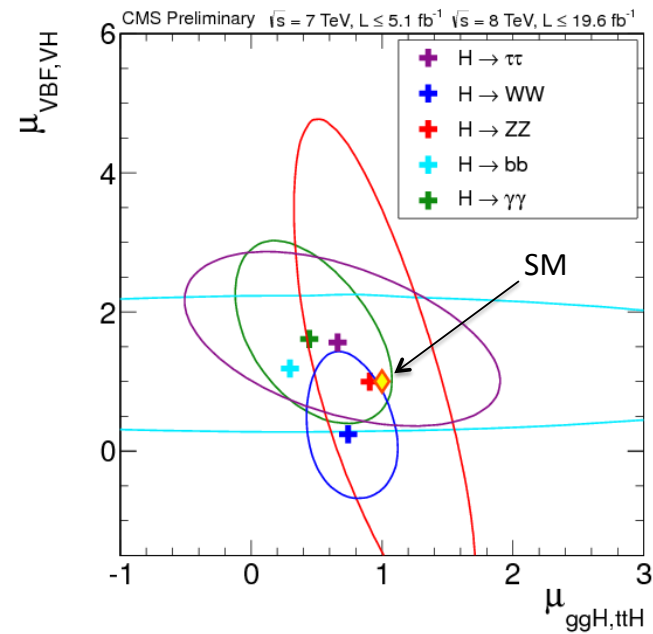
$$m_\chi \ll \Lambda \sim 4\pi f$$

$$\langle \chi \rangle \equiv f \sim v$$

and nothing else!

*We have never encountered something like this in
particle physics*

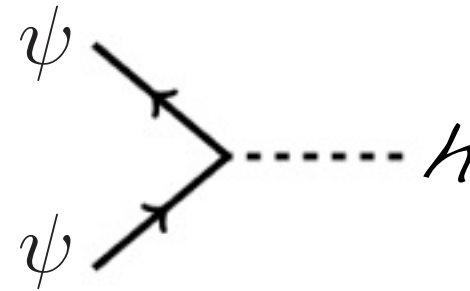
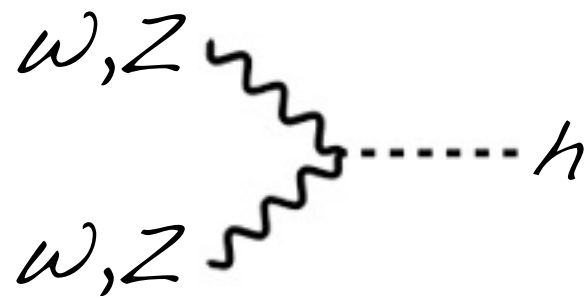
1



Customary parametrization of Higgs couplings

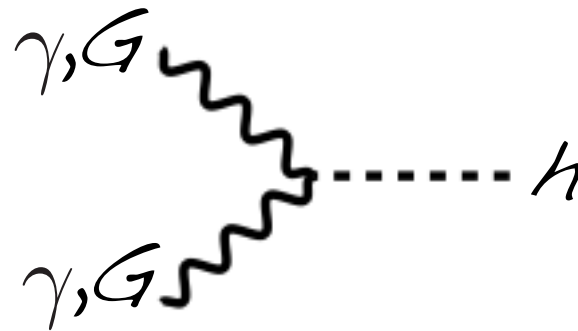
0-derivatives:

$$\mathcal{L}_{(0)} = \frac{h}{v} \left[c_V (2m_W^2 W_\mu^\dagger W^\mu + m_Z^2 Z_\mu Z^\mu) - c_t \sum_{\psi=u,c,t} m_\psi \bar{\psi} \psi - c_b \sum_{\psi=d,s,b} m_\psi \bar{\psi} \psi - c_\tau \sum_{\psi=e,\mu,\tau} m_\psi \bar{\psi} \psi \right]$$



2-derivatives:

$$\mathcal{L}_{(2)} = -\frac{h}{4v} \left[2c_{WW} W_{\mu\nu}^\dagger W^{\mu\nu} + c_{ZZ} Z_{\mu\nu} Z^{\mu\nu} + 2c_{Z\gamma} A_{\mu\nu} Z^{\mu\nu} + c_{\gamma\gamma} A_{\mu\nu} A^{\mu\nu} - c_{gg} G_{\mu\nu}^a G_{\mu\nu}^a \right]$$



