

What the Higgs can tell us about Warped Extra Dimensions

- in collaboration with R. Malm and M. Neubert
- based on [hep-ph /1303.5703] and current work

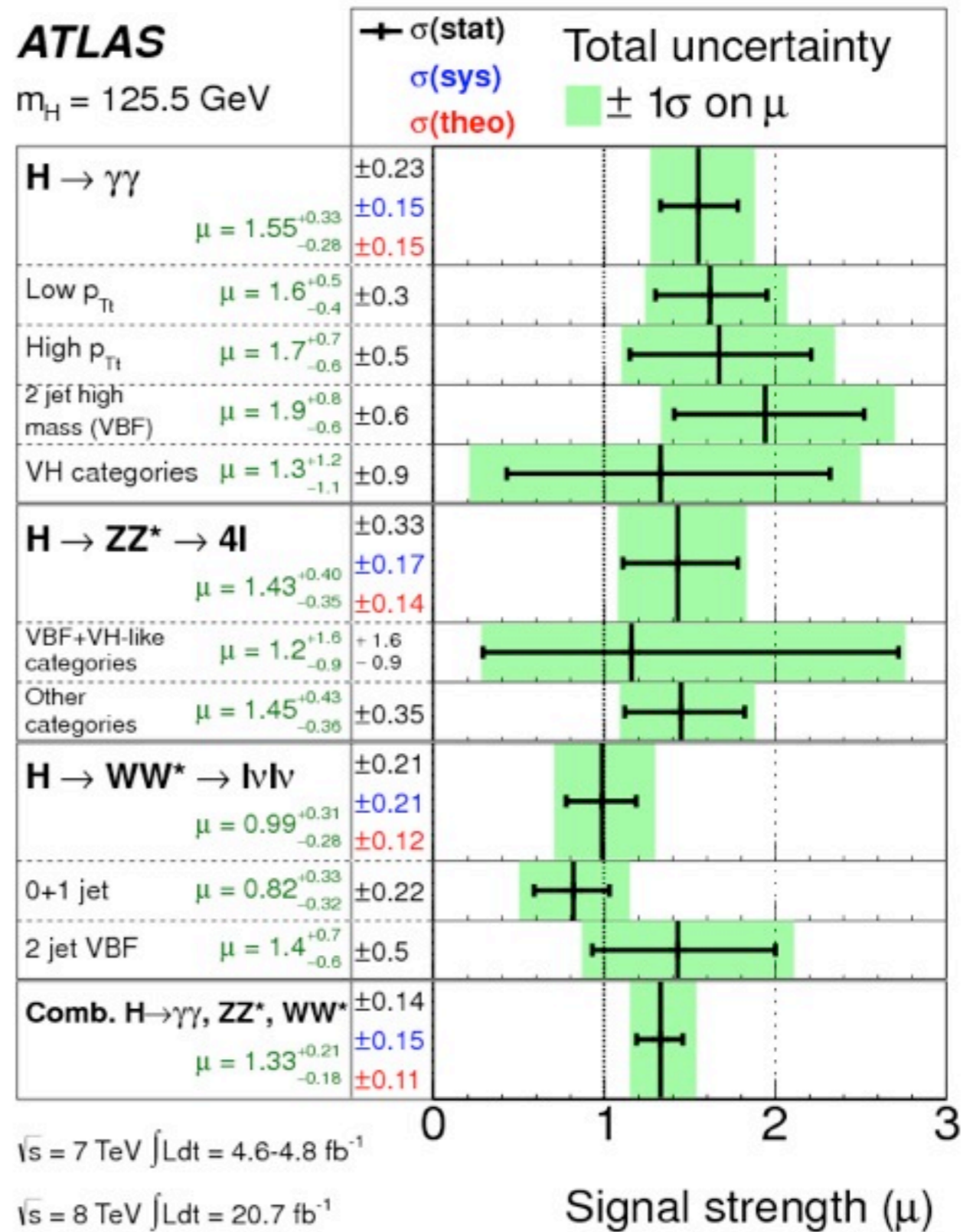
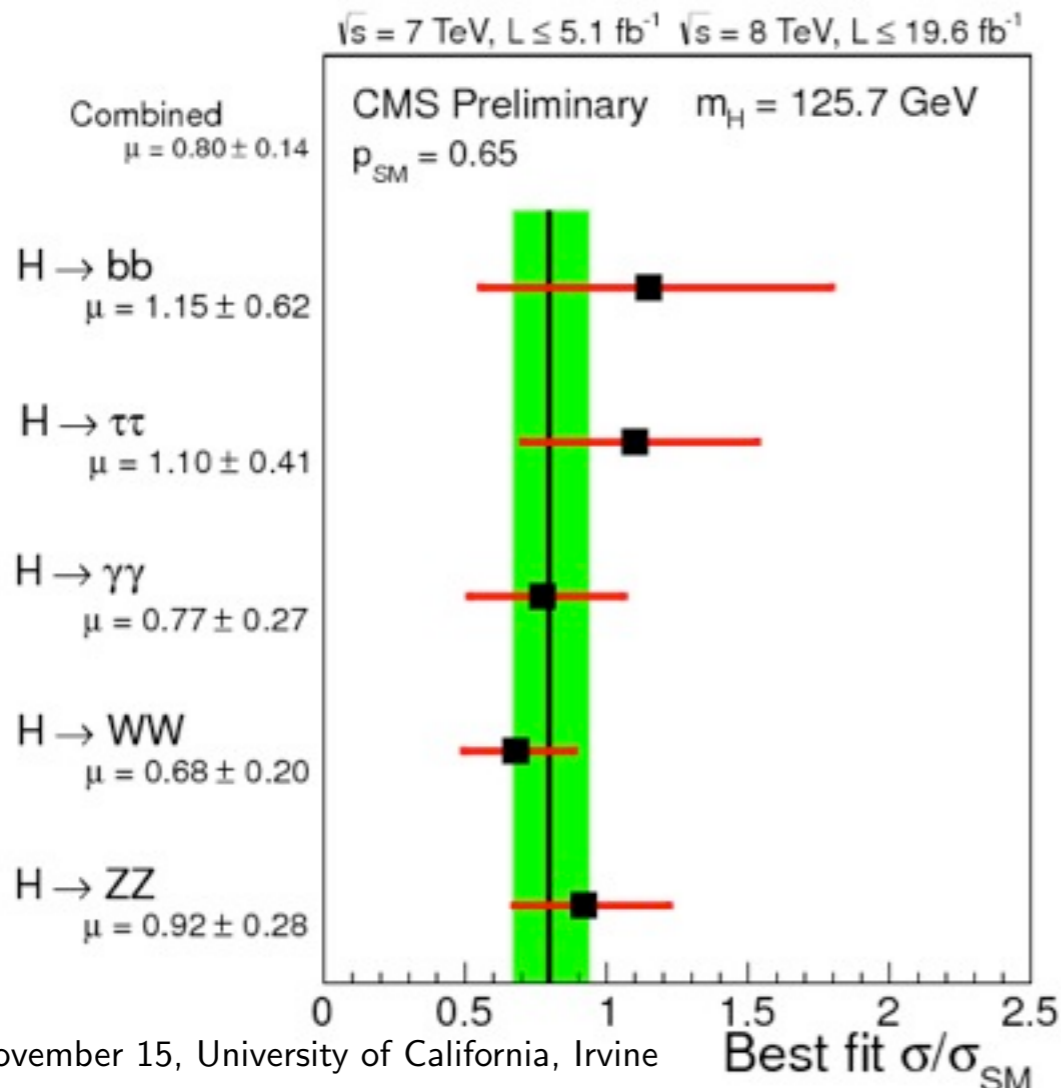
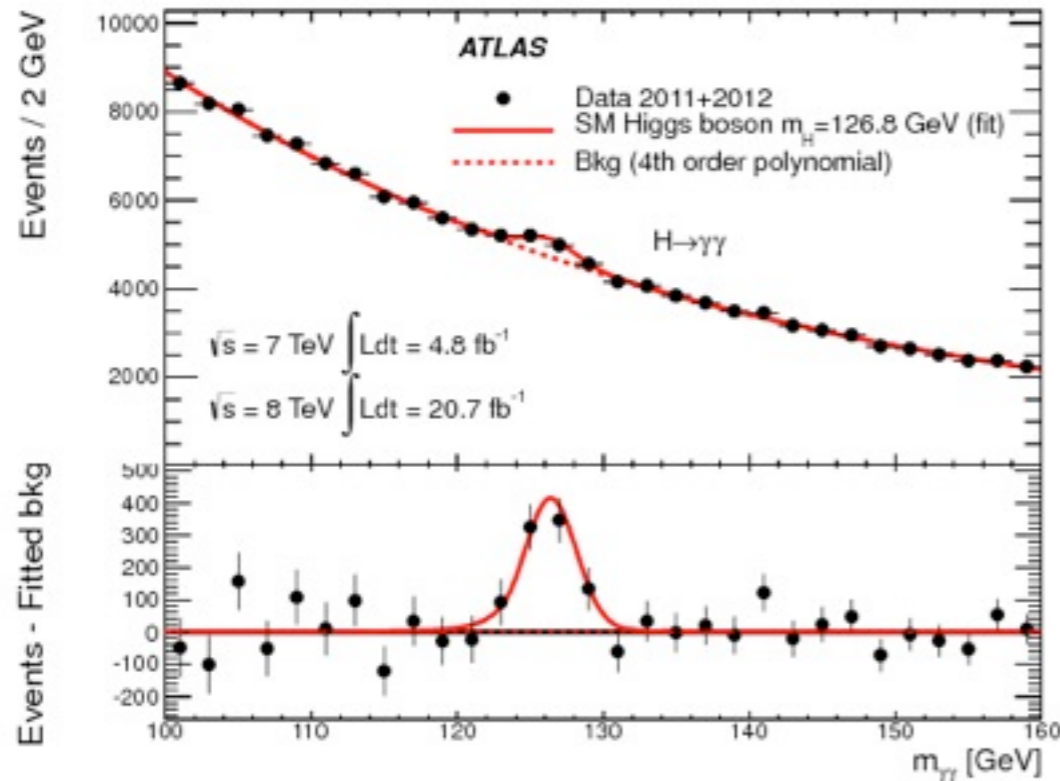
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November 15, Particle Physics Seminar
University of California, Irvine



Higgs Results



Implications for warped extra dimensions?

Outline

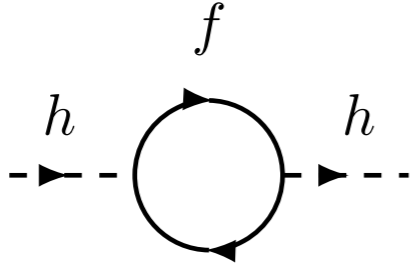
1. Basics about Warped Extra Dimensions
2. Higgs Couplings in Warped Extra Dimensions
 - Tree-level Higgs Couplings (W, Z, t, b)
 - Loop-induced Higgs Couplings (g, γ)
3. Higgs Phenomenology in Warped Extra Dimensions
 - Predictions for $pp \rightarrow h \rightarrow \gamma\gamma, ZZ^{(*)}, WW^{(*)}$
 - Bounds on the Parameter Space from Higgs Physics
4. Conclusions and Outlook

1. The Randall-Sundrum (RS) Model: Basics

Motivation: The Standard Model suffers from various problems, e.g.

- Gauge hierarchy problem:

Why is the Higgs light?


$$\Rightarrow \delta m_h^2 = -\frac{|\lambda_f|^2}{8\pi^2} [\Lambda_{UV}^2 + \dots] \quad \Lambda_{UV} \stackrel{?}{=} M_{Pl}$$

- Flavor hierarchy problem:

Why are the masses and CKM matrix elements hierarchical?

$$m_u : m_c : m_t = 1 : 560 : 75000$$

$$m_d : m_s : m_b = 1 : 20 : 800$$

$$V_{CKM} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} \quad \lambda = 0.23$$

1. The Randall-Sundrum (RS) Model: Basics

Possible solution: Warped Extra Dimensions

[L. Randall, R. Sundrum, hep-ph/9905221]

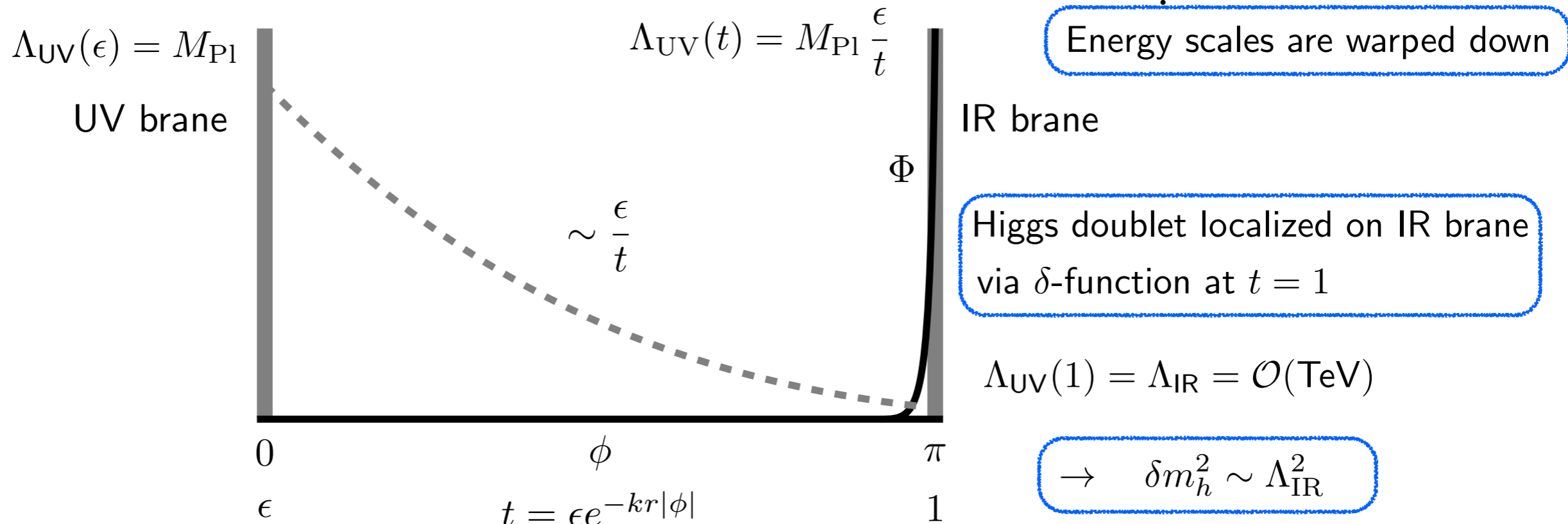
- Extra dimension: S^1/Z_2 orbifold (for chiral fermions in 5D) in a slice of AdS_5

$$ds^2 = \frac{\epsilon^2}{t^2} (dx_\mu dx^\mu - M_{\text{KK}}^{-2} dt^2)$$

warp factor $\epsilon = e^{-L} \approx 10^{-16}$

- Only one scale in theory: Planck mass $M_{\text{Pl}} \sim (k, M_{\text{Pl}(5)}, 1/r)$
- Solution for gauge hierarchy problem by moderate tuning $L = kr\pi \approx 36$

$$\int_\epsilon^1 dt \delta(t-1) \sqrt{|g(t)|} \lambda_5 \left(|\Phi|^2 - v_0^2/2 \right)^2 \rightarrow \lambda_5 \left(|\Phi|^2 - (\epsilon v_0)^2/2 \right)^2$$



1. The Randall-Sundrum (RS) Model: Basics

Possible solution: Warped Extra Dimensions

[L. Randall, R. Sundrum, hep-ph/9905221]

- All 5D fermion and gauge fields live in the bulk
→ *KK decomposition* of 5D fields

$$\Phi(x, t) \sim \sum_{n=0}^{\infty} \phi_n(x) \chi_n(t)$$

$$m_n \sim n\pi M_{\text{KK}}, \quad M_{\text{KK}} = k\epsilon \sim \mathcal{O}(\text{TeV})$$

- Couplings depend on overlap integrals of *profiles* $\sim \int_{\epsilon}^1 dt \chi_i(t) \chi_j(t) \chi_k(t)$

- Additional parameter in the theory: *bulk-mass parameters* $c_{Q_i, q_i} \sim \mathcal{O}(1)$

$$\mathcal{L}_{\text{quark}} \ni k \bar{Q} c_Q Q$$

- Explanation for flavor puzzle by localizations along the extra dimension

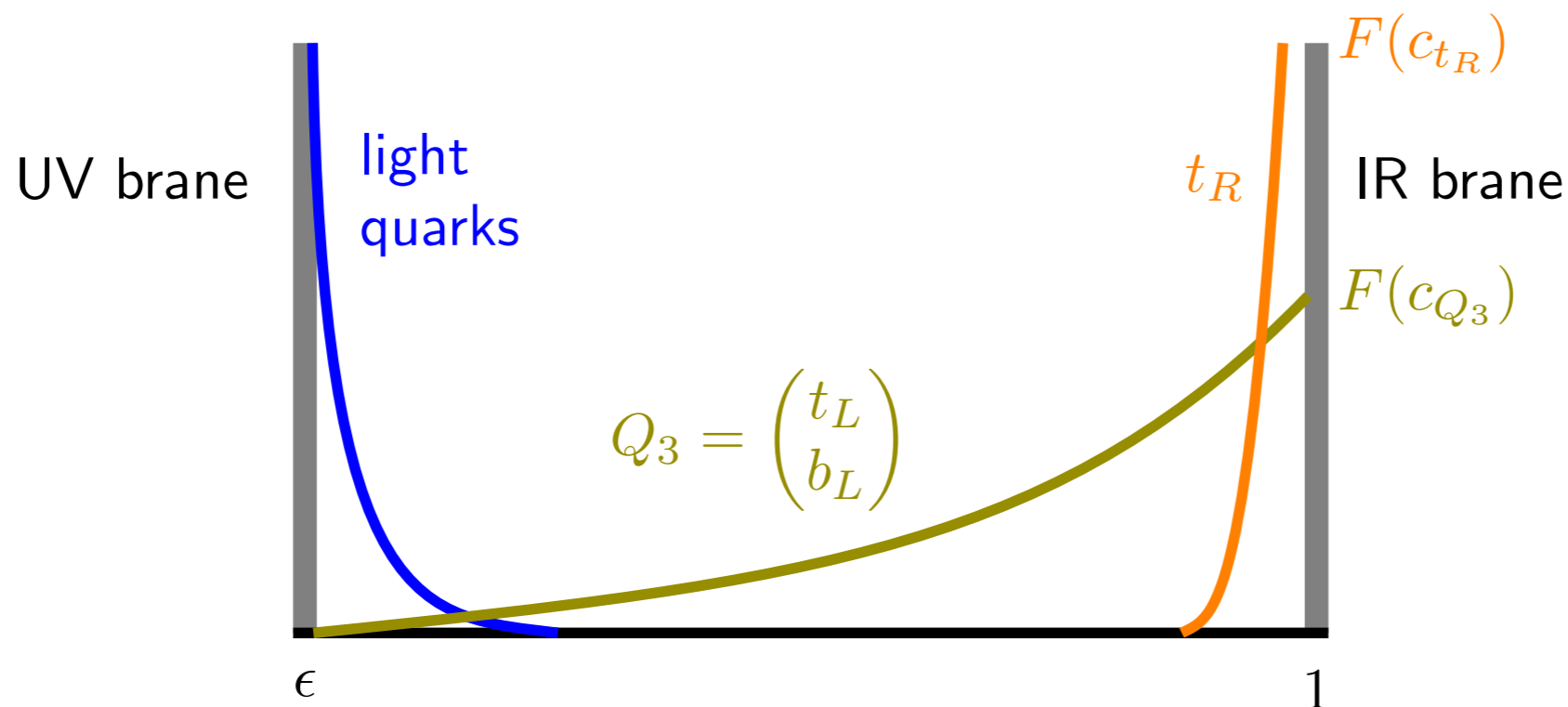
$$5\text{D Yukawas } Y_{q_{ij}} \sim \mathcal{O}(1)$$

overlap with Higgs (IR brane)

$$F(c) \sim \sqrt{\frac{1+2c}{1-\epsilon^{1+2c}}} \approx \begin{cases} \sqrt{1+2c} & c > -1/2 \\ \sqrt{-1-2c} \epsilon^{-1-2c} & c < -1/2 \end{cases}$$

effective Yukawa

$$Y_q^{\text{eff}} \sim F(c_Q) Y_q F(c_q)$$



1. The RS Model: Minimal and Custodial Version

Minimal RS model: [e.g. Casagrande et al, hep-ph/0807.4937]

- Based on SM group $SU(3)_C \times SU(2)_L \times U(1)_Y$
- Gives too large contributions to T parameter and to $Zb\bar{b}$ vertex
- Lower Bound on KK scale: $M_{\text{KK}} > 4.0 \text{ TeV} \rightarrow M_{g^{(1)}} > 9.8 \text{ TeV}$ (lightest KK state)
($M_{g^{(1)}} = 2.45 M_{\text{KK}}$)

Custodial RS model: [e.g. Casagrande et al, hep-ph/1005.4315]

- Based on SM group $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$
- Reduces contributions to T parameter and to $Zb\bar{b}$ vertex
- Lower Bound on KK scale: $M_{\text{KK}} > 1.9 \text{ TeV} \rightarrow M_{g^{(1)}} > 4.7 \text{ TeV}$
- Quark Content: up-type, down-type, λ -type ($Q=5/3$, no zero modes) quarks

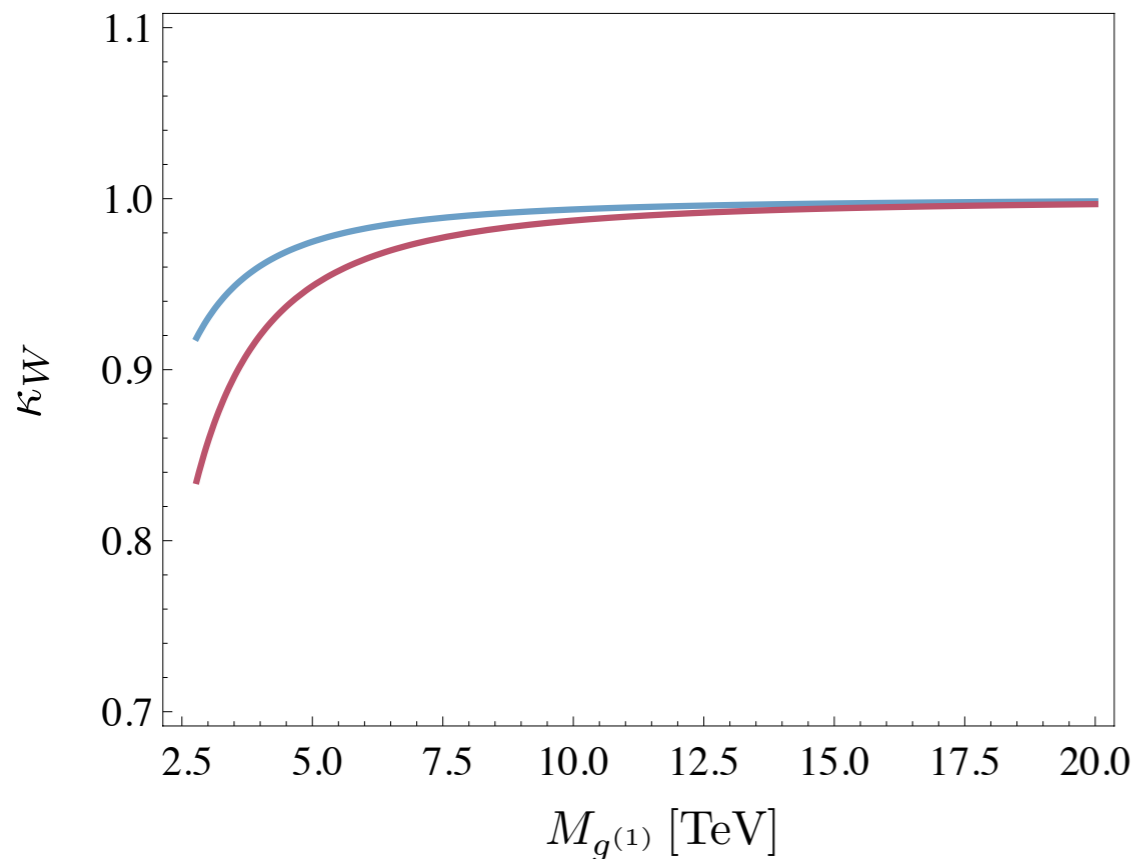
Randomized parameters in RS models:

- 2×9 complex Yukawa matrix elements $|(\mathbf{Y}_q)_{ij}| \leq y_* \sim \mathcal{O}(1)$
- one free c -parameter ($c_{q_3} \leq 1$)
- KK scale M_{KK} , volume $L = kr\pi = 33.5$ ($\rightarrow \Lambda_{\text{IR}} \approx 30 \text{ TeV}$)
- Constraint: Reproduction of SM quark masses and Wolfenstein Parameters

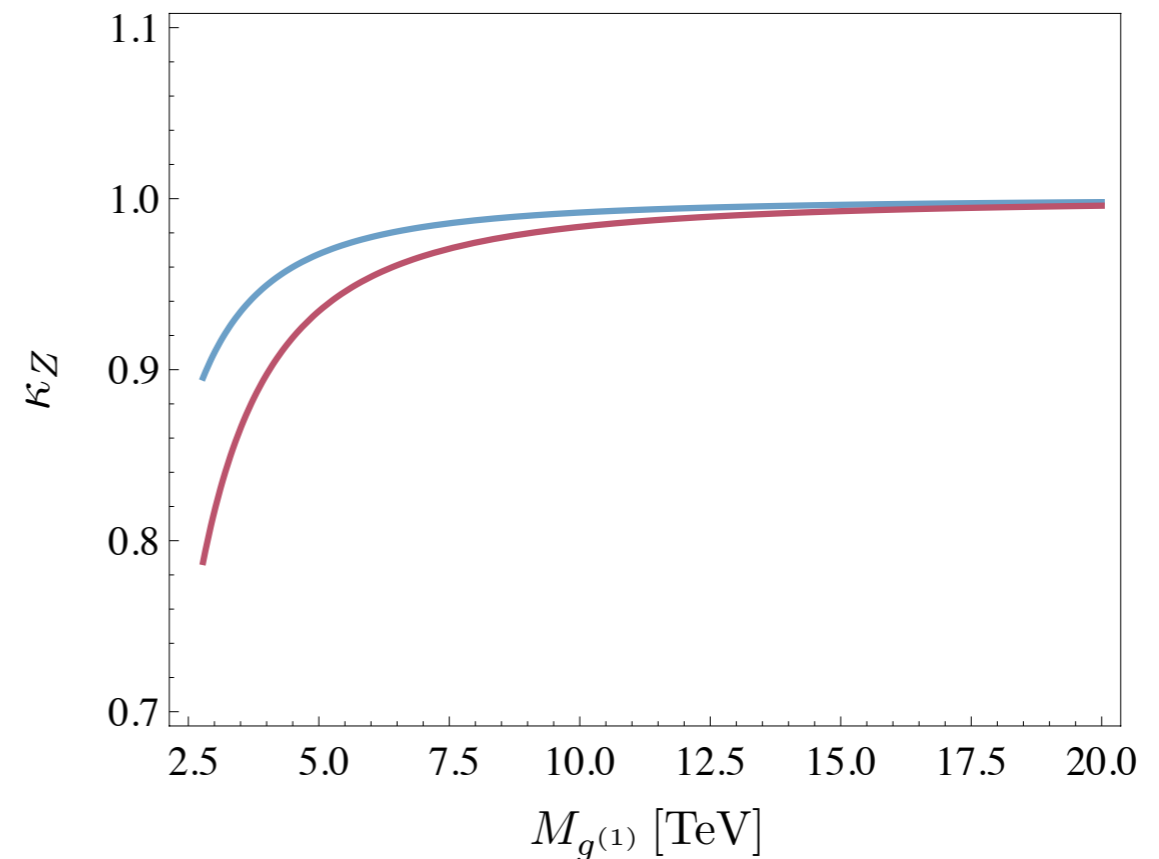
2. Higgs Couplings in RS Models: Tree-level Couplings

- Description via effective Lagrangian: $\mathcal{L}_{\text{eff}} = c_W \frac{2m_W^2}{v} h W_\mu^+ W^{-\mu} + c_Z \frac{2m_Z^2}{v} h Z_\mu Z^\mu$
- Couplings are given by overlap integrals: $c_{W,Z} \sim \int_\epsilon^1 dt \delta(t-1) \chi_{W,Z}(t) \chi_{W,Z}(t)$
- Results: $c_{W,Z} = 1 - \frac{m_{W,Z}^2}{2M_{\text{KK}}^2} \left(2L - 1 + \frac{1}{2L} \right)$, for **minimal** (**custodial**) RS model
- $\kappa_{W,Z} \equiv \frac{c_{W,Z}}{\kappa_v}$, corrected for vev shift $\kappa_v = \frac{v}{v_{\text{RS}}} = 1 + 2 \frac{L m_W^2}{2M_{\text{KK}}^2}$ [Casagrande et al, hep-ph/0807.4937]
[Casagrande et al, hep-ph/1005.4315]
[Bouchart et al, hep-ph/0909.4812]

W boson



Z boson

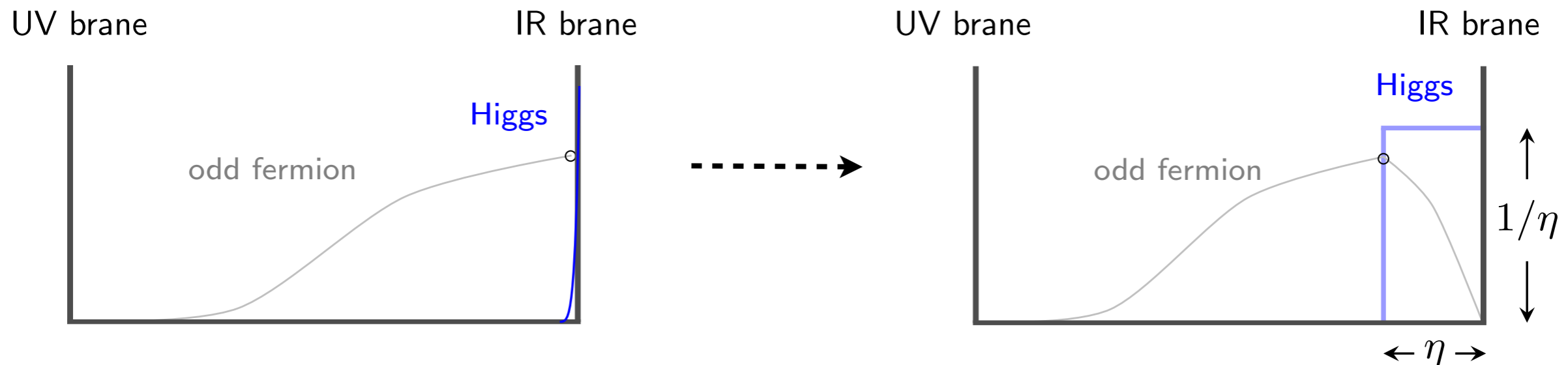


- Only small corrections for $M_{g(1)} \geq 5$ TeV, but could be detectable by e.g. ILC

2. Higgs Couplings in RS Models: Tree-level Couplings

- Effective Lagrangian: $\mathcal{L}_{\text{eff}} = -\frac{m_t}{v} h \bar{t} (c_t + c_{t5} i\gamma_5) t - \frac{m_b}{v} h \bar{b} (c_b + c_{b5} i\gamma_5) b$
- Couplings are given by overlap integrals: $c_{t,b} \sim \int_{\epsilon}^1 dt \delta(t-1) \left[Q_L^\dagger \mathbf{Y}_q q_R^c + Q_R^\dagger \mathbf{Y}_q q_L^c \right]$
- e.g. 5D doublets: $Q(x, t) = Q_L^0(x) \chi_L^0(t) + Q_L^1(x) \chi_L^1(t) + Q_R^1(x) \chi_R^1(t) + \dots$
- Subtlety: Z_2 -odd profiles of Q_R, q_L^c vanish at $t = 1$
 → Regularized Higgs profile $\delta^\eta(t - 1)$ with width η

[Azatov et al, hep-ph/0906.1990]



- Width η is an unphysical parameter in the case of a brane Higgs
- Gives a finite contribution in the limit $\eta \rightarrow 0$

2. Higgs Couplings in RS Models: Tree-level Couplings

- Effective Lagrangian: $\mathcal{L}_{\text{eff}} = -\frac{m_t}{v} h \bar{t} (c_t + c_{t5} i\gamma_5) t - \frac{m_b}{v} h \bar{b} (c_b + c_{b5} i\gamma_5) b$
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- Subtlety: Z_2 -odd profiles Q_R, q_L^c vanish at $t = 1$
 - Regularized Higgs profile $\delta^\eta(t-1)$ with width η
- Results: $c_t + ic_{t5} = 1 - (\delta_Q, \Phi_Q)_{33} - (\delta_u, \Phi_u)_{33} - \frac{2v^2}{3M_{\text{KK}}^2} \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} \sim (2N_g - 1) \frac{y_*^2}{2}$

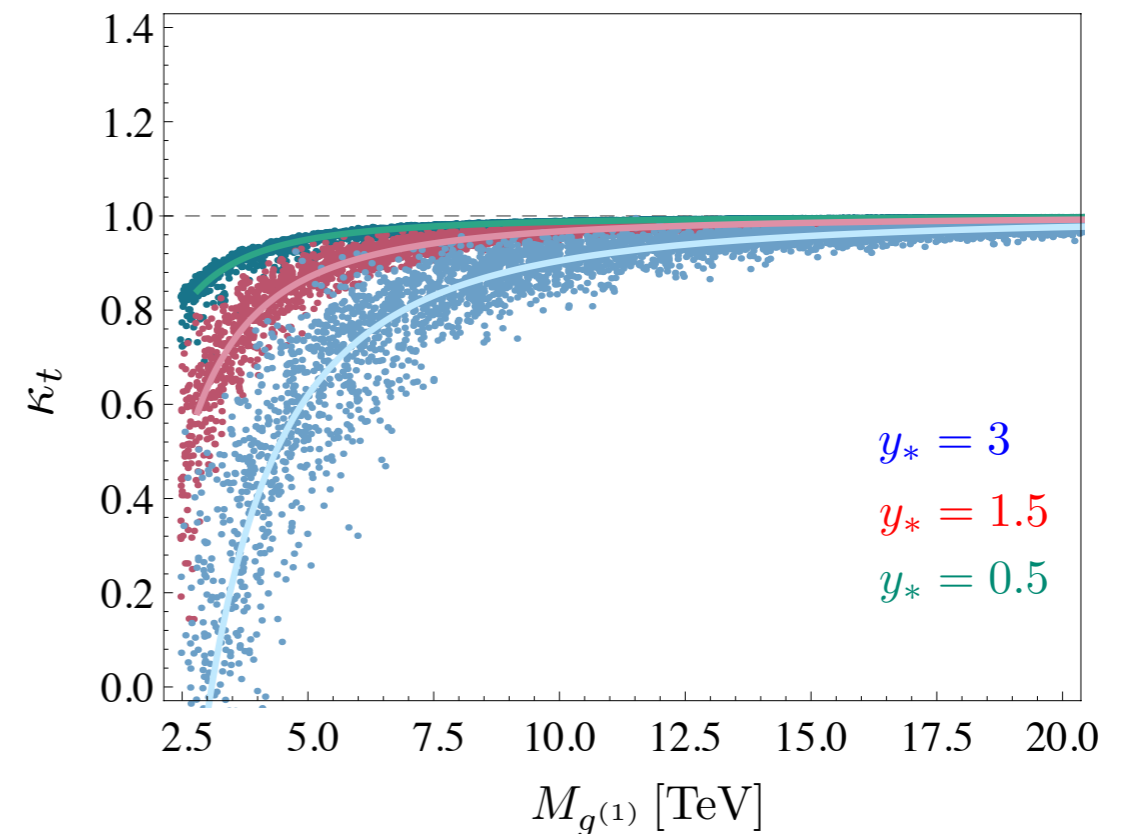
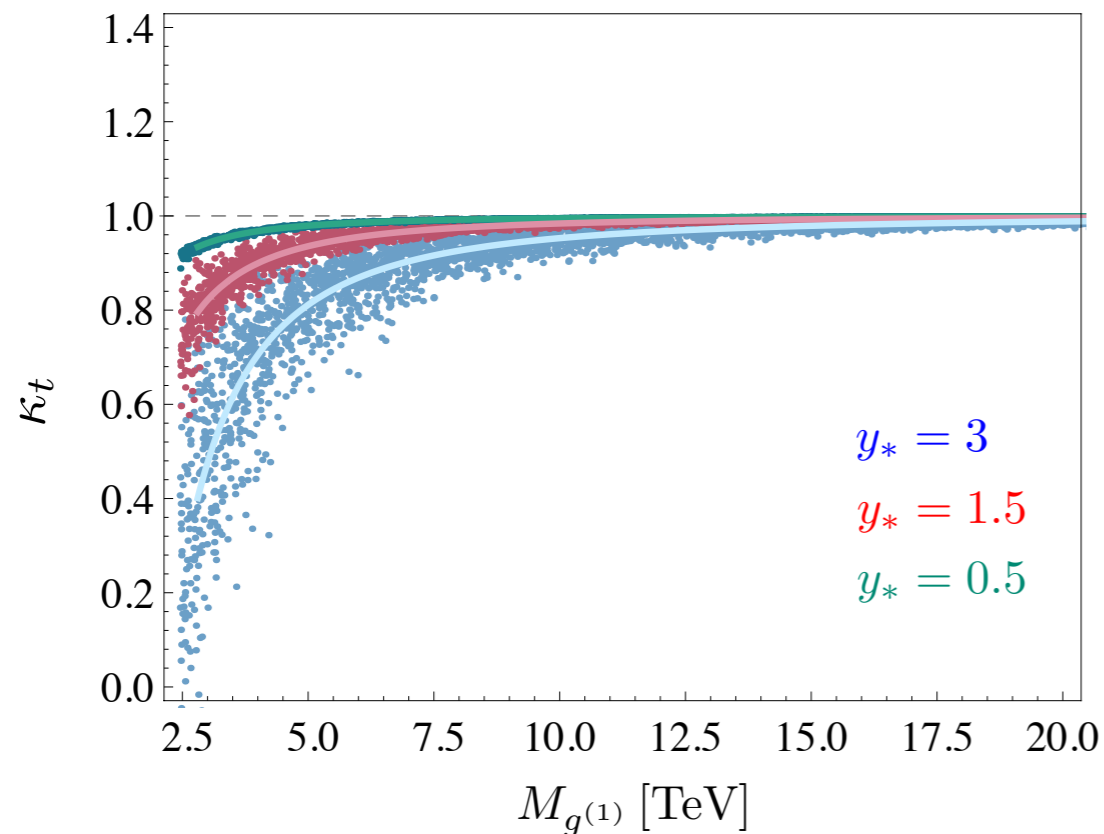
[Azatov et al, hep-ph/0906.1990]