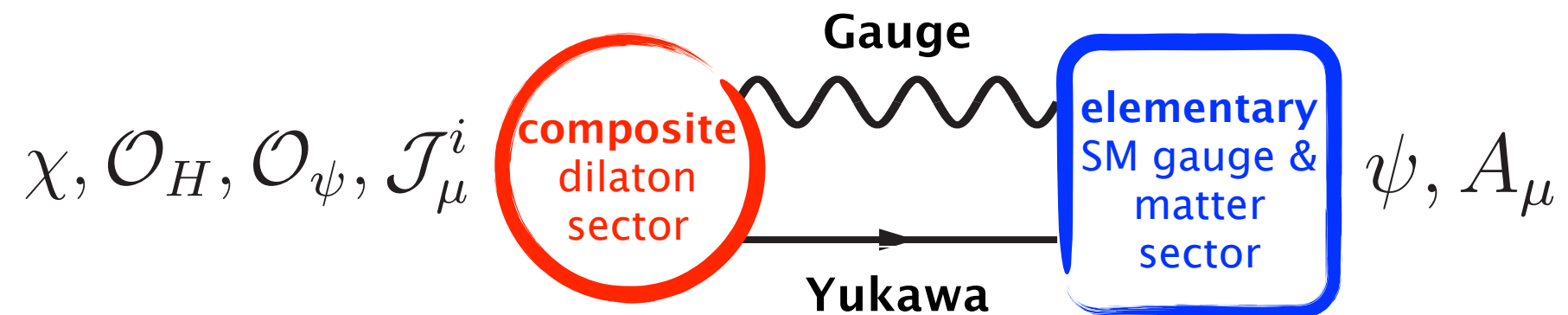
Standard Model

$$c_V = c_t = c_b = c_\tau = 1$$

$$c_{\gamma\gamma} = c_{Z\gamma} = c_{gg} = 0$$

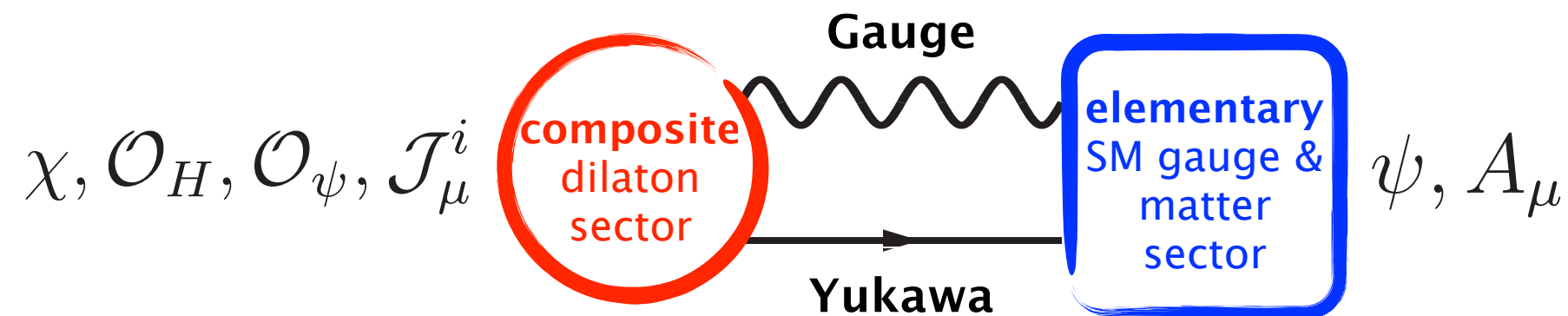
Dilaton

Couplings to SM fields dictated by scale invariance and its breaking



Dilaton

Couplings to SM fields dictated by scale invariance and its breaking



Scale invariance

$$\sum_i \langle \mathcal{O}_i \rangle \equiv f \rightarrow \chi$$

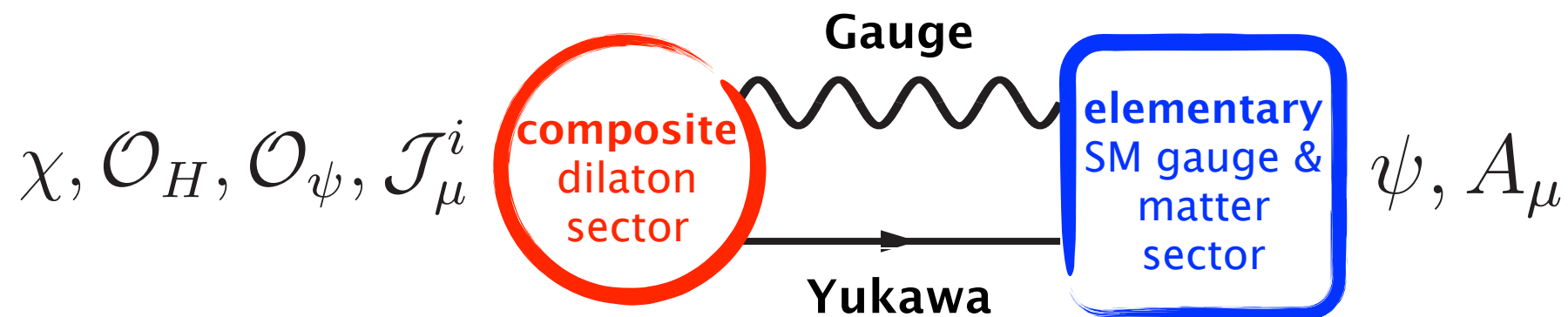
Electroweak symmetry breaking

$$\langle \mathcal{O}_H \rangle = v$$

$$v \rightarrow \frac{v}{f} \chi$$

Dilaton

Couplings to SM fields dictated by scale invariance and its breaking



Scale invariance

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Scale explicit breaking

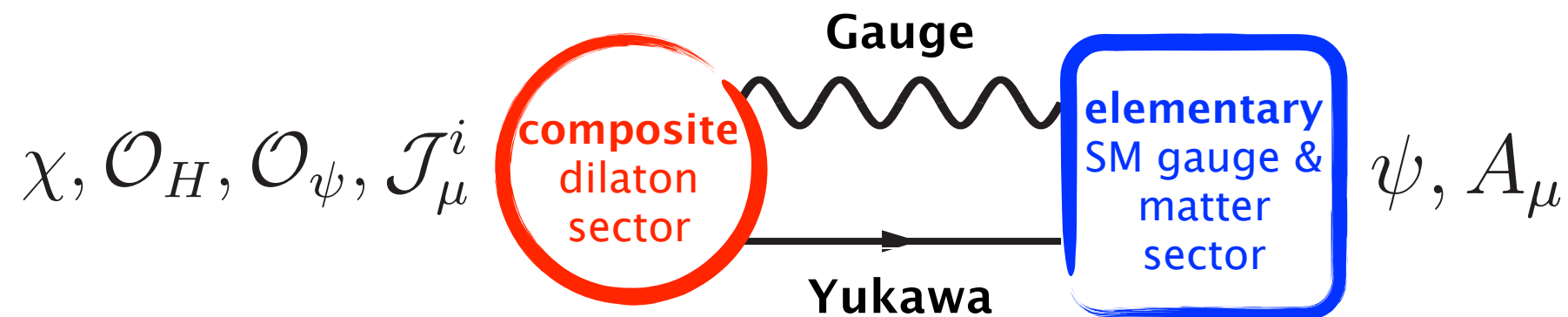
Gauge couplings

$$A_\mu^i \mathcal{J}^{\mu i}$$

$$d(A_i) = 1 - \frac{b_{UV}^i}{8\pi^2} + \frac{b_{IR}^i}{8\pi^2}$$

Dilaton

Couplings to SM fields dictated by scale invariance and its breaking



Scale invariance

$$\sum_i \langle \mathcal{O}_i \rangle \equiv f \rightarrow \chi$$

Electroweak symmetry breaking

$$\langle \mathcal{O}_H \rangle = v$$

$$v \rightarrow \frac{v}{f} \chi$$

Scale explicit breaking

Gauge couplings

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$$d(A_i) = 1 - \frac{b_{UV}^i}{8\pi^2} + \frac{b_{IR}^i}{8\pi^2}$$

Yukawa couplings

$$\psi \mathcal{O}_\psi$$

$$d(\mathcal{O}_\psi) = 3/2 - \gamma_\psi$$

Dilaton

$$c_V = \frac{v}{f}$$

$$c_f = \frac{v}{f}(1 + \gamma_f)$$

$$c_{\gamma\gamma,gg} = \frac{(g'^2, g_S^2)}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(EM,3)} - b_{UV}^{(EM,3)} \right)$$

$$c_{Z\gamma} \sim \frac{g^2}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(2)} - b_{UV}^{(2)} \right)$$

Dilaton

<1 (model independent)

$$c_V = \frac{v}{f}$$

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Dilaton

scaling anomalies
<1, >1 (model dependent)

$$c_V = \frac{v}{f}$$

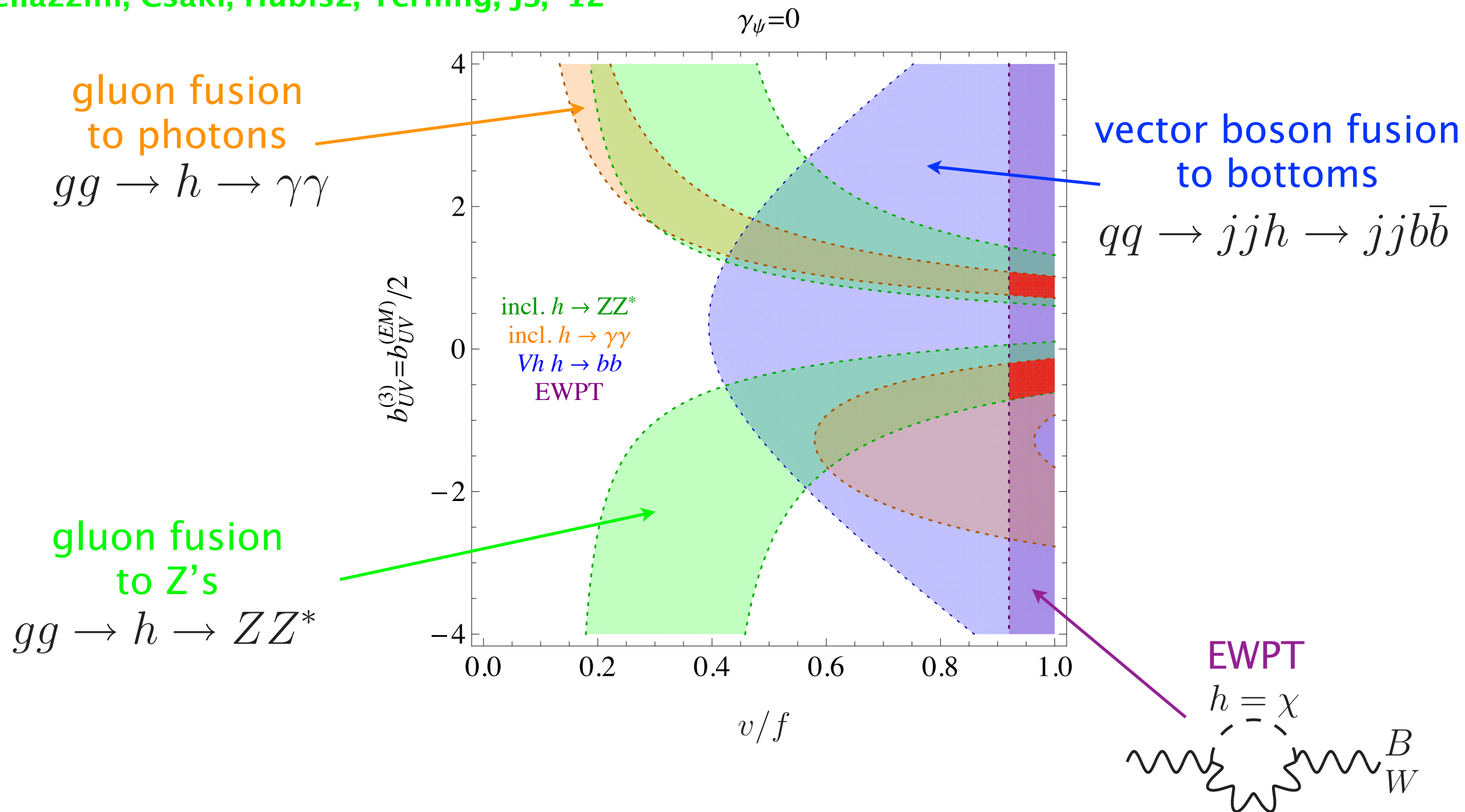
$$c_f = \frac{v}{f} (1 + \gamma_f)$$

$$c_{\gamma\gamma,gg} = \frac{(g'^2, g_S^2)}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(EM,3)} - b_{UV}^{(EM,3)} \right)$$

$$c_{Z\gamma} \sim \frac{g^2}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(2)} - b_{UV}^{(2)} \right)$$

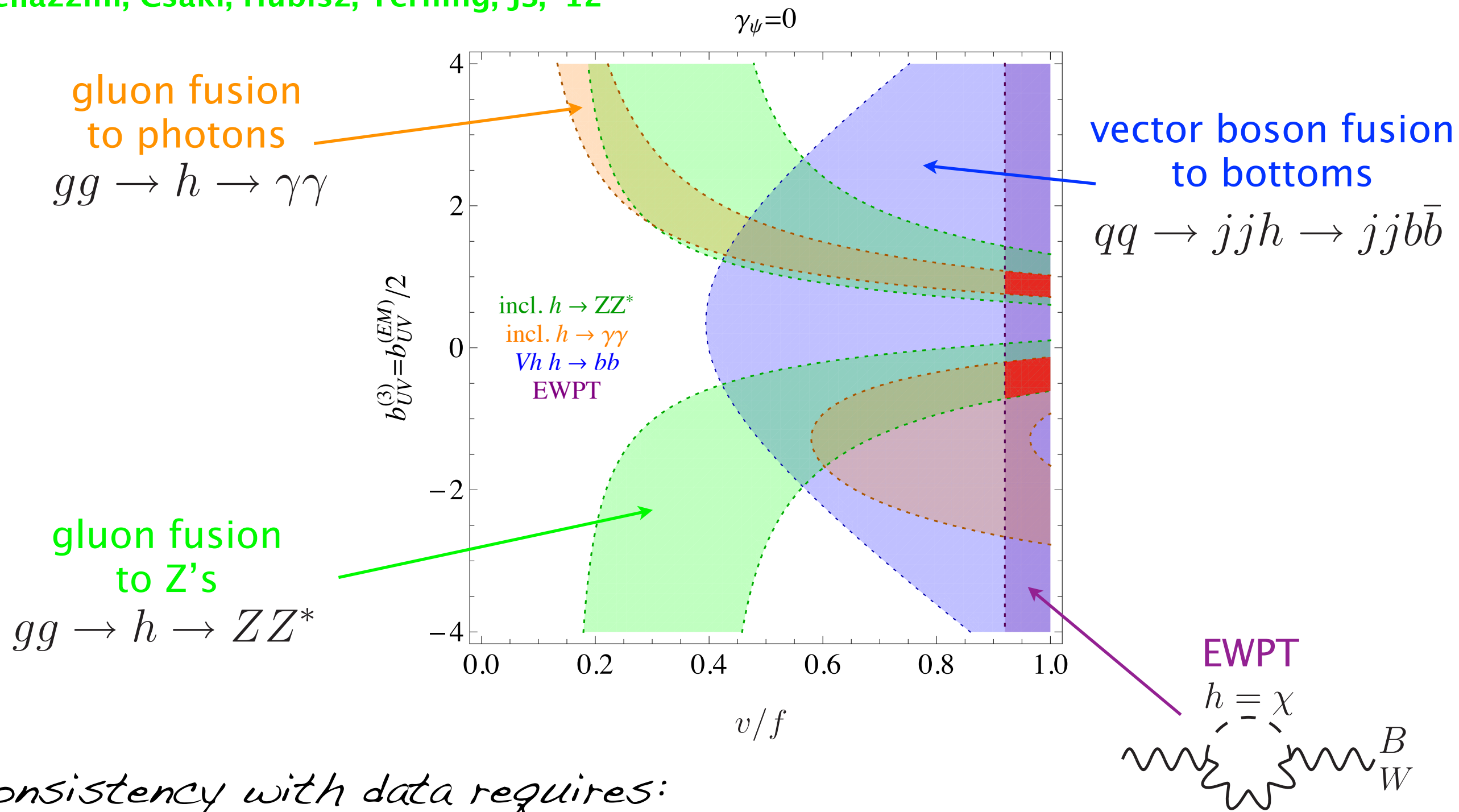
Contrasting with Higgs Data

Bellazzini, Csaki, Hubisz, Terning, JS, '12



Contrasting with Higgs Data

Bellazzini, Csaki, Hubisz, Terning, JS, '12



Consistency with data requires:

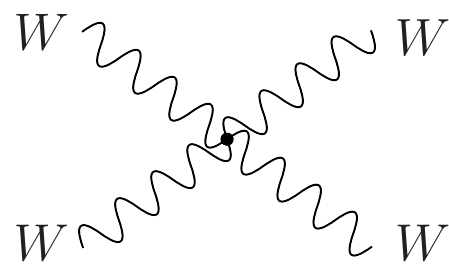
$$\frac{v}{f} \simeq 1$$

$$b^{(i)}, \gamma_f \lesssim O(1) \quad \text{consistent with } m_\chi \ll 4\pi f$$

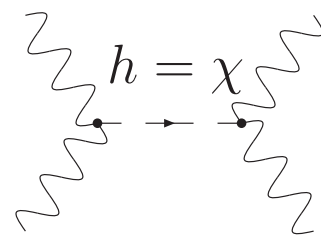
The genuine effect of compositeness is the growth of scattering amplitudes with energy

WW scattering

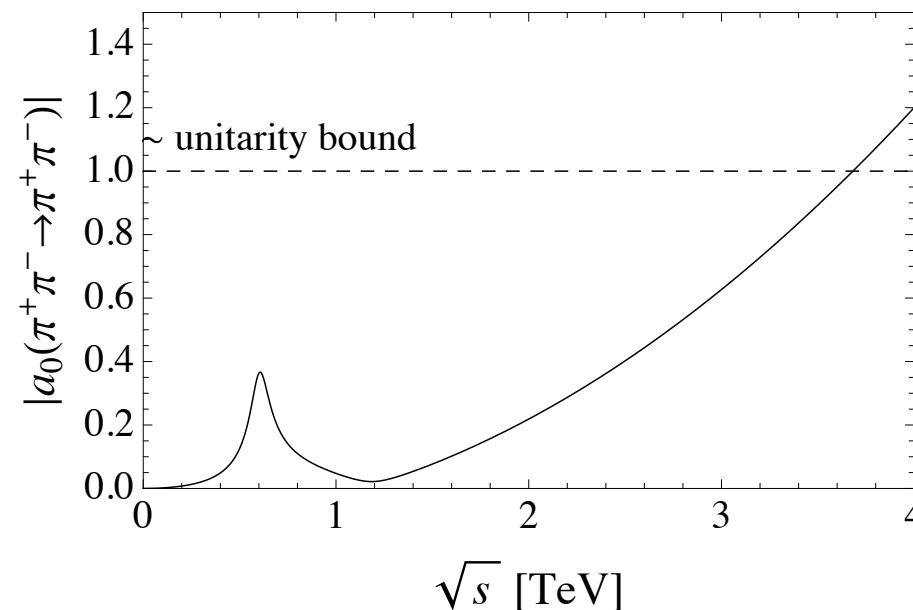
Partial unitarization only. There is a $O(s)$ growth



+



$$\mathcal{A}(s) \simeq \frac{s}{v^2} (1 - c_V^2) = s \frac{1 - v^2/f^2}{v^2}$$



Customary parametrization of double (triple) Higgs couplings

$$\mathcal{L}_{(0)}^{h^2} = \frac{h^2}{v^2} \left[\frac{d_V}{2} (2m_W^2 W_\mu^\dagger W^\mu + m_Z^2 Z_\mu Z^\mu) - d_\psi m_\psi \bar{\psi} \psi \right]$$

$$\mathcal{L}_{(2)}^{h^2} = \frac{h^2}{v^2} \left[\frac{d_{gg}}{2} G_{\mu\nu}^a G^{\mu\nu a} + \dots \right]$$

$$\mathcal{L}_{(0)}^{h^3} = -c_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3$$

Standard Model

$$d_V = c_3 = 1$$

$$d_\psi = d_{gg} = 0$$

Dilaton

$$d_V = \frac{v^2}{f^2}$$

$$d_\psi = \frac{1}{2} \frac{v^2}{f^2} \gamma_\psi$$

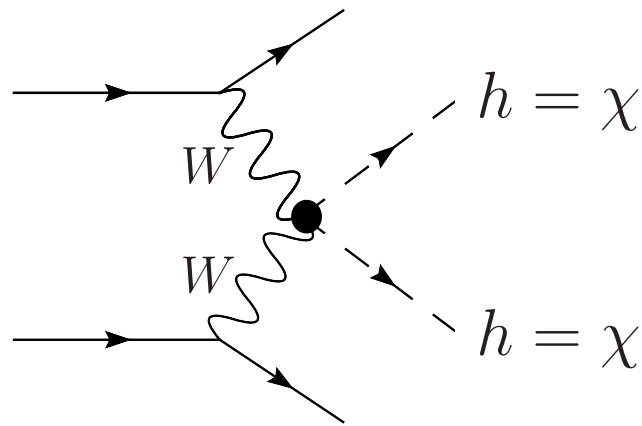
$$d_{gg} = -\frac{g_s^2}{32\pi^2} \frac{v^2}{f^2} \left(b_{IR}^{(3)} - b_{UV}^{(3)} \right)$$

$$c_3 = \frac{1}{3} \frac{v}{f} \left(5 + \alpha \frac{m_\chi^2}{(4\pi f)^2} \right)$$

The genuine effect of compositeness is the growth of scattering amplitudes with energy, in particular W_L and h

WW to hh scattering

There is NO $O(s)$ growth, but $O(s^2)$!



$$\mathcal{A}(s) \simeq \frac{s}{v^2} (d_V - c_V^2) \simeq 0 + O(s^2/f^4)$$

$$\sqrt{d_V} = c_V = \frac{v}{f}$$

$$\frac{a_{2,4}}{(4\pi)^2} \frac{(\partial\chi)^4}{\chi^4}$$

in the dilaton
“chiral” Lagrangian

Differential feature w.r.t. composite Higgs:

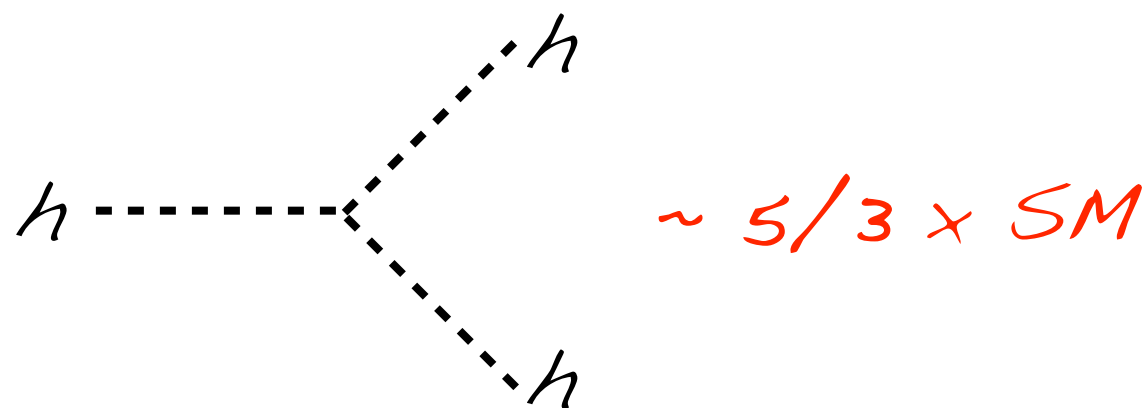
dilaton is NOT part of $SU(2)$ doublet

$$\mathcal{A}(WW \rightarrow WW) \neq \mathcal{A}(WW \rightarrow \chi\chi)$$

$$s \rightarrow \infty$$

Implications: Double Dilaton Production

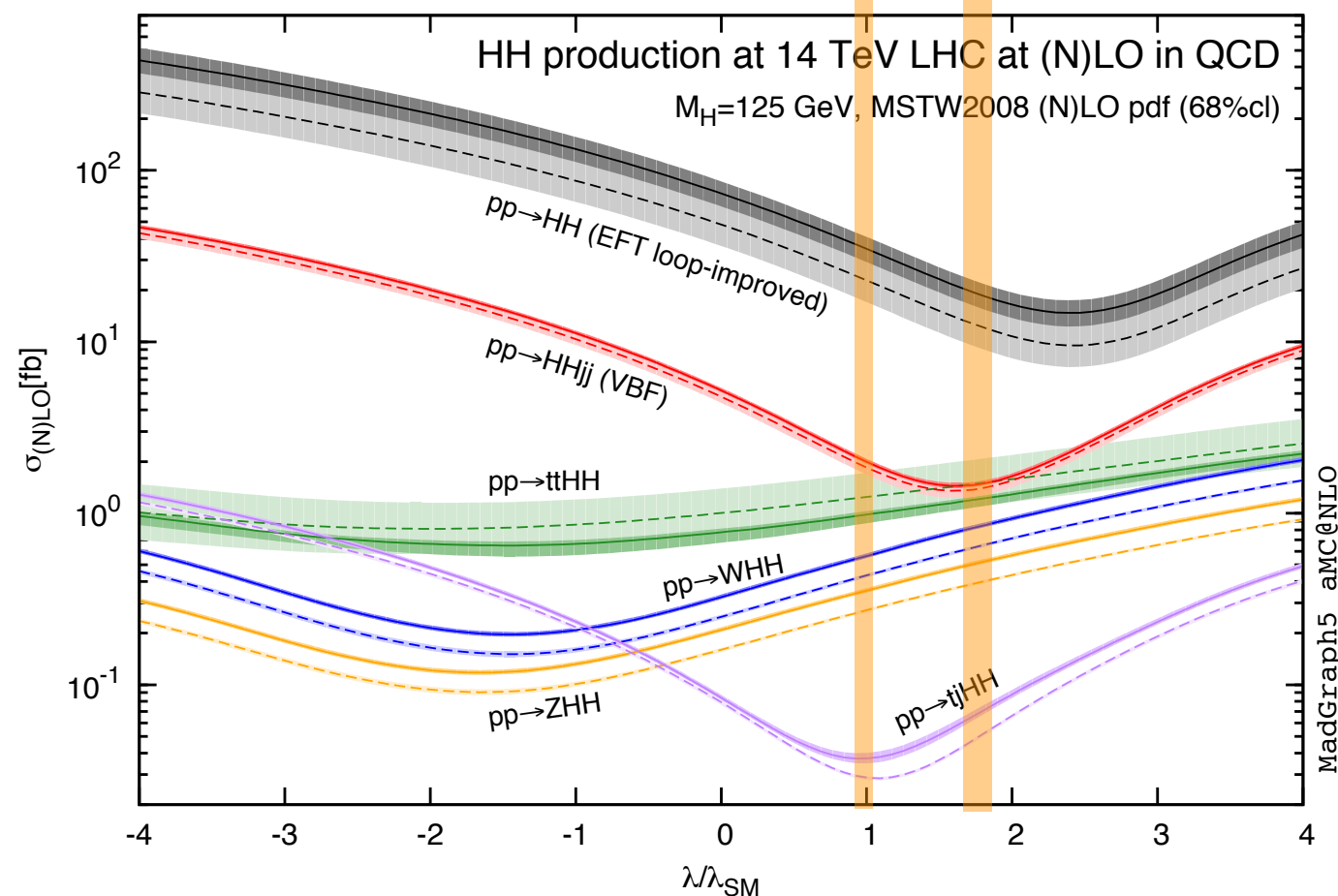
There is one differential feature w.r.t the SM Higgs even if $v/f \sim 1$ and no anomalous dimensions!



$\sim 5/3 \times SM$

Dilaton

SM



Frederix et al '14

Phenomenological Applications

*2) Cosmological Phase
Transitions*

There is one very important consequence of a true spontaneous breaking of scale invariance

$$\Lambda_{eff} = V(\langle\chi\rangle) \sim \epsilon \langle\chi\rangle^4 \quad m_\chi^2 \sim \epsilon \langle\chi\rangle^2$$

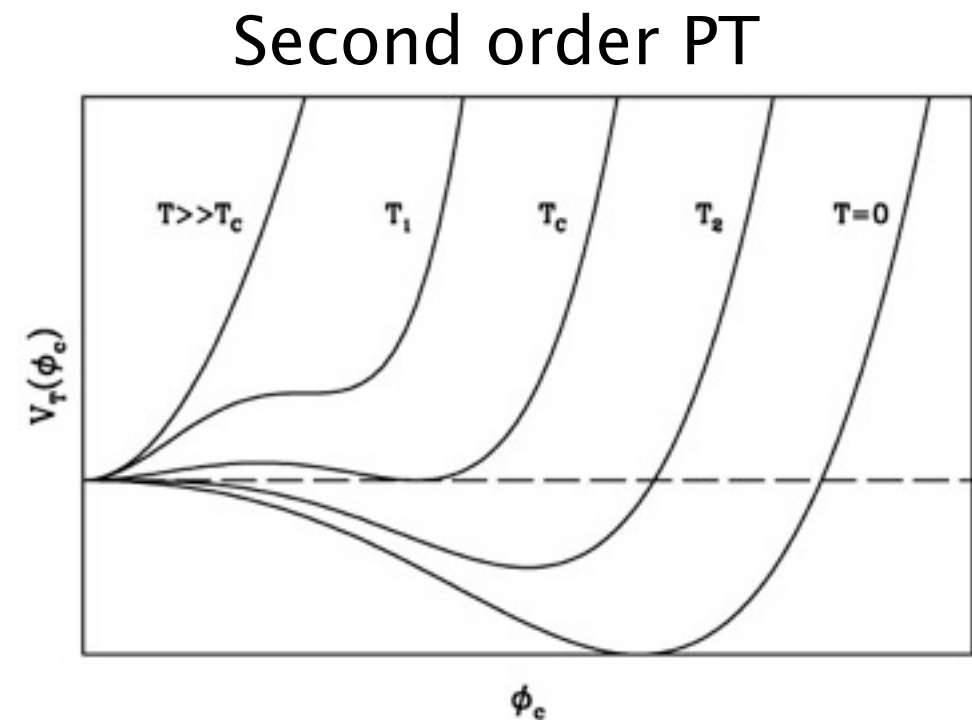
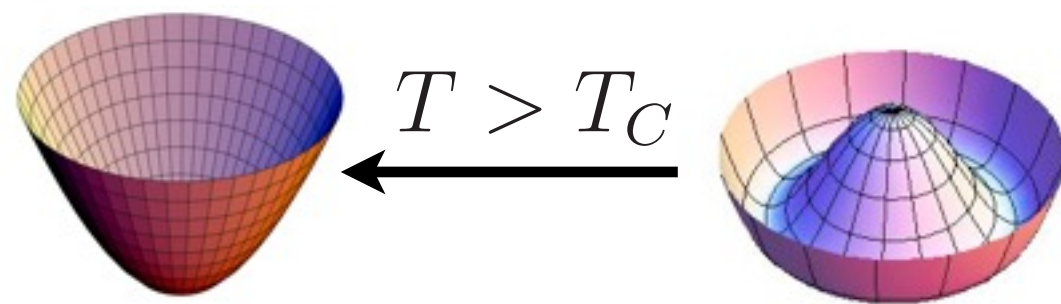
Could this occur in any of the known phase transitions?

This is a very speculative idea, but the next question per se is very interesting:

How can we learn anything about the CC?

Phase Transitions in the Early Universe

As the Universe expands, it cools off, and phase transitions take place (QCD, Electroweak,...)



Restoration of symmetry at high Temperature.

The energy densities change during PT's, and the Universe is sensitive to it.