[Casagrande et al, hep-ph/1005.4315]

$$\kappa_{t,b} = \frac{c_{t,b}}{\kappa_v}$$

Minimal RS model

Custodial RS model



2. Higgs Couplings in RS Models: Loop-induced Couplings

- Effective Lagrangian:

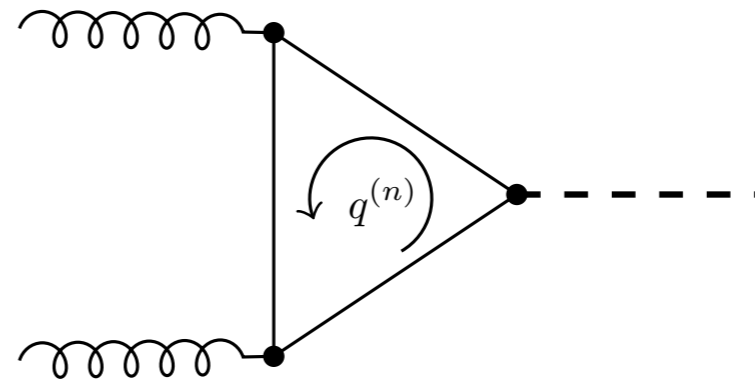
$$\mathcal{L}_{\text{eff}} = c_g \frac{\alpha_s}{12\pi v} h G_{\mu\nu}^a G^{a,\mu\nu} - c_{g5} \frac{\alpha_s}{8\pi v} h G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + c_\gamma \frac{\alpha_e}{6\pi v} h F_{\mu\nu}^a F^{a,\mu\nu} - c_{\gamma5} \frac{\alpha_e}{4\pi v} h F_{\mu\nu}^a \tilde{F}^{a,\mu\nu}$$

- Couplings are obtained by calculating loop-level diagrams

- $c_{g,g5}$ from:

- Only quark loop

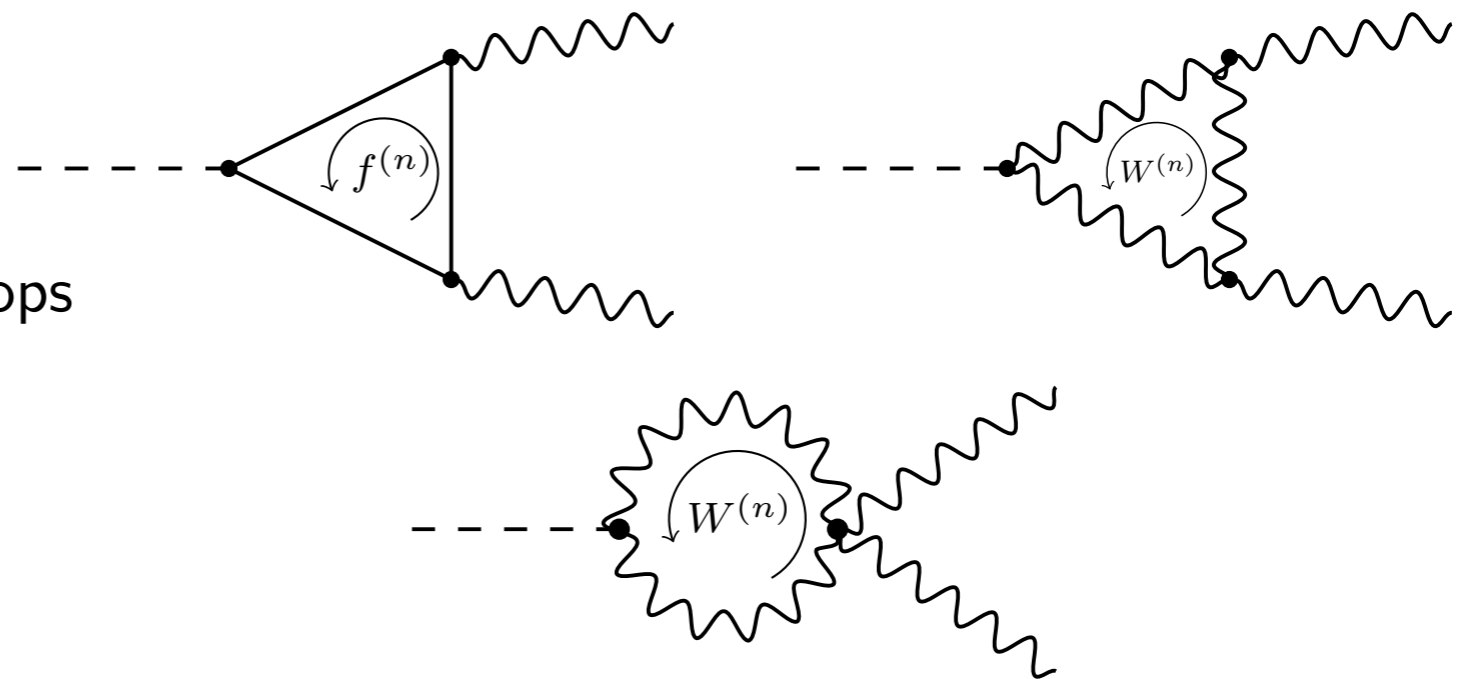
- Focused on in hep-ph/1303.5702



- $c_{\gamma,\gamma5}$ from:

- Quark, lepton, and W boson loops

- current work



2. Loop-induced Coupling c_g

How large is the KK Contribution for a brane Higgs?
Result insensitive to KK modes above the cutoff?

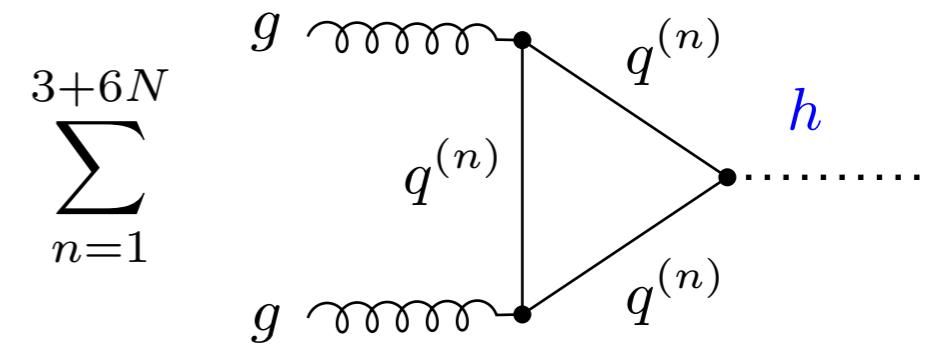
Two contradicting results

[Casagrande et al, hep-ph/1005.4315]

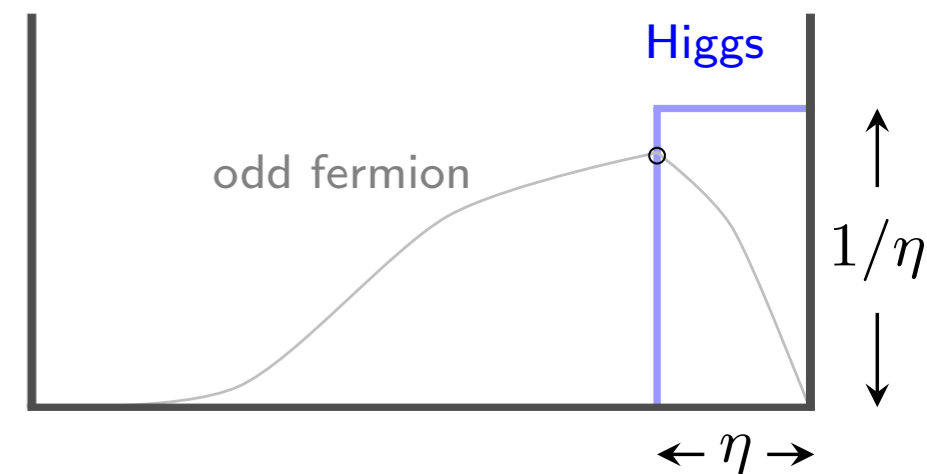
- Contribution of modes below cutoff $\Lambda_{IR} \approx 10 M_{KK}$
- Higgs coupling to Z_2 -odd fermions included
- Result: $c_g^{KK} \approx -\frac{v^2}{2M_{KK}^2} \text{Tr} [\mathbf{Y}_q \mathbf{Y}_q^\dagger]$ (negative correction to SM)

[Azatov et al, hep-ph/1006.5939]

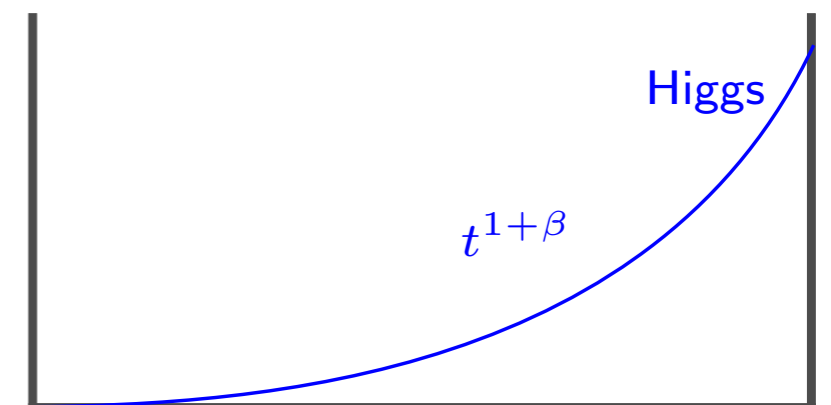
- Calculation with Bulk Higgs
- Narrow-bulk Higgs: Moving Higgs profile towards IR brane ($\beta \rightarrow \infty$)
- Result: $c_g^{KK} \approx +\frac{v^2}{2M_{KK}^2} \text{Tr} [\mathbf{Y}_q \mathbf{Y}_q^\dagger]$ (positive correction to SM)



brane-localized Higgs



narrow-bulk Higgs



2. Loop-induced Coupling c_g

How large is the KK Contribution for a brane Higgs?
Result insensitive to KK modes above the cutoff?

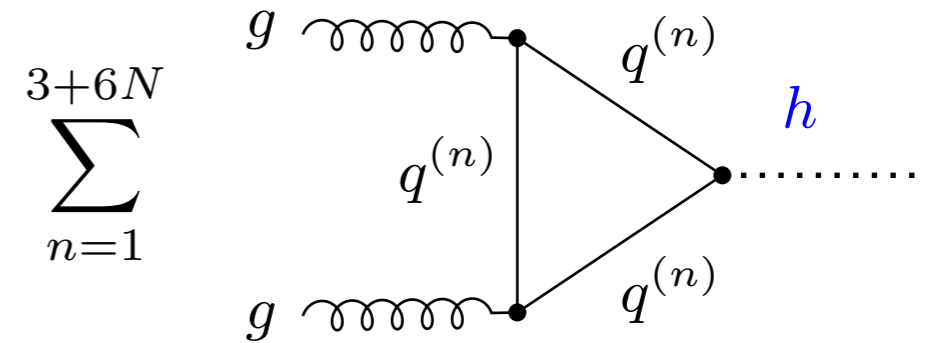
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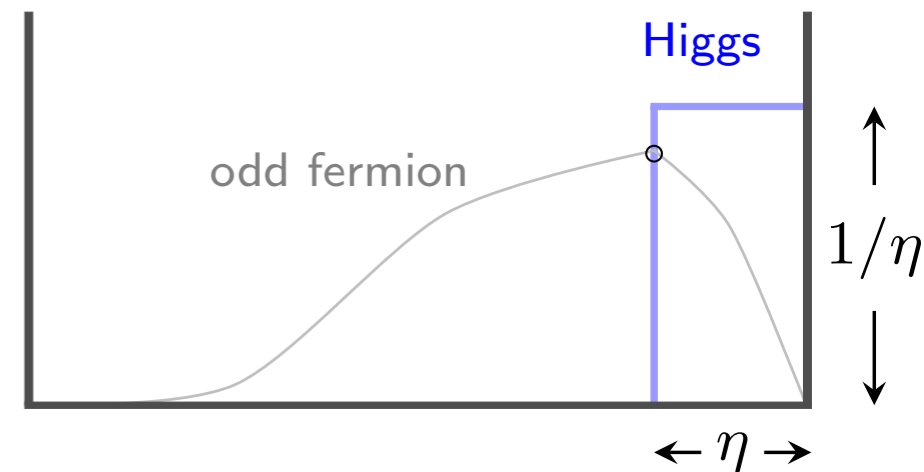
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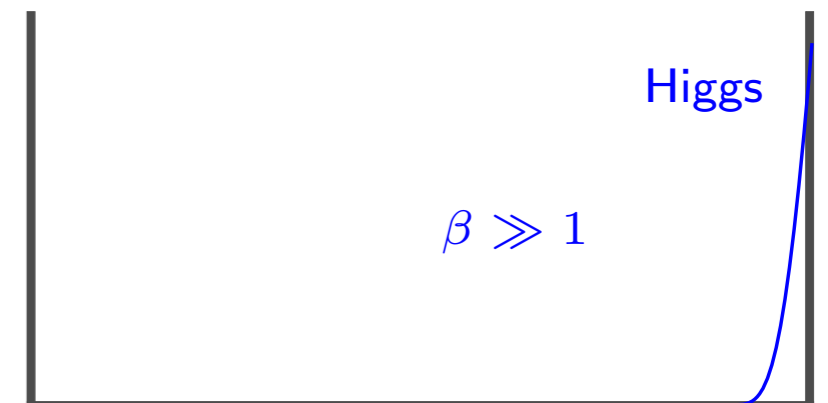
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brane-localized Higgs



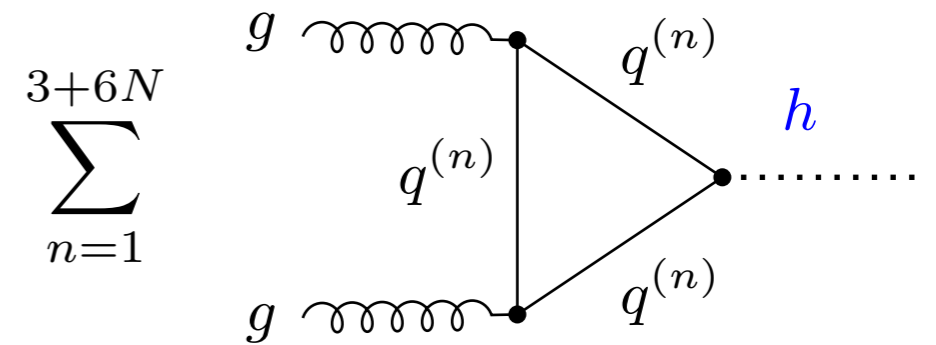
narrow-bulk Higgs



2. Loop-induced Coupling c_g

How large is the KK Contribution for a brane Higgs?
Result insensitive to KK modes above the cutoff?