Homogeneous & isotropic (flat) Universe

$$ds^2 = -dt^2 + a^2(t)dx_i^2$$

Einstein equations $G_{\mu\nu} = T_{\mu\nu}$

Assuming a perfect fluid: $T^\mu_\nu = \begin{pmatrix} \rho & 0 & 0 & 0 \\ 0 & -p & 0 & 0 \\ 0 & 0 & -p & 0 \\ 0 & 0 & 0 & -p \end{pmatrix}$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{3}\rho$$

$$\frac{\ddot{a}}{a} = -\frac{1}{6}(\rho + 3p)$$

Radiation domination

$$\rho(a) \sim a^{-4}$$

$$a(t) \sim t^{1/2}$$

Matter domination

$$\rho(a) \sim a^{-3}$$

$$a(t) \sim t^{2/3}$$

CC domination

$$\rho(a) \sim a^0$$

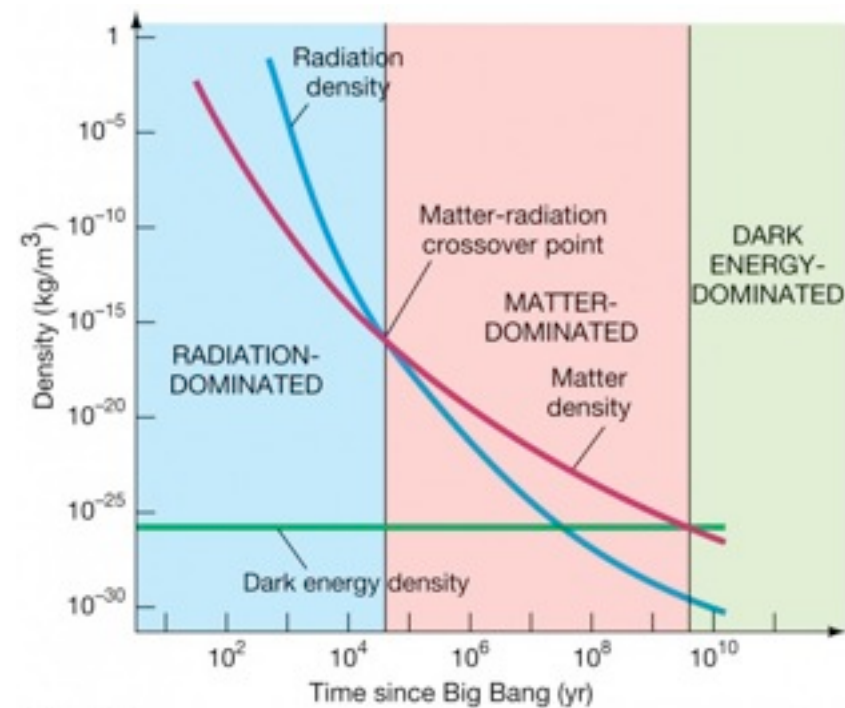
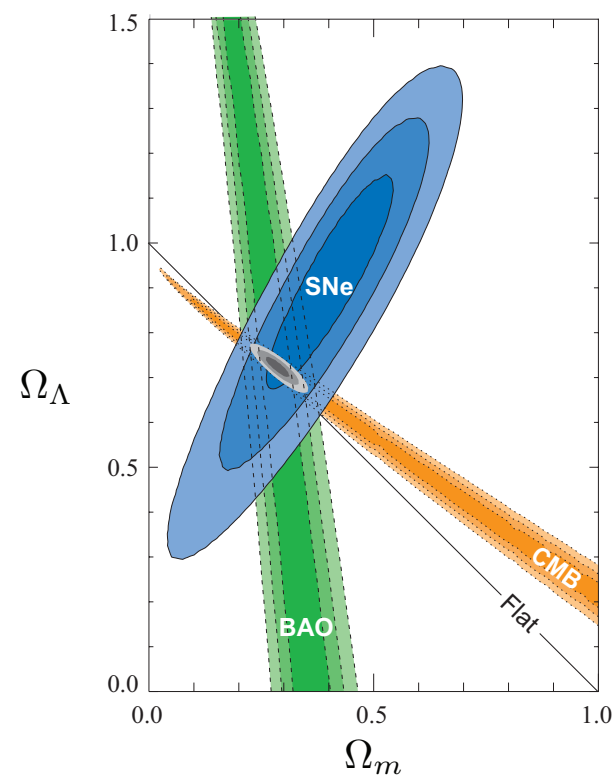
$$a(t) \sim e^{Ht}$$

Homogeneous & isotropic (flat) Universe

$$ds^2 = -dt^2 + a^2(t)dx_i^2$$

$$\text{Einstein equations } G_{\mu\nu} = T_{\mu\nu}$$

*By measuring energy densities today,
we obtain a beautiful picture for the hot early Universe*

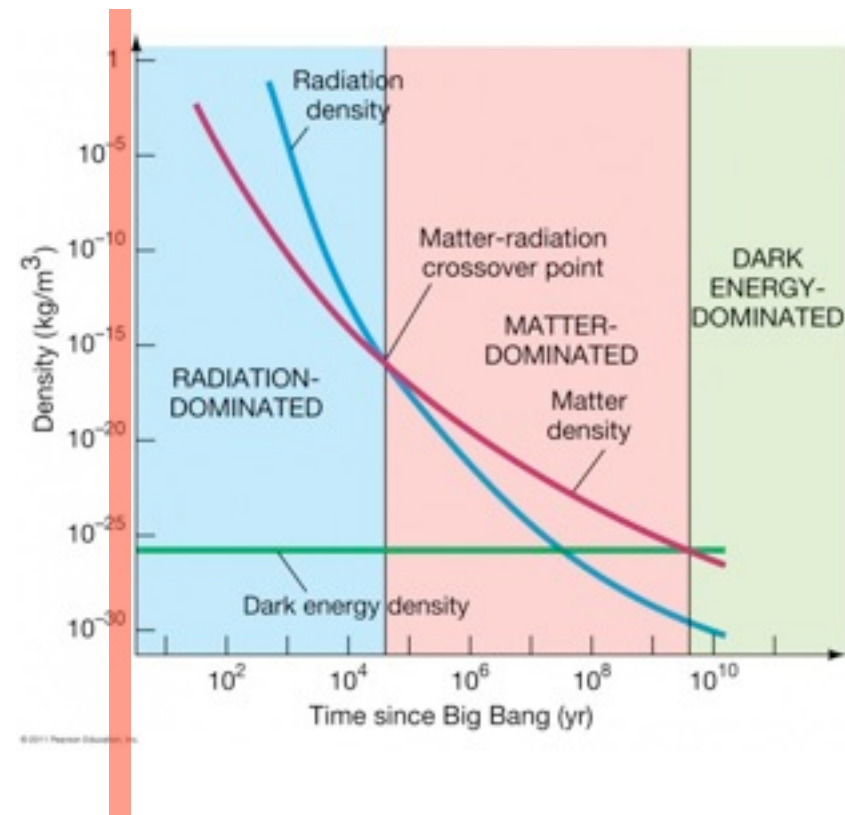
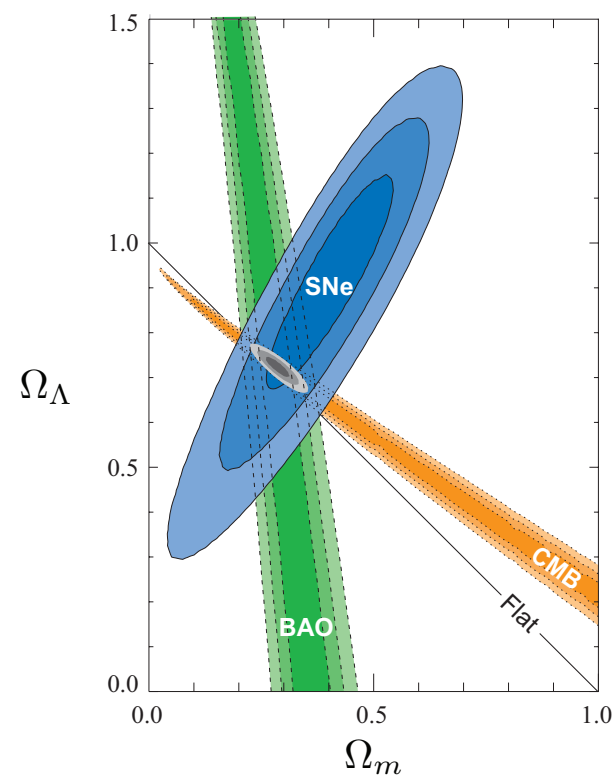