Two contradicting results



Explanation from the 4D perspective [Carena et al, hep-ph/1204.0008]

$$\lim_{N \rightarrow \infty, \eta \rightarrow 0} \sum_{n=4}^{3+6N} \frac{v g_{nn}^q(\eta)}{m_{q_n}} \left(\frac{\mu}{m_{q_n}} \right)^{4-d}$$

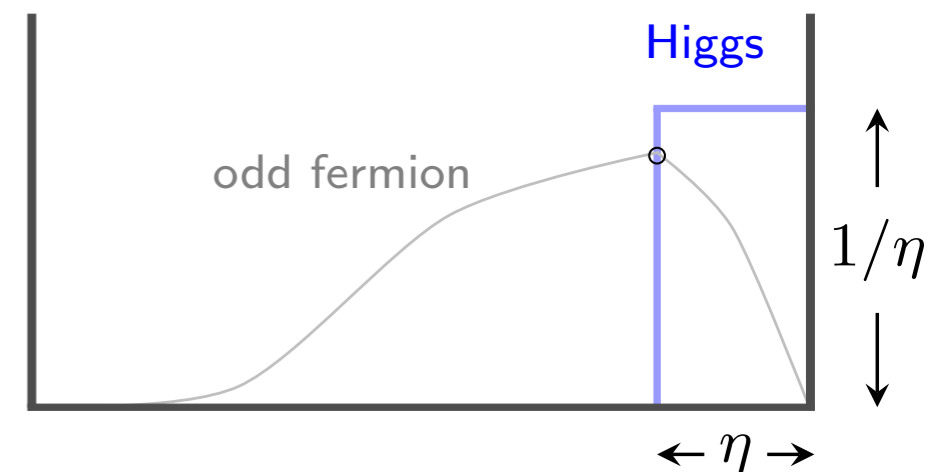
$d < 4$, with cutoff

- limits $N \rightarrow \infty$ and $\eta \rightarrow 0$ commute
- unique result: $c_g^{\text{KK}} \approx -\frac{v^2}{2M_{\text{KK}}} \text{Tr} \left[\mathbf{Y}_q \mathbf{Y}_q^\dagger \right]$

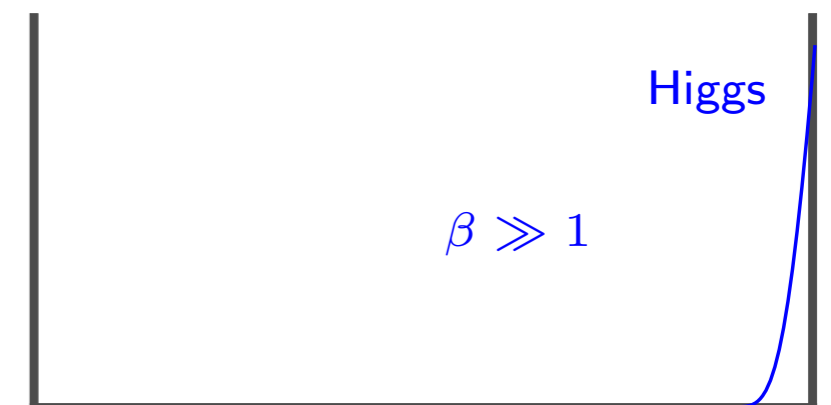
$d = 4$, without cutoff

- limits $N \rightarrow \infty$ and $\eta \rightarrow 0$ do not commute
- KK modes with $m_{q_n} \sim v|Y_q|/\eta$ contribute significantly

brane-localized Higgs



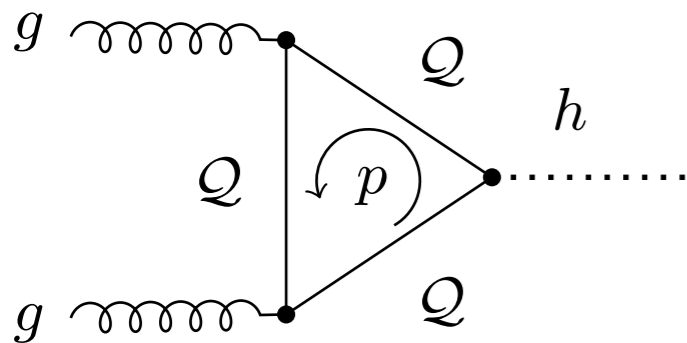
narrow-bulk Higgs



2. Loop-induced Coupling c_g

Idea of our work (hep-ph/1303.5703):

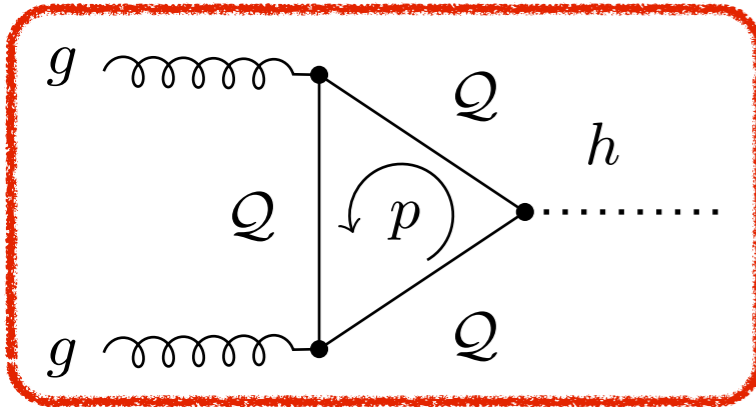
- Derive 5D fermion propagator for three generations and with exact dependence on the Yukawas \rightarrow KK modes implicitly summed up
- Use regularized δ -function for Higgs profile
- Use dimensional regularization ($d = 4 - 2\hat{\epsilon}$) for the 4D loop-momentum integral
- Check explicitly how high-momentum modes decouple



$$\begin{aligned}
 \mathcal{A}(gg \rightarrow h) &= c_g \frac{\alpha_s}{12\pi v} \langle 0 | G_{\mu\nu}^a G^{\mu\nu,a} | gg \rangle - c_{g5} \frac{\alpha_s}{8\pi v} \langle 0 | G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} | gg \rangle \\
 c_{g,g5} &\sim I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^\infty dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)
 \end{aligned}$$

- Functions T_{\pm} are integrals over the mixed-chirality components $\Delta_{LR,RL}$ of the 5D quark propagator with the regularized Higgs profile along the extra dimension

2. Loop-induced Coupling c_g



$$\mathcal{A}(gg \rightarrow h) = c_g \frac{\alpha_s}{12\pi v} \langle 0 | G_{\mu\nu}^a G^{\mu\nu,a} | gg \rangle - c_{g5} \frac{\alpha_s}{8\pi v} \langle 0 | G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} | gg \rangle$$

$$c_{g,g5} \sim I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^\infty dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2) \quad p_E^2 = -p^2$$

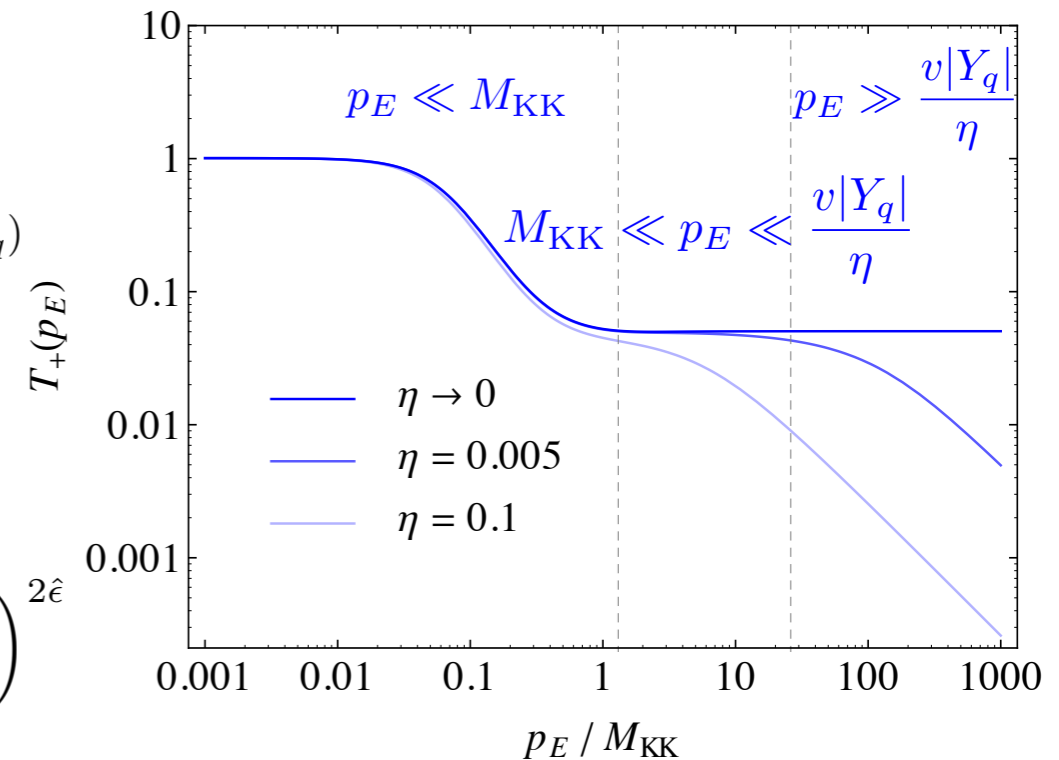
Function $T_+(p_E^2)$:

- three characteristic regions
- can be approximated by toy model $t_{0,1,3} \equiv t_{0,1,3}(\mathbf{Y}_q)$ $t_2 \equiv t_2(\mathbf{c}_j, \mathbf{Y}_q)$

$$T_+^{\text{toy}}(p_E^2) = \frac{t_0 - t_1 - t_2}{1 + \hat{p}_E^2} + \frac{t_2}{\sqrt{1 + \hat{p}_E^2}} + \frac{t_3}{\sqrt{(t_3/t_1)^2 + (\eta \hat{p}_E)^2}}$$

- Performing loop momentum integral gives

$$I_+^{\text{toy}}(0) = (t_0 - t_1 - t_2) \left(\frac{\mu}{M_{\text{KK}}} \right)^{2\hat{\epsilon}} + t_2 \left(\frac{\mu}{2M_{\text{KK}}} \right)^{2\hat{\epsilon}} + t_1 \left(\frac{t_1}{2t_3} \right)^{2\hat{\epsilon}} \left(\frac{\eta\mu}{M_{\text{KK}}} \right)^{2\hat{\epsilon}}$$



Two different choices lead to two different models! Transition region not calculable!

- send $\eta \rightarrow 0$, then remove regulator: $I_+^{\text{toy}}(0) = t_0 - t_1$ ($R_h < 1$) *brane Higgs*
- keep η finite, then remove regulator: $I_+^{\text{toy}}(0) = t_0$ ($R_h > 1$) *narrow-bulk Higgs*

2. Loop-induced Coupling c_g

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- send $\eta \rightarrow 0$, then remove regulator: $I_+^{\text{toy}}(0) = t_0 - t_1$ ($R_h < 1$) *brane Higgs*
- keep η finite, then remove regulator: $I_+^{\text{toy}}(0) = t_0$ ($R_h > 1$) *narrow-bulk Higgs*

Regulator dependent result? What about transition region?

- Repeat analysis with hard-momentum cutoff Λ_{TeV}
- Threshold corrections explicitly visible

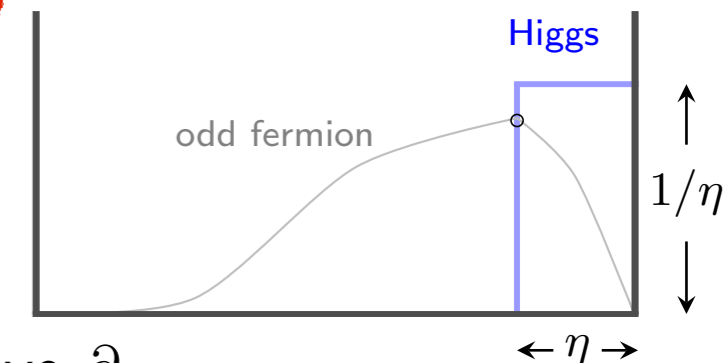
• Results:

$$I_+^{\text{toy}} = t_0 - t_1 - \frac{3t_2}{2} \frac{M_{\text{KK}}}{\Lambda_{\text{TeV}}} \quad \textit{brane Higgs}$$

$$I_+^{\text{toy}} = t_0 - \frac{3t_3}{2} \frac{M_{\text{KK}}}{\eta \Lambda_{\text{TeV}}} \quad \textit{narrow-bulk Higgs}$$

Threshold corrections in the narrow bulk-Higgs scenario

- explode for $\eta \rightarrow 0$
- can be attributed to higher-dimensional operators involving derivative ∂_t



Transition region not calculable!

2. Loop-induced Coupling c_g

$$I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^{\infty} dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)$$



$$I_+(m^2) = \sum_{q=u,d} \left\{ \text{Tr } g(\mathbf{X}_q) + \frac{1}{2} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} + \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right] \right\}$$

$$I_-(m^2) = \sum_{q=u,d} \frac{1}{2i} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} - \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right]$$

2. Loop-induced Coupling c_g

$$I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^{\infty} dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)$$



$$I_+(m^2) = \sum_{q=u,d} \left\{ \text{Tr } g(\mathbf{X}_q) + \frac{1}{2} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \right] \right.$$

$$I_-(m^2) = \sum_{q=u,d} \frac{1}{2i} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \right]$$

$$\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger, \text{ with 5D Yukawa matrices } \mathbf{Y}_q$$

- $\mathcal{L}_Y \ni \int_{\epsilon}^1 dt \bar{Q}_L(t, x) \cdot \Phi(x, t) \mathbf{Y}_d d_R^c(t, x) + \dots$
- anarchic 3×3 matrices in generation space
- $(\mathbf{Y}_q)_{ij}$ are random complex numbers
- $|(\mathbf{Y}_q)_{ij}| \leq y_* \sim \mathcal{O}(1)$

2. Loop-induced Coupling c_g

$$I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^{\infty} dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)$$



$$\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$$

$$I_+(m^2) = \sum_{q=u,d} \left\{ \text{Tr } g(\mathbf{X}_q) + \frac{1}{2} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} + \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right] \right\}$$

$$I_-(m^2) = \sum_{q=u,d} \frac{1}{2i} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} - \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right]$$

- Depends on the RS scenario

$$g(\mathbf{X}_q)|_{\text{brane}} = -\frac{\mathbf{X}_q \tanh \mathbf{X}_q}{\cosh \mathbf{X}_q} = -\mathbf{X}_q^2 + \dots$$

$$g(\mathbf{X}_q)|_{\text{narrow bulk}} = \mathbf{X}_q \tanh \mathbf{X}_q = +\mathbf{X}_q^2 + \dots$$

- Independent of bulk mass parameters $c_{Q,q}$
- Dependent on rank of matrix $\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$
- Vanishes in the limit $M_{\text{KK}} \rightarrow \infty$
 → Contribution from KK tower

2. Loop-induced Coupling c_g

$$I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^{\infty} dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)$$



$$\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$$

$$I_+(m^2) = \sum_{q=u,d} \left\{ \text{Tr } g(\mathbf{X}_q) + \frac{1}{2} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} + \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right] \right\}$$

$$I_-(m^2) = \sum_{q=u,d} \frac{1}{2i} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} - \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right]$$

$$g(\mathbf{X}_q)|_{\text{brane}} = -\frac{\mathbf{X}_q \tanh \mathbf{X}_q}{\cosh \mathbf{X}_q} = -\mathbf{X}_q^2 + \dots$$

$$g(\mathbf{X}_q)|_{\text{narrow bulk}} = \mathbf{X}_q \tanh \mathbf{X}_q = +\mathbf{X}_q^2 + \dots$$

- Independent of bulk mass parameters $\mathbf{c}_{Q,q}$
- Dependent on rank of matrix $\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$
- Vanishes in the limit $M_{\text{KK}} \rightarrow \infty$
→ Contribution from KK tower

$$\mathbf{Z}_q(p_E^2) = \frac{v^2}{2M_{\text{KK}}^2} \frac{\tanh \mathbf{X}_q}{\mathbf{X}_q} \mathbf{Y}_q \mathbf{R}_q(\hat{p}_E) \mathbf{Y}_q^\dagger \frac{\tanh \mathbf{X}_q}{\mathbf{X}_q} \mathbf{R}_Q(\hat{p}_E)$$

$\hat{p}_E = \frac{p_E}{M_{\text{KK}}}$

- $\mathbf{R}_{Q,q}$ are ratios of Bessel functions
- $\mathbf{R}_{Q,q}$ include bulk mass parameters $\mathbf{c}_{Q,q}$
- Small momentum behavior $\mathbf{R}_{Q,q} = \frac{F^2(\mathbf{c}_{Q,q})}{\hat{p}_E} + \mathcal{O}(\hat{p}_E)$
- Non-vanishing contributions in the limit $M_{\text{KK}} \rightarrow \infty$
→ \mathbf{Z}_q includes zero-mode contribution

2. Loop-induced Coupling c_g

$$I_{\pm}(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^\infty dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_{\pm}(p_E^2 + m^2)$$



$$\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$$

$$I_+(m^2) = \sum_{q=u,d} \left\{ \text{Tr } g(\mathbf{X}_q) + \frac{1}{2} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} + \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right] \right\}$$

$$I_-(m^2) = \sum_{q=u,d} \frac{1}{2i} \text{Tr} \left[\frac{2\mathbf{X}_q}{\sinh 2\mathbf{X}_q} \left(\frac{\mathbf{Z}_q(-m^2)}{1 + \mathbf{Z}_q(-m^2)} - \frac{\mathbf{Z}_q^\dagger(-m^2)}{1 + \mathbf{Z}_q^\dagger(-m^2)} \right) \right]$$

Integration over the Feynman parameter yields the Wilson coefficients

$$c_g = \frac{3}{2} \int_0^1 dz (1-z) f(z) I_+ \left(-z \frac{m_h^2}{4} - i0 \right)$$

$$c_{g5} = \int_0^1 dz f(z) I_- \left(-z \frac{m_h^2}{4} - i0 \right)$$

$$f(z) = \text{arctanh} \sqrt{1-z}$$

$g(\mathbf{X}_q)$

$g(\mathbf{X}_q)|_{\text{naive}}$

- Independent

- Dependence

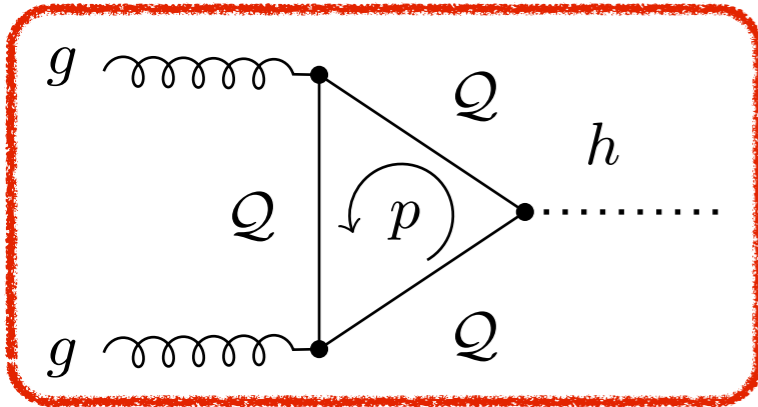
- Vanishes

→ Cont

(\hat{p}_E)