Homogeneous & isotropic (flat) Universe

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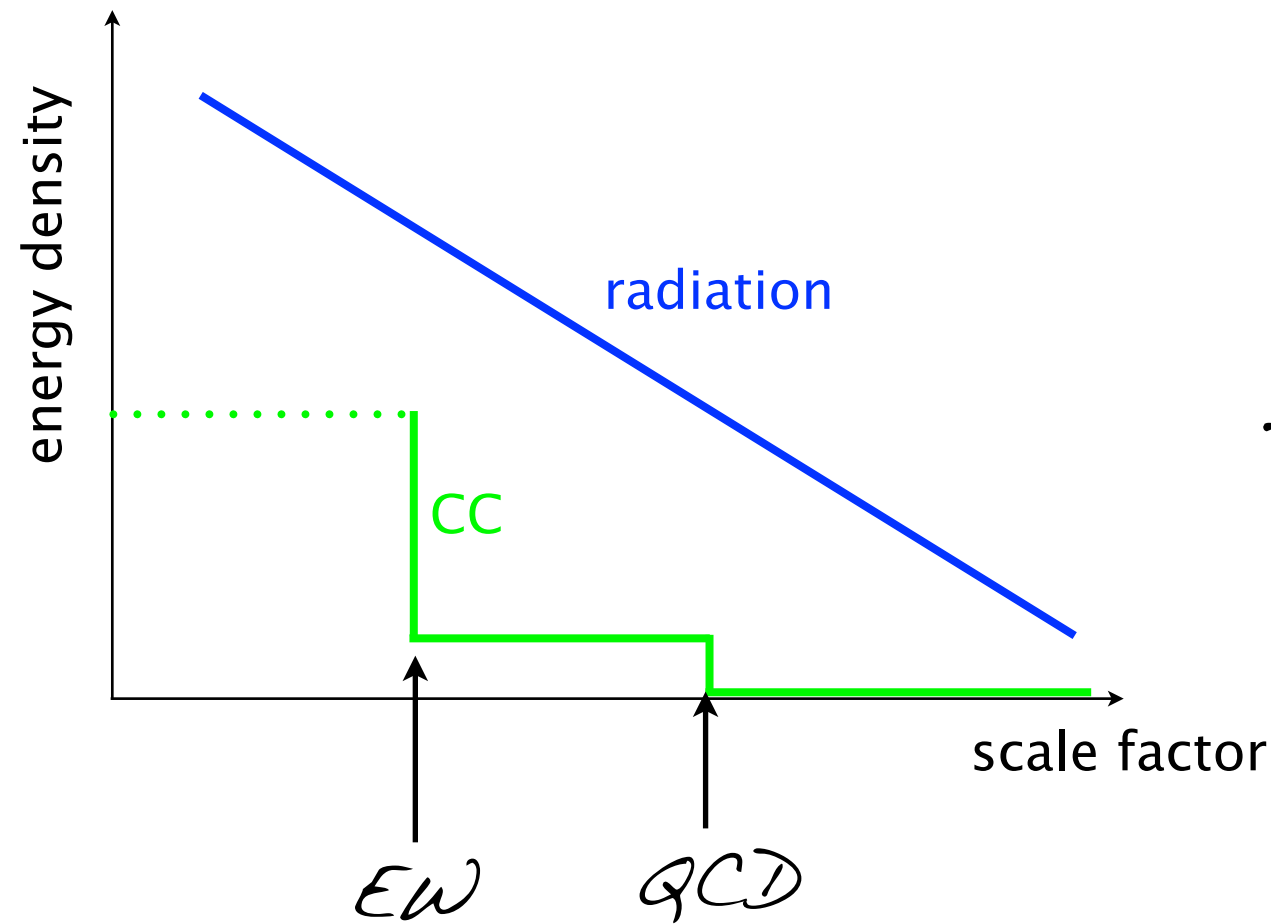
*By measuring energy densities today,
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But we are interested in what happens outside here!

Early Universe Evolution

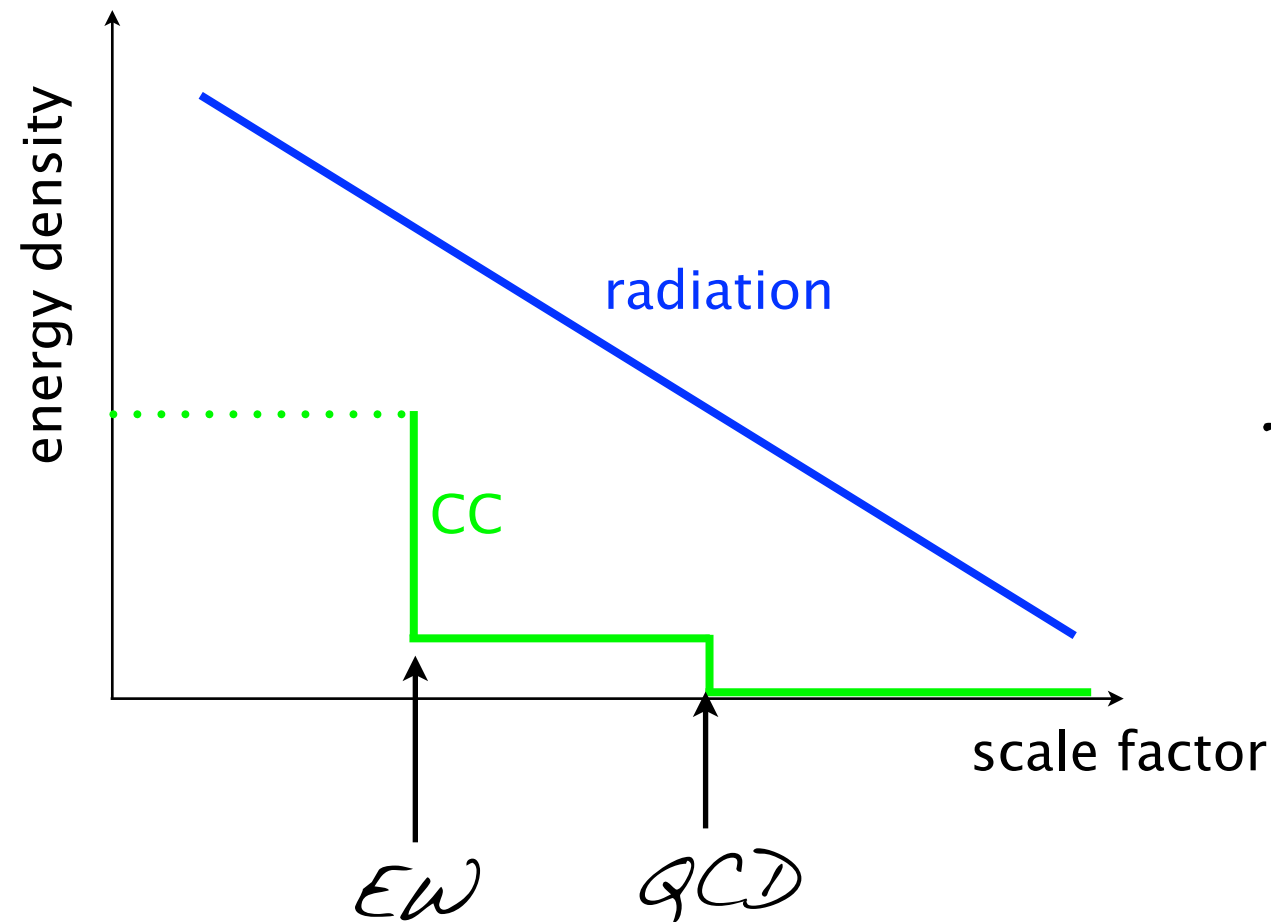
Actually, what happens in the very early Universe is similar to this:



*The CC jumps at each
phase transition!*

*To end up at the very small
value we observe today*

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The CC jumps at each phase transition!

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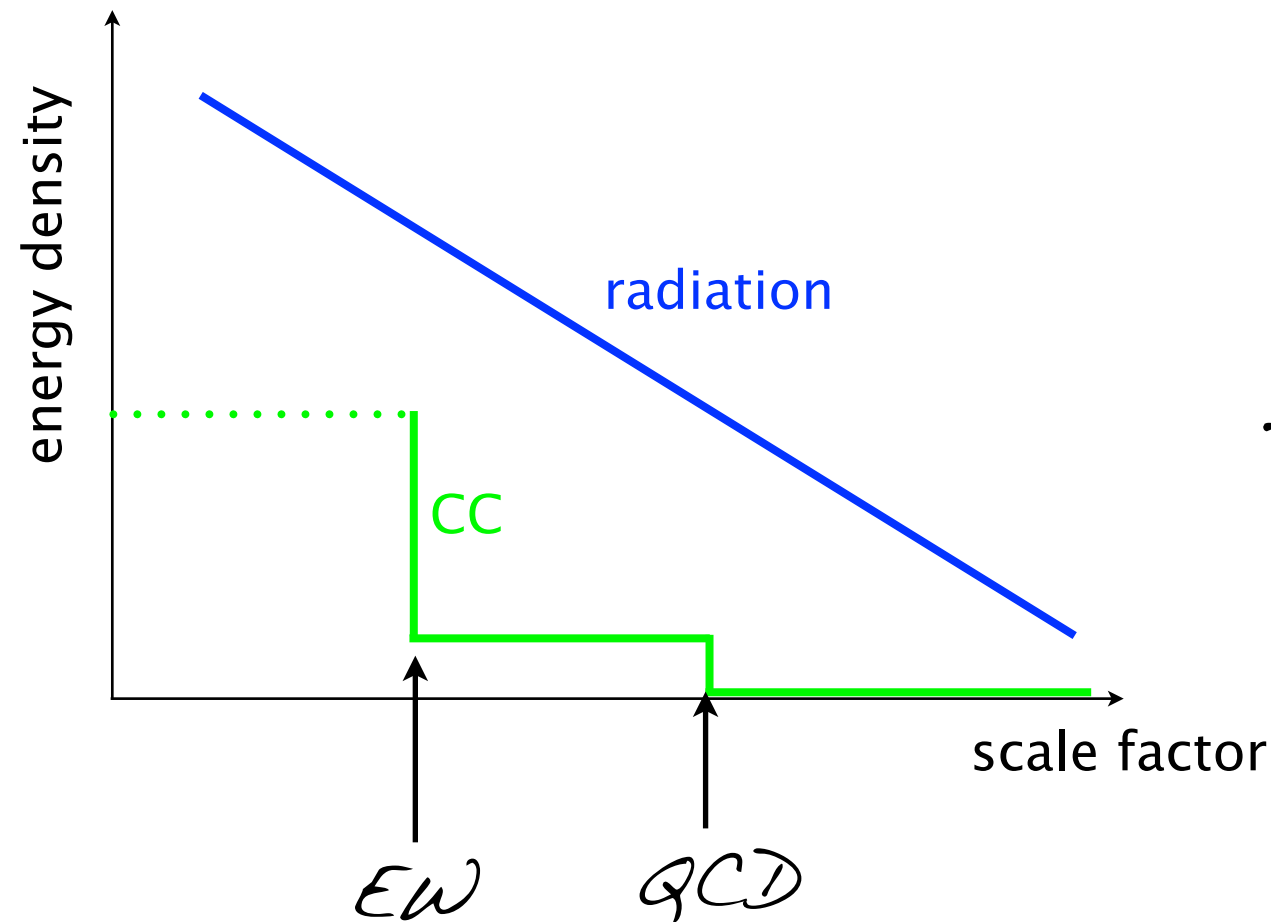
$$V(\phi) = V_0 - m^2\phi^2 + \lambda\phi^4$$