$\mathcal{O}(\hat{p}_E)$

2. Loop-induced Coupling c_g



$$\mathcal{A}(gg \rightarrow h) = c_g \frac{\alpha_s}{12\pi v} \langle 0 | G_{\mu\nu}^a G^{\mu\nu,a} | gg \rangle - c_{g5} \frac{\alpha_s}{8\pi v} \langle 0 | G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} | gg \rangle$$

$$c_g \approx \text{Tr } g(\sqrt{2}\mathbf{X}_u) + 3 \text{Tr } g(\sqrt{2}\mathbf{X}_d) + \left[1 - \frac{2v^2}{3M_{\text{KK}}^2} \text{Re} \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} \right] A(\tau_t) + A(\tau_b)$$

$$c_{g5} \approx -\frac{2v^2}{3M_{\text{KK}}^2} \text{Im} \frac{(\mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u)_{33}}{(\mathbf{Y}_u)_{33}} B(\tau_t)$$

minimal
custodial

$$g(\mathbf{X}_q)|_{\text{brane}} = -\frac{\mathbf{X}_q \tanh \mathbf{X}_q}{\cosh \mathbf{X}_q} = -\mathbf{X}_q^2 + \dots$$

$$g(\mathbf{X}_q)|_{\text{narrow bulk}} = \mathbf{X}_q \tanh \mathbf{X}_q = +\mathbf{X}_q^2 + \dots$$

- Independent of bulk mass parameters $c_{Q,q}$
- Dependent on rank of matrix $\mathbf{X}_q^2 = \frac{v^2}{2M_{\text{KK}}^2} \mathbf{Y}_q \mathbf{Y}_q^\dagger$
- Vanishes in the limit $M_{\text{KK}} \rightarrow \infty$
→ Contribution from KK tower

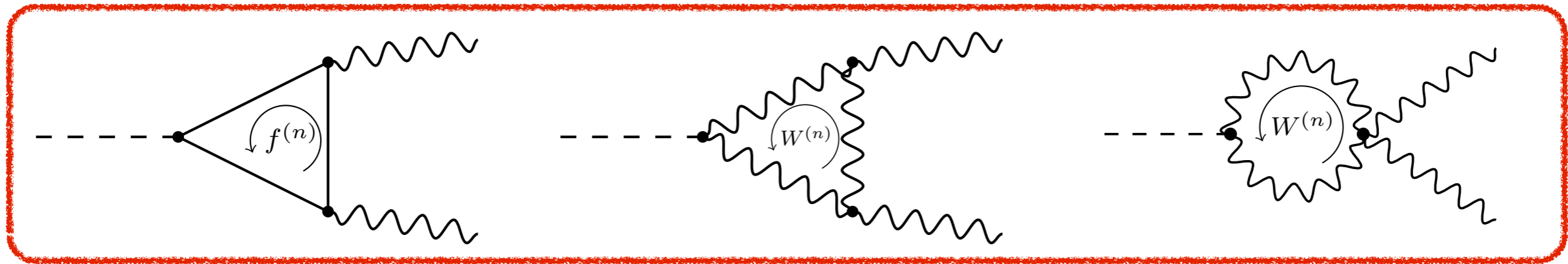
Factor of 4 larger!

$$A(\tau) = \frac{3\tau}{2} \left[1 + (1 - \tau) \arctan^2 \frac{1}{\sqrt{\tau - 1}} \right] \quad \tau_i = 4m_{q_i}^2/m_h^2 - i0$$

$$B(\tau) = \tau \arctan^2 \frac{1}{\sqrt{\tau - 1}}$$

- Contribution from SM quarks
- Only top and bottom quark relevant
- Modified couplings to top due to mixing with KK modes

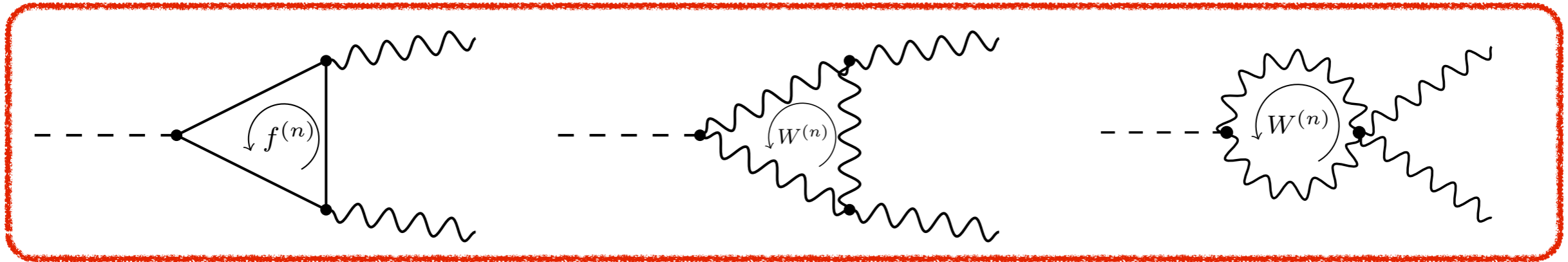
2. Loop-induced Coupling c_γ



- $c_{\gamma,\gamma 5} = c_{\gamma,\gamma 5}^q + c_{\gamma,\gamma 5}^l + c_{\gamma,\gamma 5}^W$ [$c_{\gamma,\gamma 5}^{q,l}$ from $c_{g,g 5}$ ($g_{sta} \rightarrow eQ_f$)]
- Idea to determine $c_{\gamma,\gamma 5}^W$:
 - Calculate each diagram in R_ξ gauge
 - Show that at each KK level the sum of all diagrams is gauge-independent
 - Only the two diagrams above contribute [Marciano et al, hep-ph/1109.5304]
 - Relate amplitude to expressions involving 5D boson propagator
- Result:

$$c_\gamma^W = -3\pi\tilde{m}_W^2 \left[T_W(0) + 3 \int_0^1 dz \left(1 - \frac{z}{2} \right) \operatorname{arctanh}(\sqrt{1-z}) I_W \left(z \frac{m_h^2}{4} \right) \right]$$

2. Loop-induced Coupling c_γ



$$c_\gamma^W = -3\pi\tilde{m}_W^2 \left[T_W(0) + 3 \int_0^1 dz \left(1 - \frac{z}{2}\right) \operatorname{arctanh}(\sqrt{1-z}) I_W\left(z \frac{m_h^2}{4}\right) \right]$$

$$T_W(p_E^2) = \int_\epsilon^1 dt \delta_h^\eta(t-1) D_W^{\xi=1}(t, t; p_E^2)$$

$$I_W(m^2) = -\frac{e^{\hat{\epsilon}\gamma_E} \mu^{2\hat{\epsilon}}}{\Gamma(1-\hat{\epsilon})} \int_0^\infty dp_E p_E^{-2\hat{\epsilon}} \frac{\partial}{\partial p_E} T_W(p_E^2 - m^2 - i0)$$

- Integral over regularized Higgs profile and 5D propagator

- $T_W(0) = \frac{1}{2\pi\tilde{m}_W^2}$

- $T_W(p_E^2) = \frac{L}{2\pi M_{\text{KK}}^2} \frac{1}{\hat{p}_E}$ for $p_E \gg M_{\text{KK}}$

- No plateau! Unambiguous result!

Correction to W boson c_W

SM result

KK tower contribution

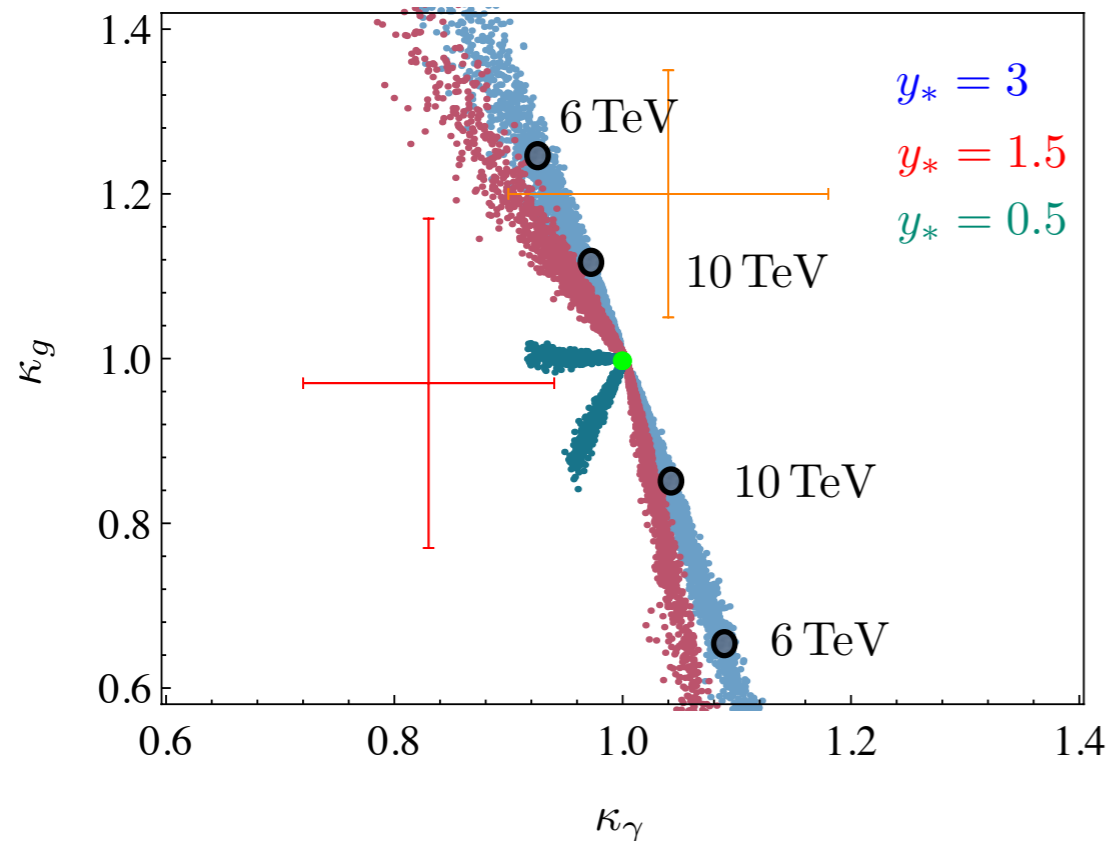
$$c_\gamma^W \approx \left[1 - \frac{m_W^2}{2M_{\text{KK}}^2} \left(L - 1 + \frac{1}{2L} \right) \right] A_W^h(\tau_W) - \frac{21}{8} \frac{m_W^2}{M_{\text{KK}}^2} \left(L - 1 + \frac{1}{2L} \right)$$

2. Loop-induced Couplings c_g and c_γ

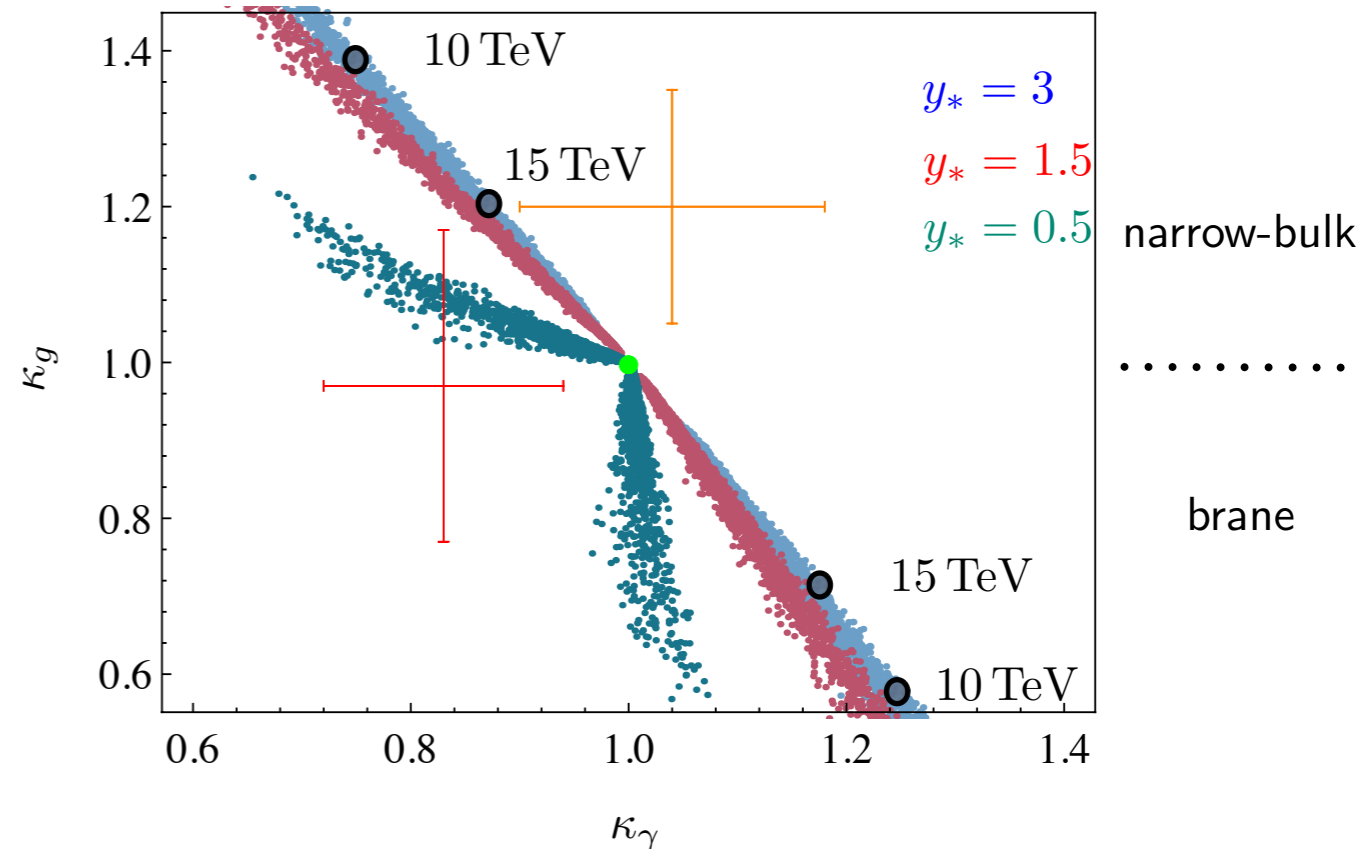
ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005

$$\kappa_{g,\gamma} = \frac{c_{g,\gamma}}{c_{g,\gamma}^{\text{SM}} \kappa_v}$$

Minimal model



Custodial model



$$\kappa_g \approx 1 - \frac{v^2}{2M_{\text{KK}}^2} \left[4 \left(\pm 4N_g^2 + 2\frac{2}{3}N_g - 2\frac{1}{3} \right) \langle |\mathbf{Y}_{ij}|^2 \rangle + \frac{2Lm_W^2}{v^2} \right]$$

$$\kappa_\gamma \approx 1 - \frac{v^2}{2M_{\text{KK}}^2} \left[\frac{1}{\hat{c}_\gamma^{\text{SM}}} \left(\pm 9\frac{8}{3}N_g^2 + 2\frac{16}{9}N_g - 2\frac{8}{9} \right) \langle |\mathbf{Y}_{ij}|^2 \rangle + \frac{2Lm_W^2}{\hat{c}_\gamma^{\text{SM}} v^2} \left(\frac{23}{4} + A_h^W(\tau_W) \right) \right]$$

$$\mp \text{Tr } \mathbf{X}_q^2 = \mp \frac{v^2}{2M_{\text{KK}}^2} \sum_{i,j=1}^{N_g} |(\mathbf{Y}_q)_{ij}|^2 \approx \mp \frac{v^2}{2M_{\text{KK}}^2} \frac{N_g^2 y_*^2}{2}$$

Factor of 4 (9, electric charge of λ -quarks!) larger!
Compensates for suppression by $\hat{c}_\gamma^{\text{SM}} \approx -4.9$

3. Higgs Phenomenology in Warped Extra Dimensions

- Investigate $pp \rightarrow h \rightarrow BB = \gamma\gamma, WW^{(*)}, ZZ^{(*)}$

Gluon fusion $f_{GF} = 0.9$

Vector boson fusion $f_{VBF} = 0.1$

$$R_{BB} \equiv \frac{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow BB)_{\text{RS}}}{(\sigma \cdot \text{BR})(pp \rightarrow h \rightarrow BB)_{\text{SM}}} = \frac{[(|\kappa_g|^2 + |\kappa_{g5}|^2) f_{GF} + \kappa_V^2 f_{VBF}] [|\kappa_B|^2 + |\kappa_{B5}|^2]}{\kappa_h}$$

Correction to Higgs width $\kappa_h = \frac{\Gamma_h^{\text{RS}}}{\Gamma_h^{\text{SM}}} = 0.57 |\kappa_b|^2 + 0.22 |\kappa_W|^2 + 0.06 (|\kappa_g|^2 + |\kappa_{g5}|^2) + 0.15$

- Plot R_{BB} as a function of $M_{g(1)}$ for $y_* = 0.5, 1.5$ and 3
- Compare with data, calculate $R_{BB}^{\text{th}}/R_{BB}^{\text{exp}}$ and check compatibility with 1
- Derive exclusion ranges in $y_* - M_{g(1)}$ parameter space

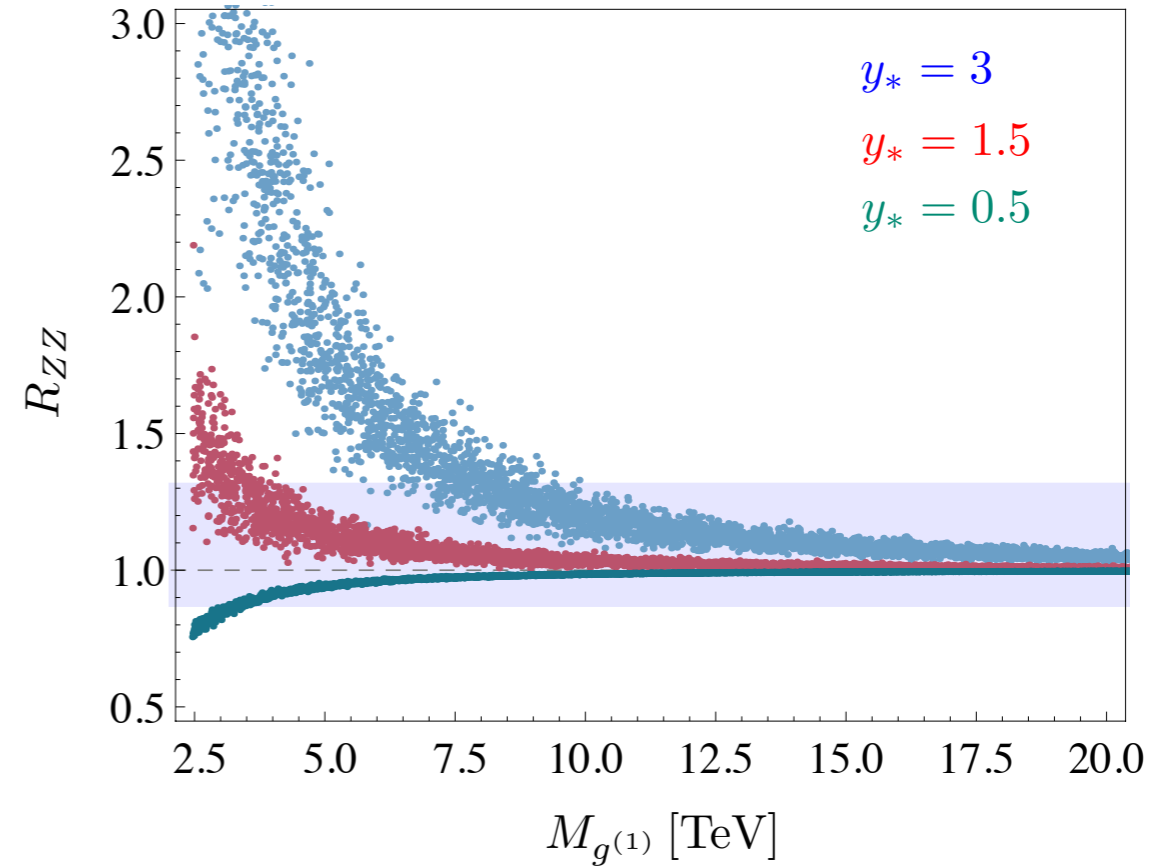
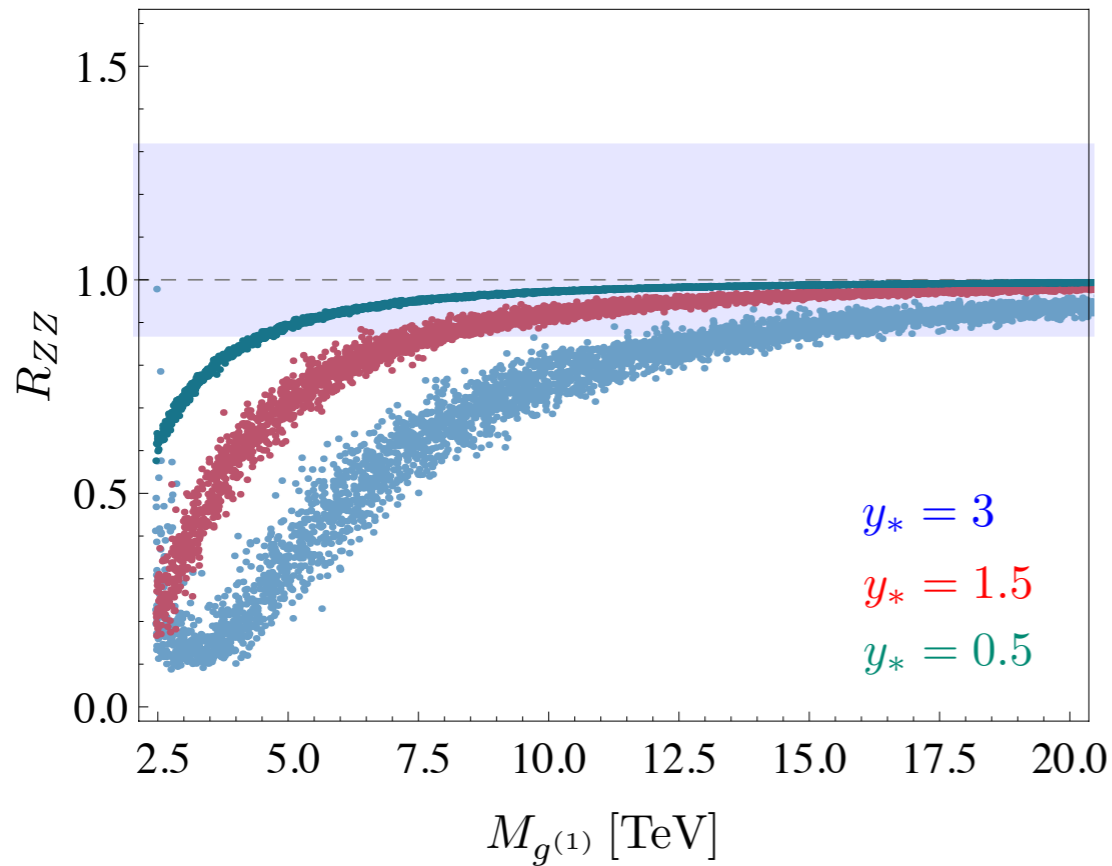
3. Phenomenology: RS predictions for $pp \rightarrow h \rightarrow ZZ^{(*)}$

ATLAS: hep-ex/1307.1427
 CMS: CMS-PAS-HIG-13-005

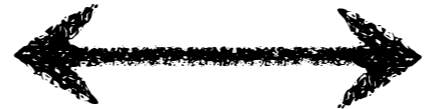
Minimal model

Brane Higgs

Narrow Bulk Higgs



• R_h strictly below 1



• R_h above 1

- Effect increases with larger y_*
- Possible to set limits on mass of lightest KK gluon $M_{g^{(1)}} = 2.45 M_{\text{KK}}$
- Data disfavor KK gluon masses in the low TeV range

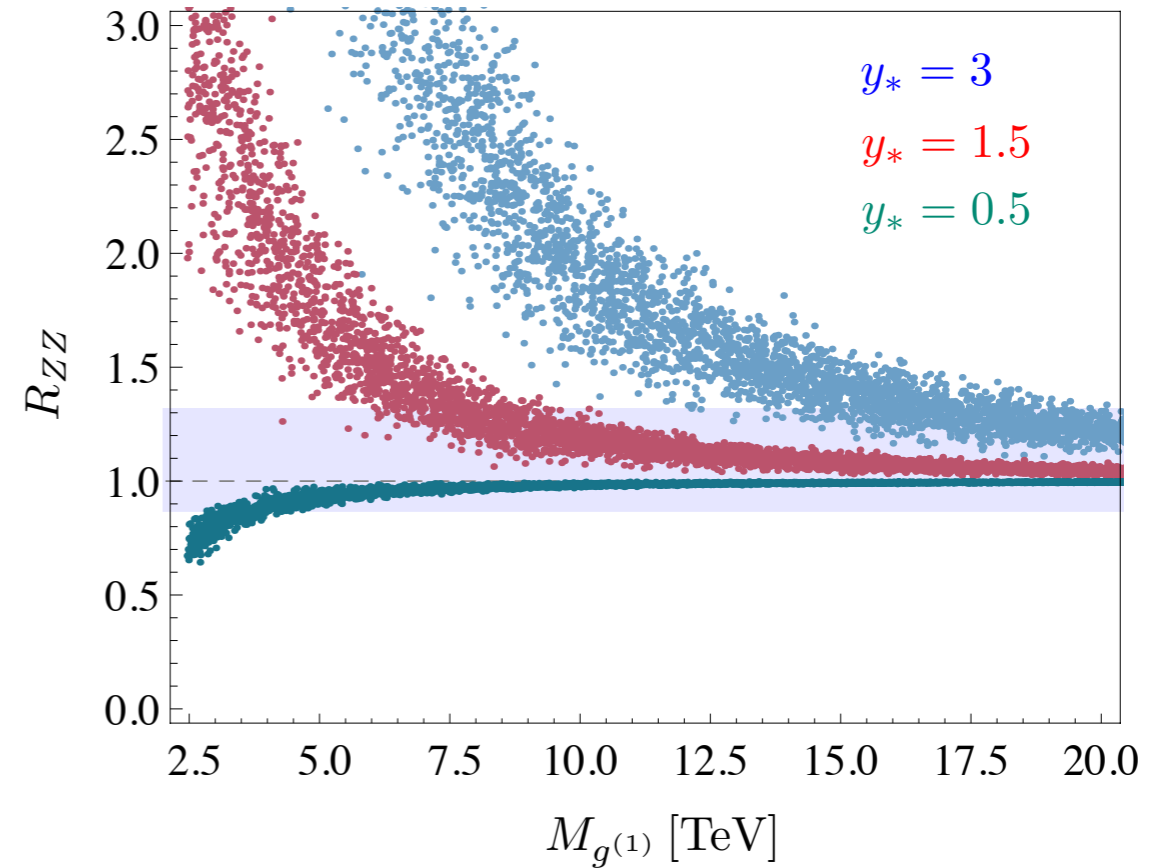
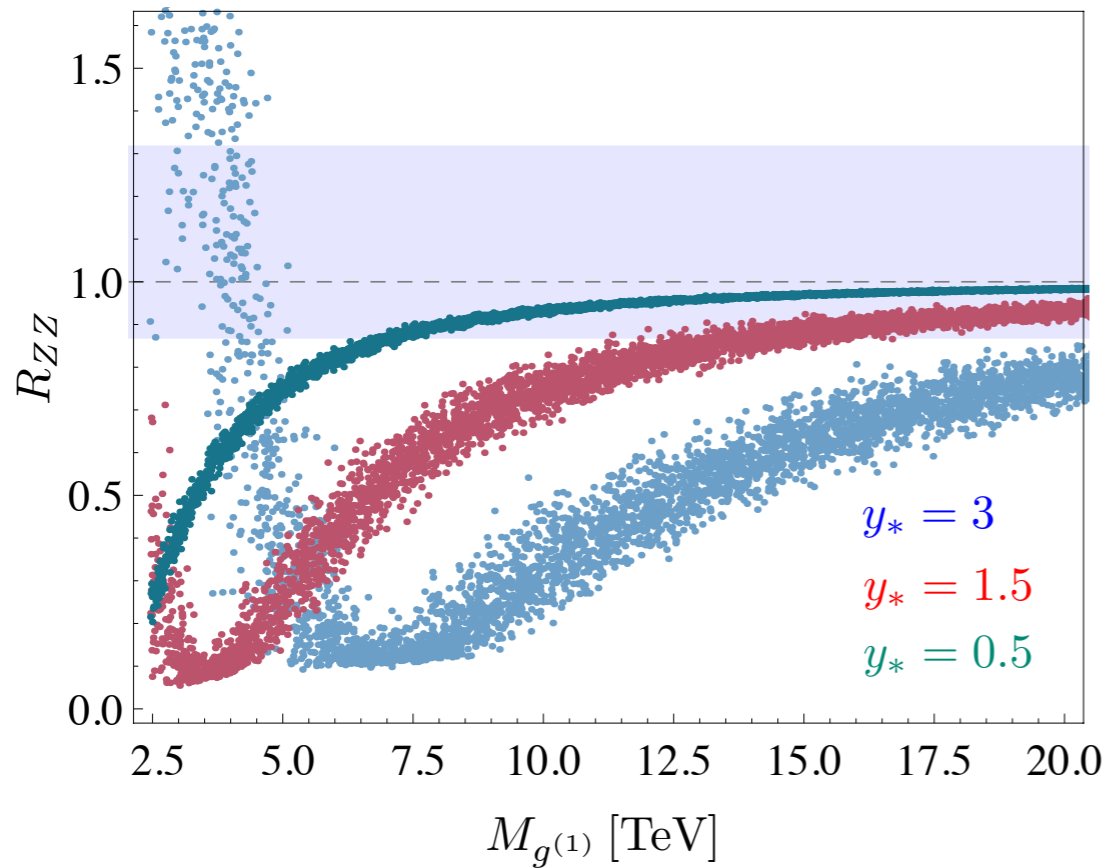
3. Phenomenology: RS predictions for $pp \rightarrow h \rightarrow ZZ^{(*)}$

ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005

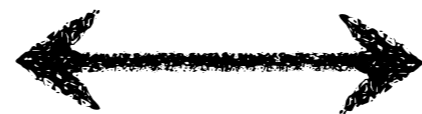
Custodial model

Brane Higgs

Narrow Bulk Higgs



• R_h below or above 1



• R_h above 1

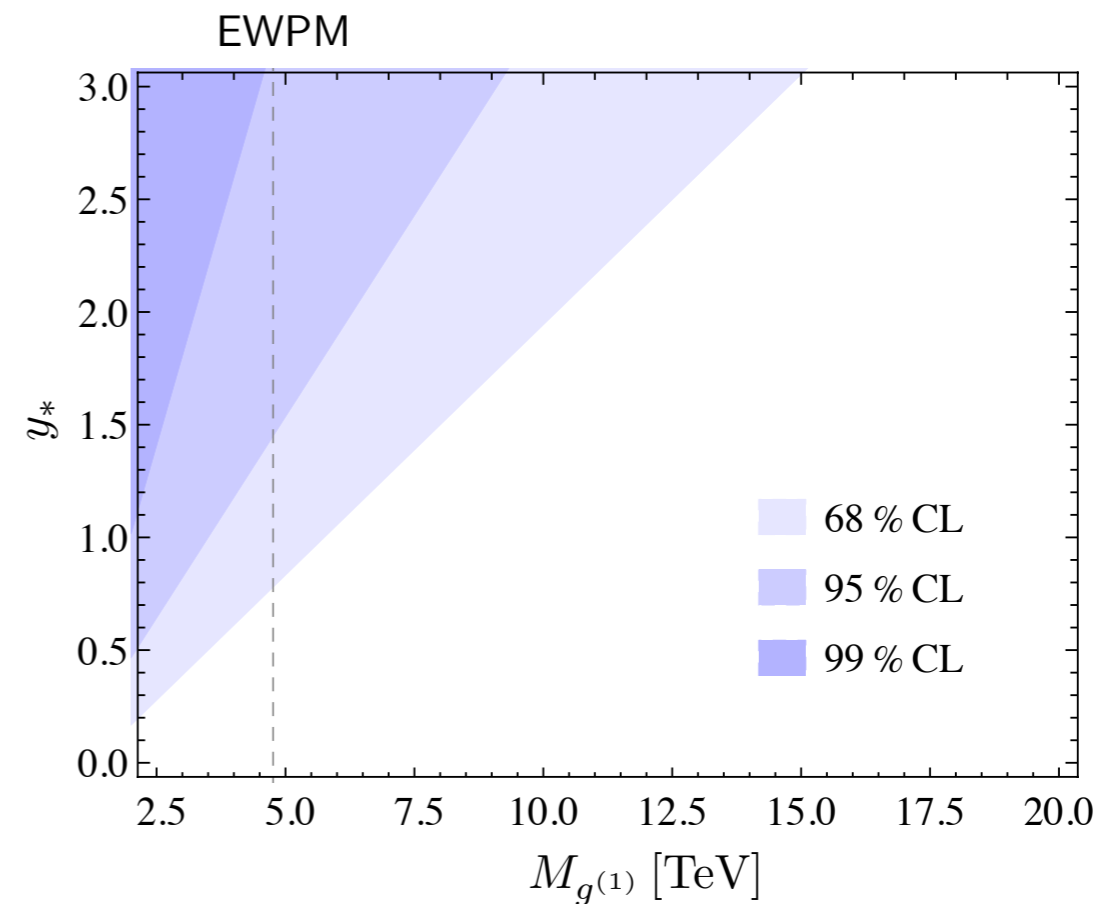
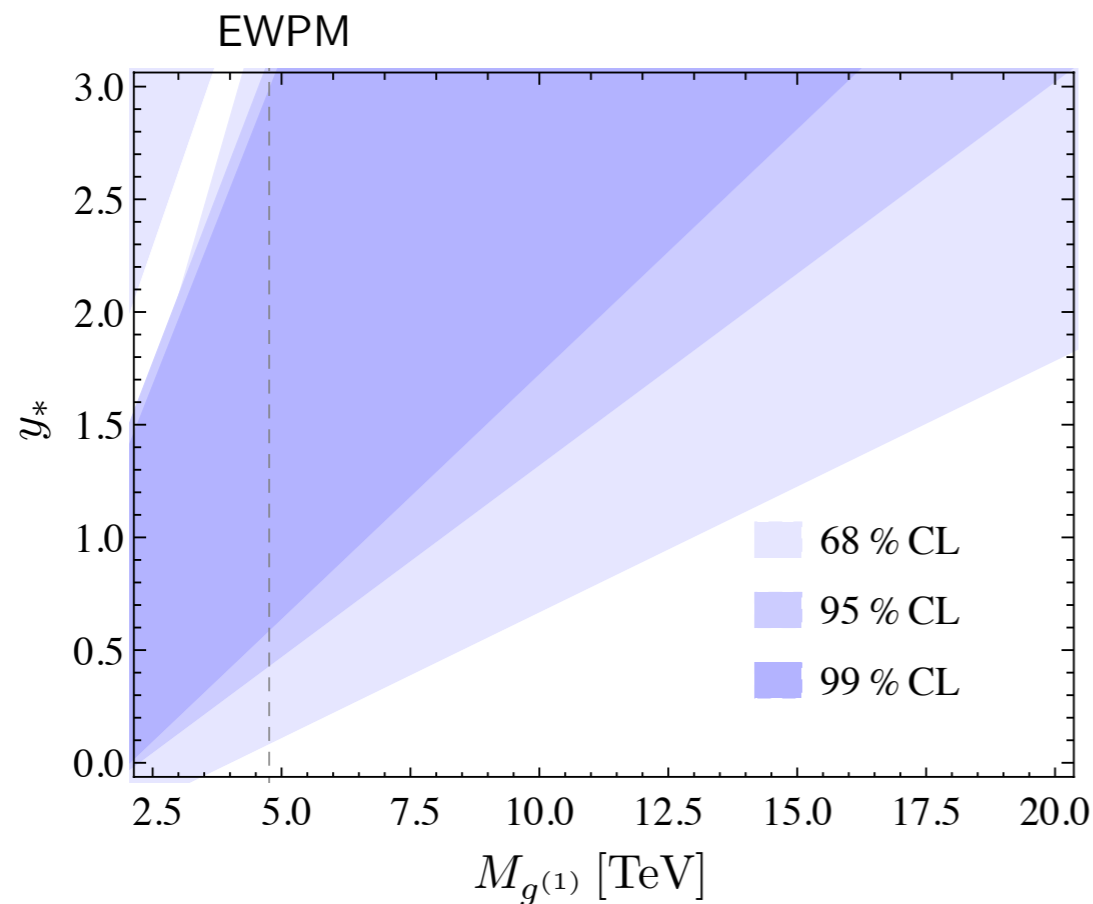
- Even larger effect due to factor of 4
- For large y_* KK contribution exceeds SM contribution
- Data disfavor KK gluon masses in the low TeV range