$$T_{PT} \sim -\langle\phi\rangle \sim \frac{m}{\sqrt{g}} \quad \text{and} \quad V(\langle\phi\rangle) \sim 0 \Rightarrow V_0 \sim \frac{m^4}{g}$$

At the PT, radiation and CC are closest

$$\rho_{cc} \sim V_0 \lesssim \rho_{\text{radiation}} \sim T_{PT}^4 \sim \frac{m^4}{g^2}$$

Actually, what happens in the very early Universe is similar to this:



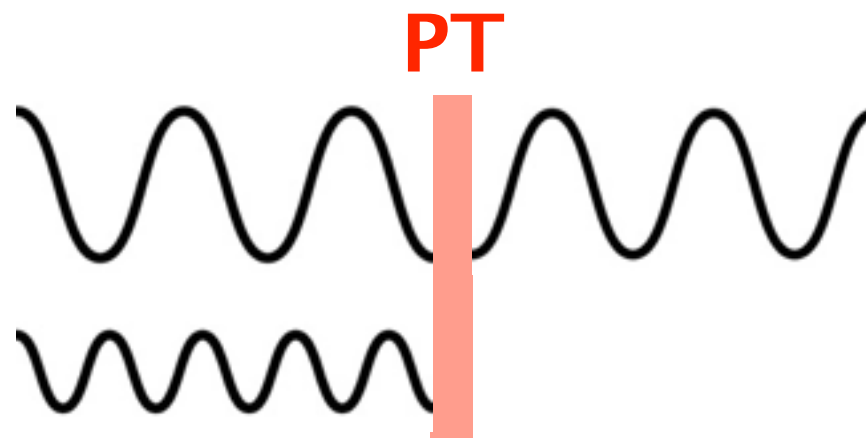
The CC jumps at each phase transition!

To end up at the very small value we observe today

$$V(\langle\phi\rangle) \sim V_0 \sim 0$$

How could we tell if there has been a jump or NOT?

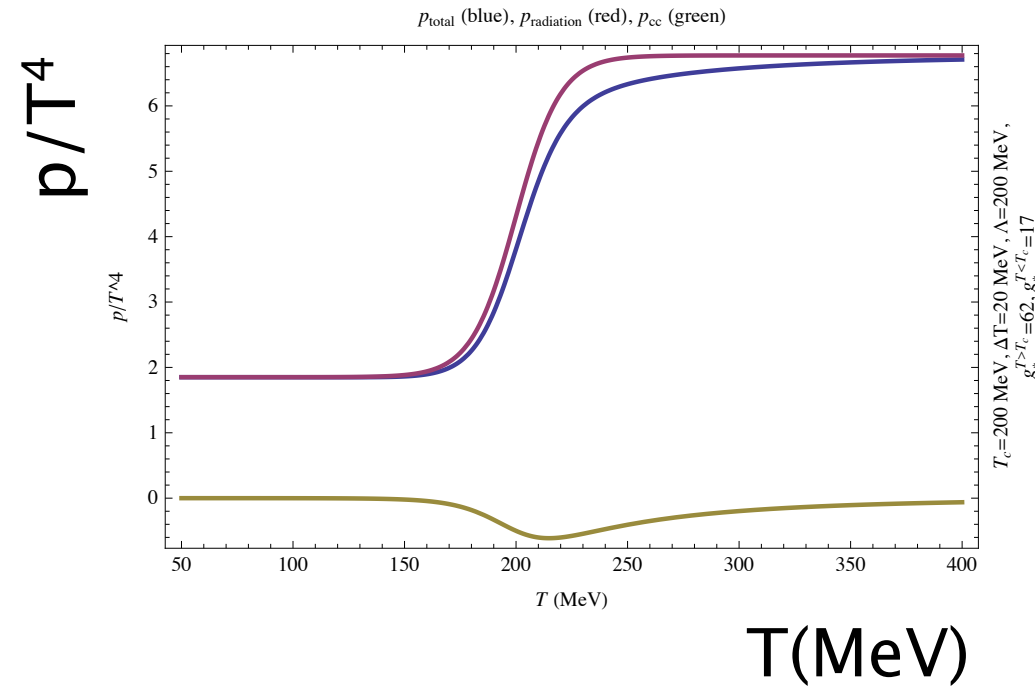
Certainly gravitational waves will be affected and will reach us later



The Free energy is continuous (decreasing) & $F = p$

Pressure ansatz:

Matches well lattice simulations



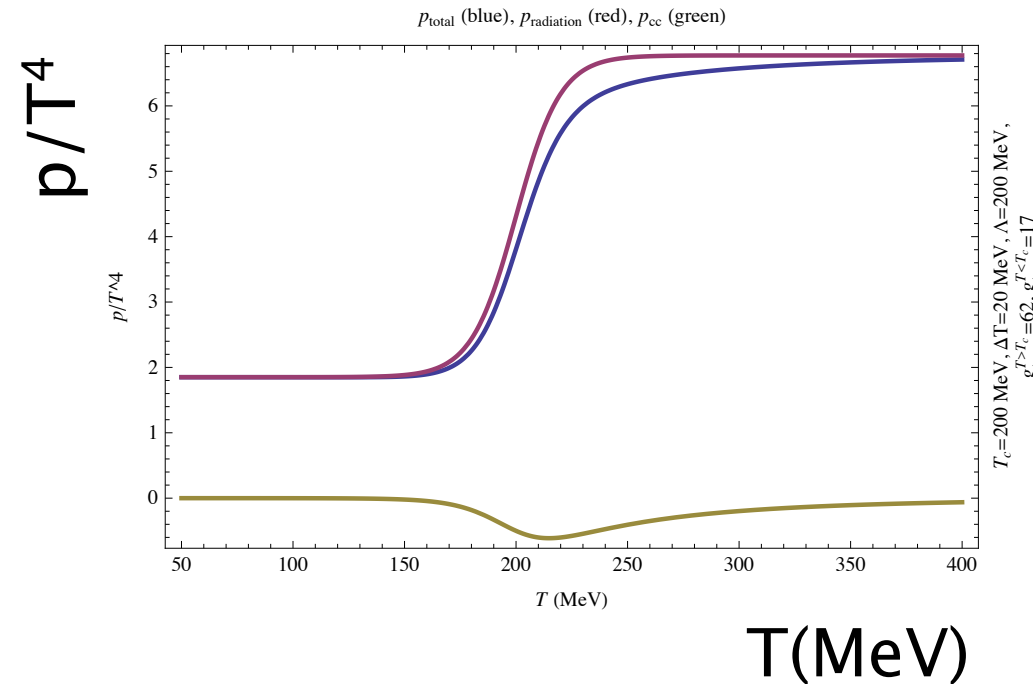
The number of degrees of freedom changes

The CC disappears

The Free energy is continuous (decreasing) & $\mathcal{F} = p$

Pressure ansatz:

Matches well lattice simulations



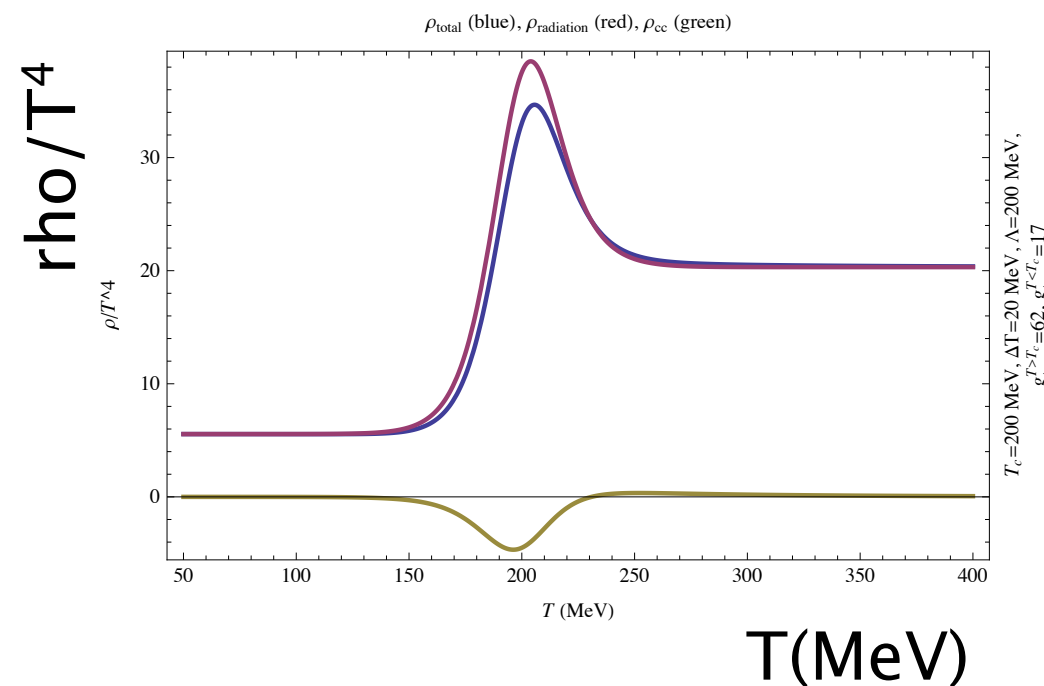
The number of degrees of freedom changes