3. Phenomenology: RS predictions for $pp \rightarrow h \rightarrow ZZ^{(*)}$

Exclusion plots: Custodial model

Brane Higgs

Narrow Bulk Higgs



- Huge range of KK masses disfavored for not too small y_*
- For large y_* low TeV-range KK gluon masses allowed
- But: Low KK scales disfavored by EWPM
- Custodial model loses its advantage of lowering the KK scale

3. Phenomenology: Bounds on KK gluon mass

minimal RS model

model	brane Higgs	narrow bulk-Higgs
$h \rightarrow WW^{(*)}$	$M_{g(1)} > 6.4 \text{ TeV}$	$M_{g(1)} > 7.3 \text{ TeV}$
$h \rightarrow ZZ^{(*)}$	$M_{g(1)} > 10.1 \text{ TeV}$	$M_{g(1)} > 4.4 \text{ TeV}$
$h \rightarrow \gamma\gamma$	$M_{g(1)} > 8.5 \text{ TeV}$	—

95% CL
 $y_* = 3$

custodial RS model

model	brane Higgs	narrow bulk-Higgs
$h \rightarrow WW^{(*)}$	$2.9 \text{ TeV} < M_{g(1)} < 5.1 \text{ TeV}$ or $M_{g(1)} > 12.9 \text{ TeV}$	$M_{g(1)} > 15.0 \text{ TeV}$
$h \rightarrow ZZ^{(*)}$	$3.4 \text{ TeV} < M_{g(1)} < 4.6 \text{ TeV}$ or $M_{g(1)} > 19.9 \text{ TeV}$	$M_{g(1)} > 9.1 \text{ TeV}$
$h \rightarrow \gamma\gamma$	$3.5 \text{ TeV} < M_{g(1)} < 5.9 \text{ TeV}$ or $M_{g(1)} > 13.4 \text{ TeV}$	$3.8 \text{ TeV} < M_{g(1)} < 5.2 \text{ TeV}$ or $M_{g(1)} > 8.4 \text{ TeV}$

- Strongest bounds from $h \rightarrow ZZ^{(*)}$ (brane) and $h \rightarrow WW^{(*)}$ (narrow-bulk)
- Bounds in minimal model weaker than those from EWPM
- Bounds in custodial model much stronger than those from EWPM
- Custodial model loses its advantage of lowering the KK scale

3. Phenomenology: Bounds on maximal value of Yukawas

minimal RS model

model	brane Higgs	narrow bulk-Higgs
$h \rightarrow WW^{(*)}$	$y_* < 2.1$	$y_* < 2.2$
$h \rightarrow ZZ^{(*)}$	$y_* < 1.1$	—
$h \rightarrow \gamma\gamma$	$y_* < 1.5$	—

95% CL
 $M_{g^{(1)}} = 5 \text{ TeV}$

custodial RS model

model	brane Higgs	narrow bulk-Higgs
$h \rightarrow WW^{(*)}$	$y_* < 0.9$ or $y_* > 2.9$	$y_* < 1.0$
$h \rightarrow ZZ^{(*)}$	$y_* < 0.5$	$y_* < 1.5$
$h \rightarrow \gamma\gamma$	$y_* < 0.9$ or $y_* > 2.5$	$y_* < 1.7$ or $y_* > 2.9$

- Strongest bounds from $h \rightarrow ZZ^{(*)}$ (brane) and $h \rightarrow WW^{(*)}$ (narrow-bulk)
- Small values preferred, in particular for custodial model
- Too small values for y_* problematic for ϵ_K
- KK particles probably too heavy for direct detection at the LHC

4. Conclusions

- The RS model is able to explain the hierarchy problems of the SM (by warp factor and different localization of fermions in bulk)
- Could explain the contradictory results for $gg \rightarrow h$ in the RS model
 - Narrow bulk vs. brane Higgs (two different models!)
 - Transition region not calculable!
- Loop-induced couplings very sensitive on virtual effects of KK excitations
- Large Effects possible even for high KK masses, in particular in custodial RS model
- Current measurements: R_{WW} , R_{ZZ} , and $R_{\gamma\gamma}$ excellent quantities to distinguish between RS scenarios and to give bounds on RS parameter space
- Direct detection of KK particles at the LHC disfavored (in either scenario)
- Thus, (more precise) measurements of R_{WW} , R_{ZZ} , and $R_{\gamma\gamma}$ and the couplings κ_i desirable → indirect detection

4. Outlook

- Complete the discussion of Higgs physics in warped extra dimensions by studying Higgs processes in bulk-Higgs RS models
- Use solutions for 5D propagators to study $b \rightarrow s\gamma$ or $\mu \rightarrow e\gamma$

Thank you for your attention!

Backup: Classification of Models

Model	bulk Higgs	narrow bulk-Higgs	transition region	brane Higgs
Higgs profile width	$\eta = \mathcal{O}(1)$	$\frac{v Y_q }{\Lambda_{\text{TeV}}} \ll \eta \ll \frac{v Y_q }{M_{\text{KKK}}}$	$\eta \sim \frac{v Y_q }{\Lambda_{\text{TeV}}}$	$\eta \ll \frac{v Y_q }{\Lambda_{\text{TeV}}}$
Power corrections	$\sim \frac{M_{\text{KKK}}}{\Lambda_{\text{TeV}}}$	$\sim \frac{M_{\text{KKK}}}{\eta \Lambda_{\text{TeV}}}$	$\sim \frac{M_{\text{KKK}}}{v Y_q }$	$\sim \frac{M_{\text{KKK}}}{\Lambda_{\text{TeV}}}$
Higgs profile	resolved by all modes	resolved by high-momentum modes	partially resolved by high-momentum modes	not resolved
$\mathcal{A}(gg \rightarrow h)$	enhanced [hep-ph/1006.5939]	enhanced	not calculable	suppressed

Backup: Derivation of 5D quark propagator

- 5D Dirac equation $\mathcal{D} \mathbf{S}^q(t, t'; p) = \delta(t - t')$
- 5D Dirac operator $\mathcal{D} = \not{p} - M_{\text{KK}} \gamma_5 \partial_t - M_{\text{KK}} \mathcal{M}_q(t)$
- Mass matrix $\mathcal{M}_q(t) = \frac{1}{t} \begin{pmatrix} \mathbf{c}_Q & 0 \\ 0 & -\mathbf{c}_q \end{pmatrix} + \frac{v}{\sqrt{2} M_{\text{KK}}} \delta^\eta(t - 1) \begin{pmatrix} 0 & \mathbf{Y}_q \\ \mathbf{Y}_q^\dagger & 0 \end{pmatrix}$
- Propagator $\mathbf{S}^q(t, t'; p) = [\Delta_{LL}^q(t, t'; -p^2) \not{p} + \Delta_{RL}^q(t, t'; -p^2)] P_R + L \leftrightarrow R$
- This gives coupled differential equations for $\Delta_{RL, LL}^q$
- UV/IR Boundary conditions given by BC for fermion profiles
- Together with jump conditions at $t = t'$ (due to $\delta(t - t')$) we get unique solutions for bulk ($t < 1 - \eta$) and sliver ($t > 1 - \eta$)
- Then: Evaluate (with sliver solution)

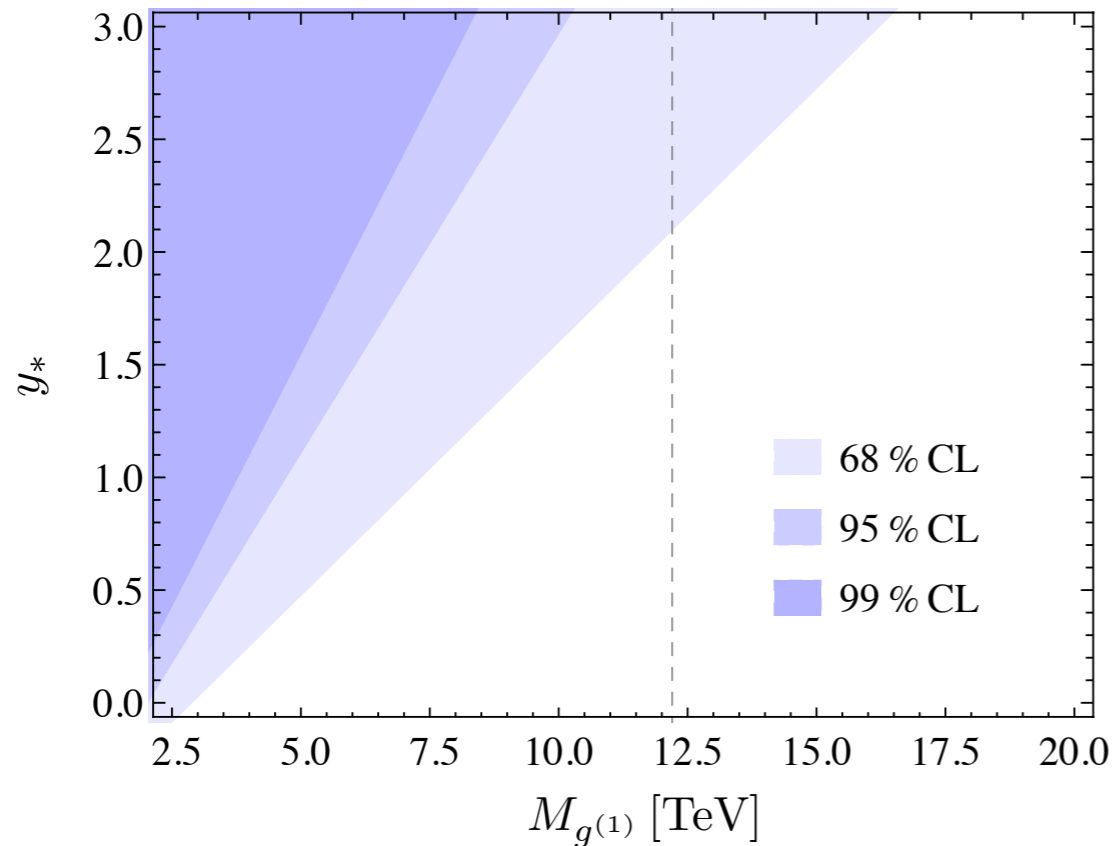
$$T_+(p_E^2) = - \sum_{u,d} \frac{v}{\sqrt{2}} \int_\epsilon^1 \delta^\eta(t - 1) \text{Tr} \left[\begin{pmatrix} 0 & \mathbf{Y}_q \\ \mathbf{Y}_q^\dagger & 0 \end{pmatrix} \frac{\Delta_{RL}^q(t, t; -p^2) + \Delta_{LR}^q(t, t; -p^2)}{2} \right]$$