The CC disappears

Entropy is conserved:

$$\frac{dp}{dT} = \frac{p + \rho}{T}$$

Energy density:



We wish to compute the power spectrum

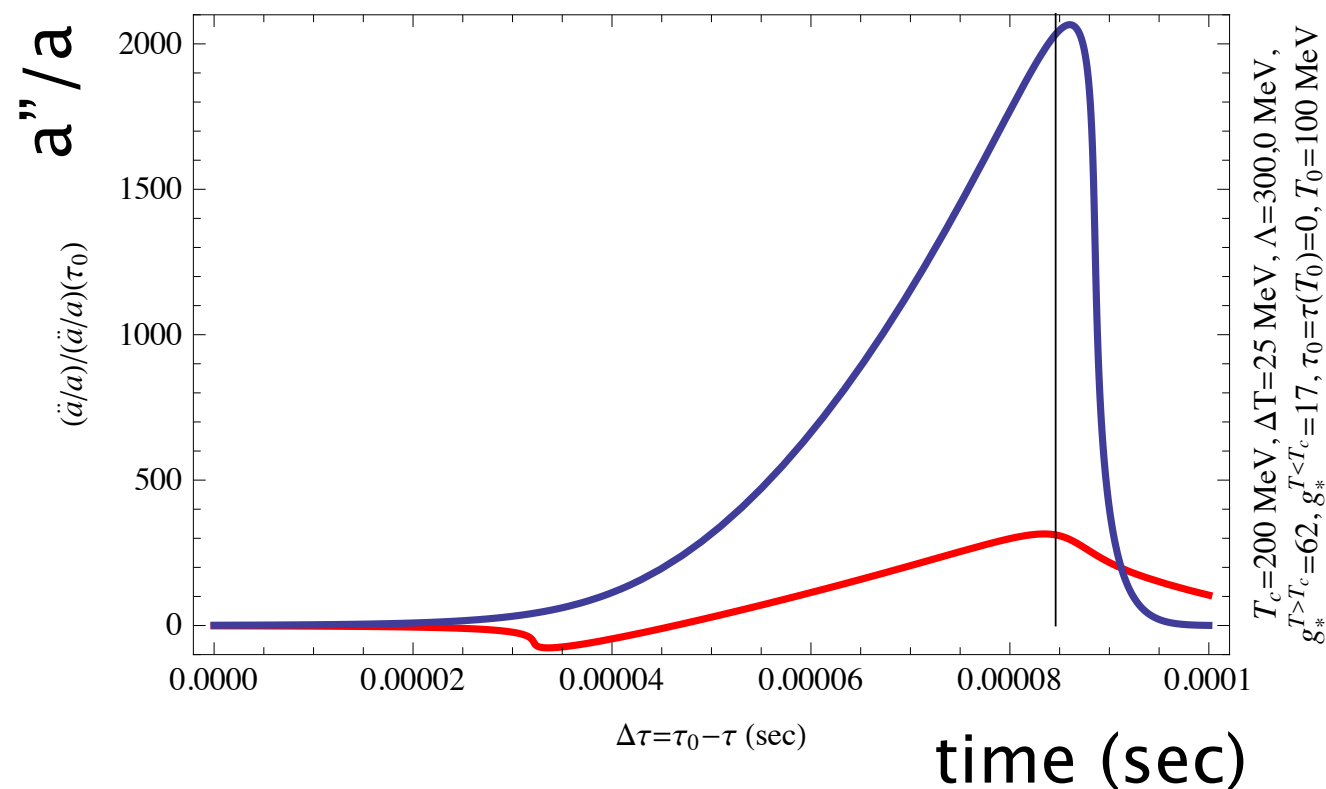
$$\Delta_t^2(\tau, k) = \frac{2k^3}{2\pi^2} \langle |h_k(\tau)|^2 \rangle$$

Wave equation

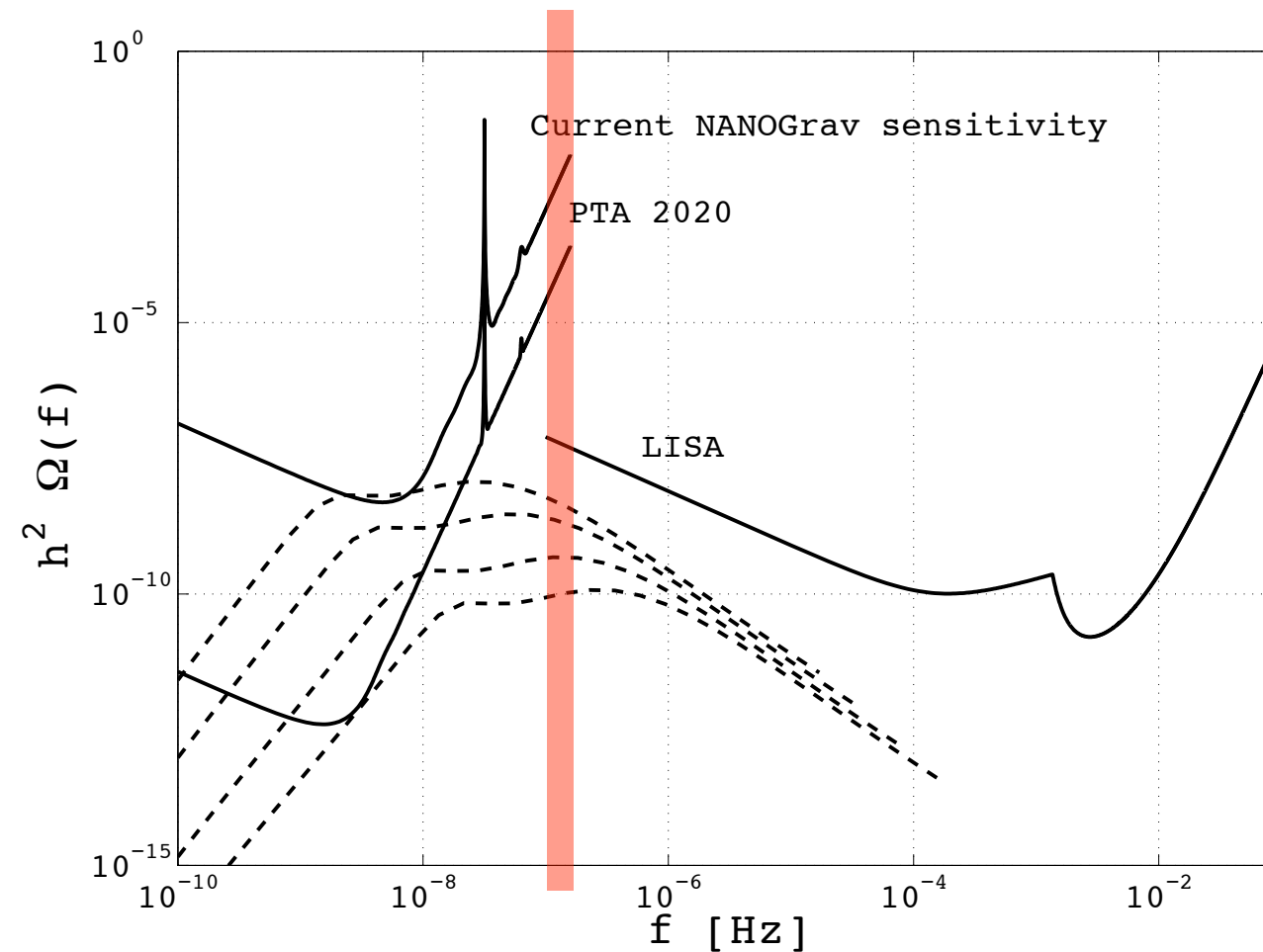
$$(ah_k)'' + \left(k^2 - \frac{a''}{a} \right) (ah_k) = 0$$

de Sitter space

$$a''/a = 2/\tau^2$$



Unfortunately, for the QCD phase transition, experiments are not very sensitive



Caprini et al '10

But who knows in the future?! Or other PT's?!

*Approximate spontaneous breaking of scale invariance
offers a NATURAL way to obtain a light scalar
and to suppress the Cosmological Constant*

Is this possibility realized in Nature?

**A Higgs-like Dilaton
Dilaton in Phase Transitions
QCD?**

...

We just have to wait and see



Thank you for your attention