3. Phenomenology: RS predictions for $pp \rightarrow h \rightarrow ZZ^{(*)}$

Exclusion plots: Minimal model

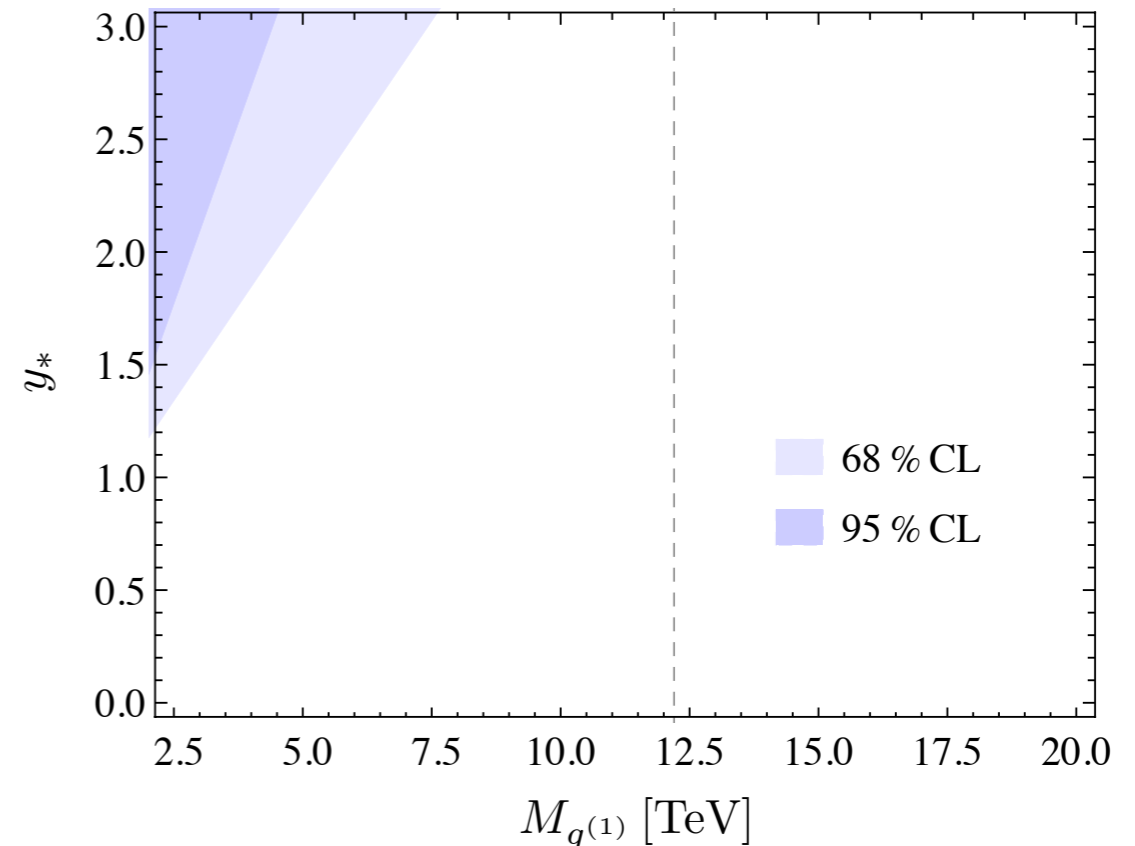
Brane Higgs

EWPM



Narrow Bulk Higgs

EWPM

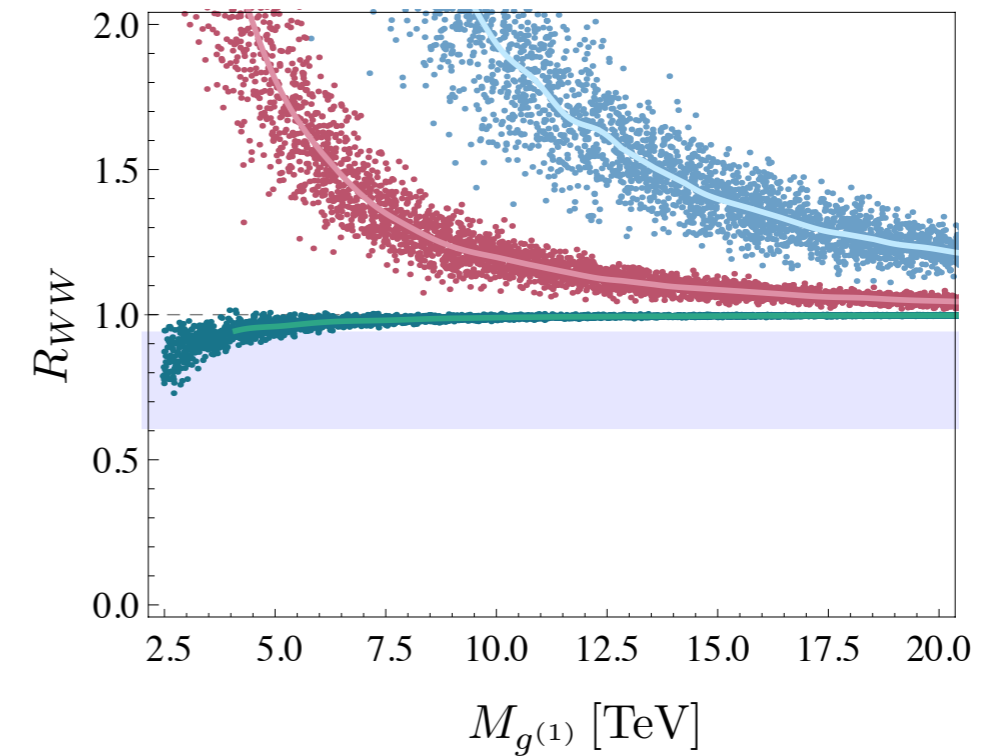
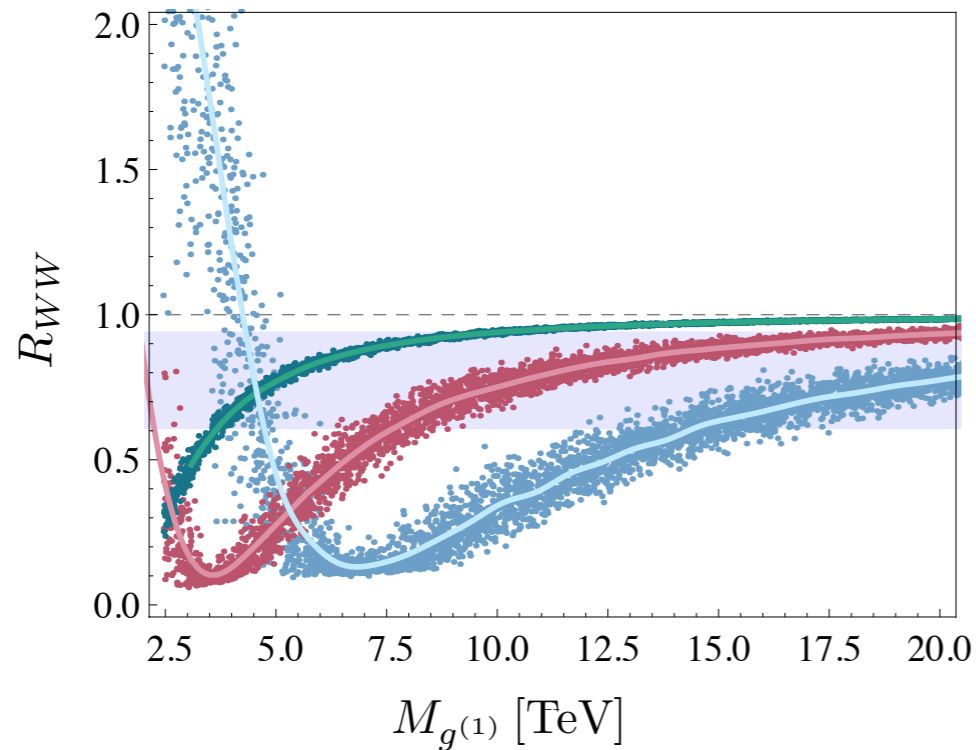
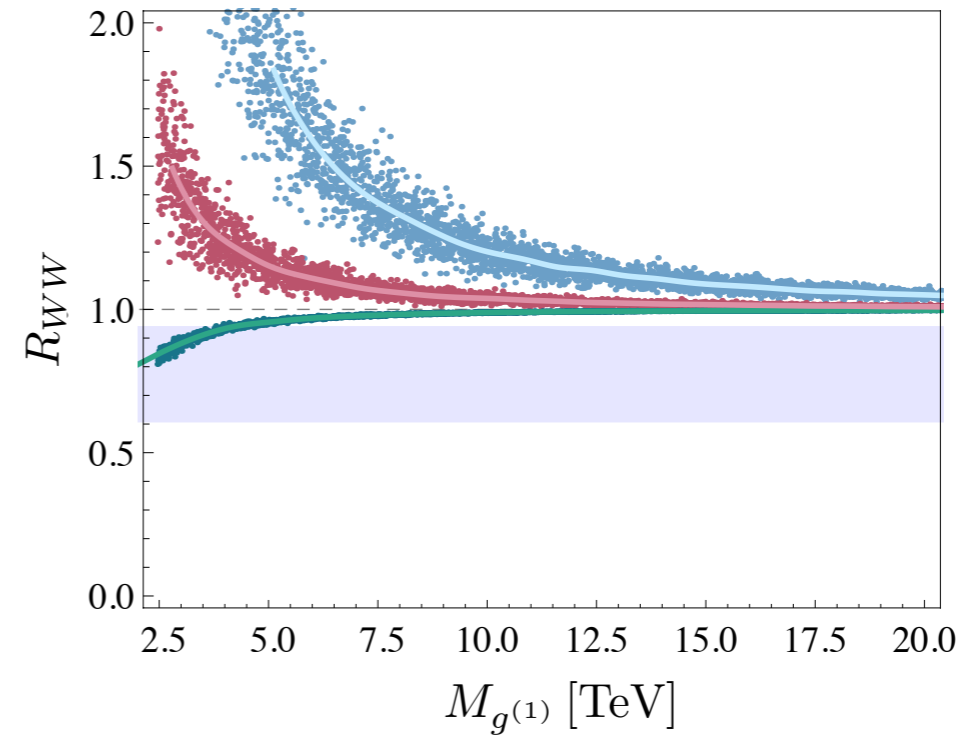
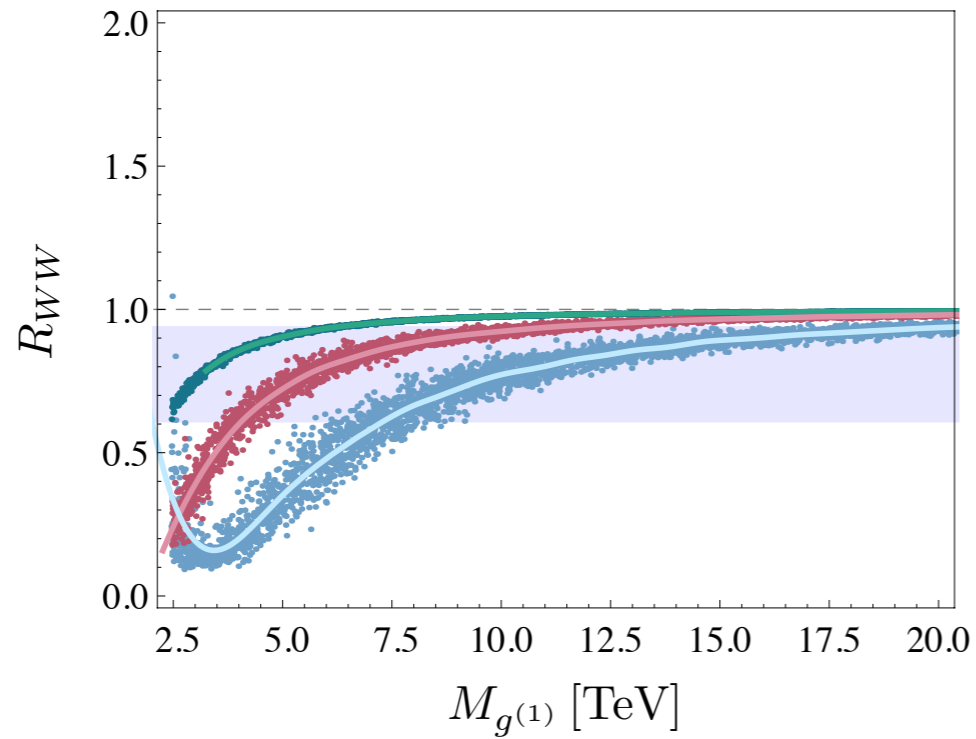


- For large (small) y_* low TeV-range KK gluon masses disfavored (favored)
- Brane Higgs: constraints comparable with those from EWPM
- Narrow-bulk Higgs: weaker constraints than those from EWPM

Backup: RS predictions for $pp \rightarrow h \rightarrow WW^{(*)}$

ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005

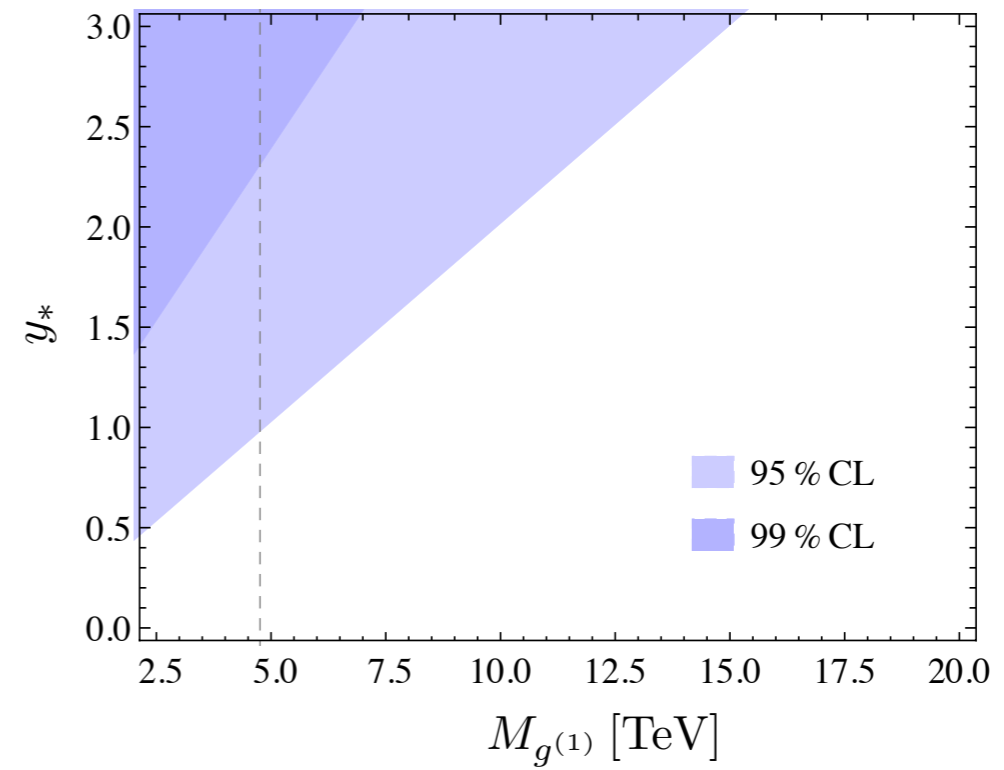
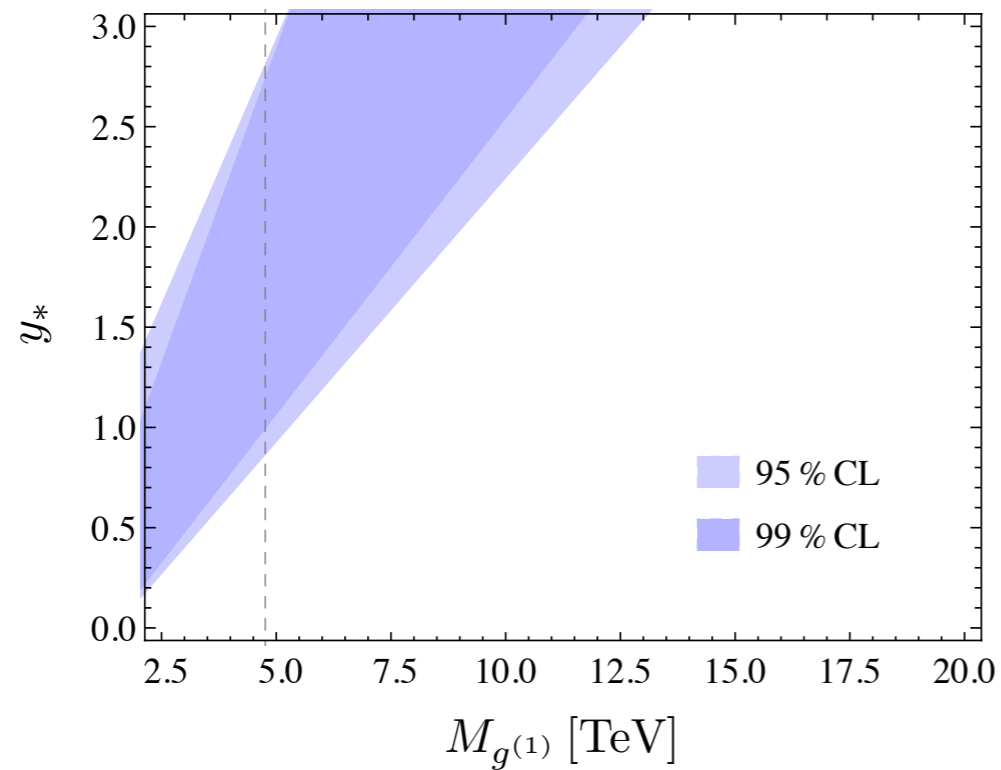
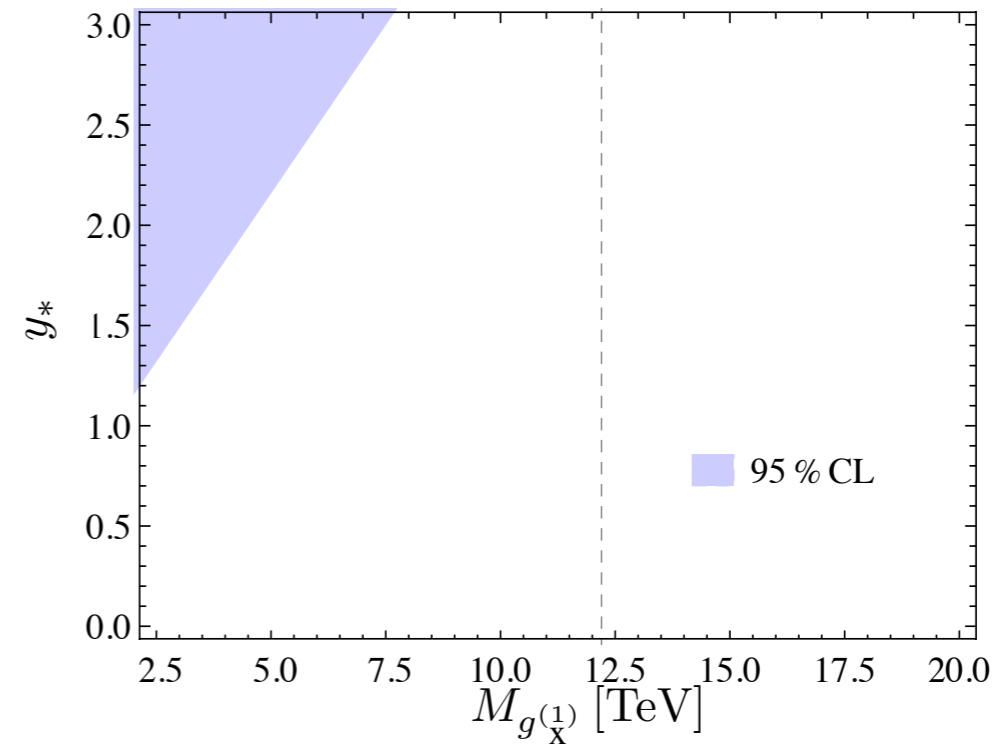
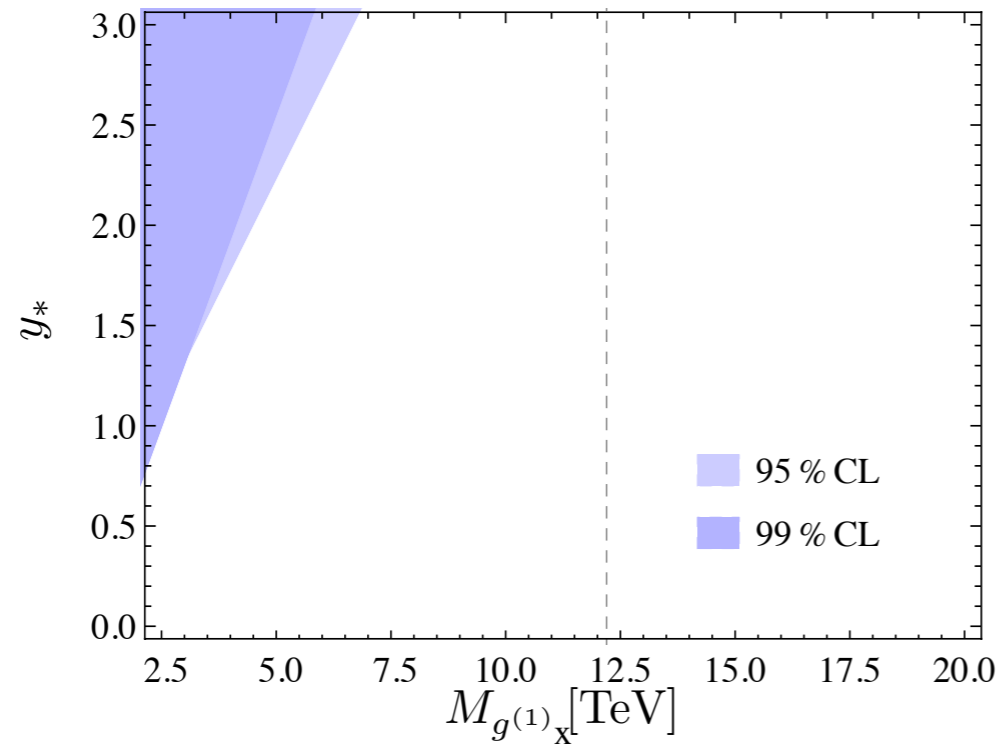
$y_* = 3$
 $y_* = 1.5$
 $y_* = 0.5$



Backup: RS predictions for $pp \rightarrow h \rightarrow WW^{(*)}$

Exclusion plots

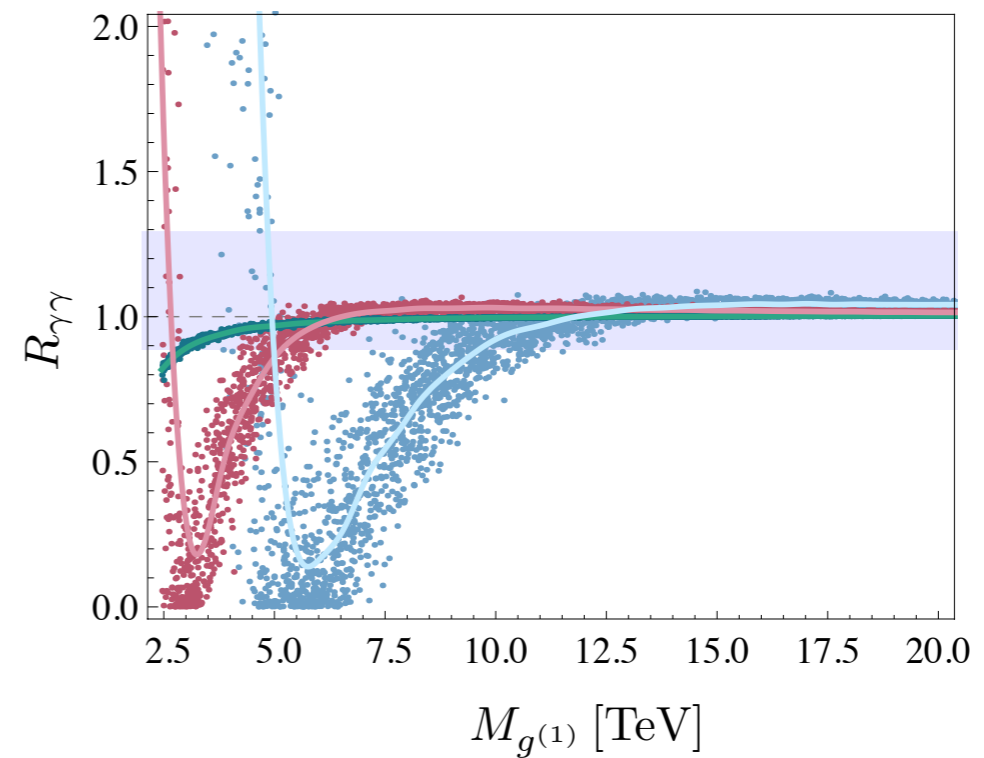
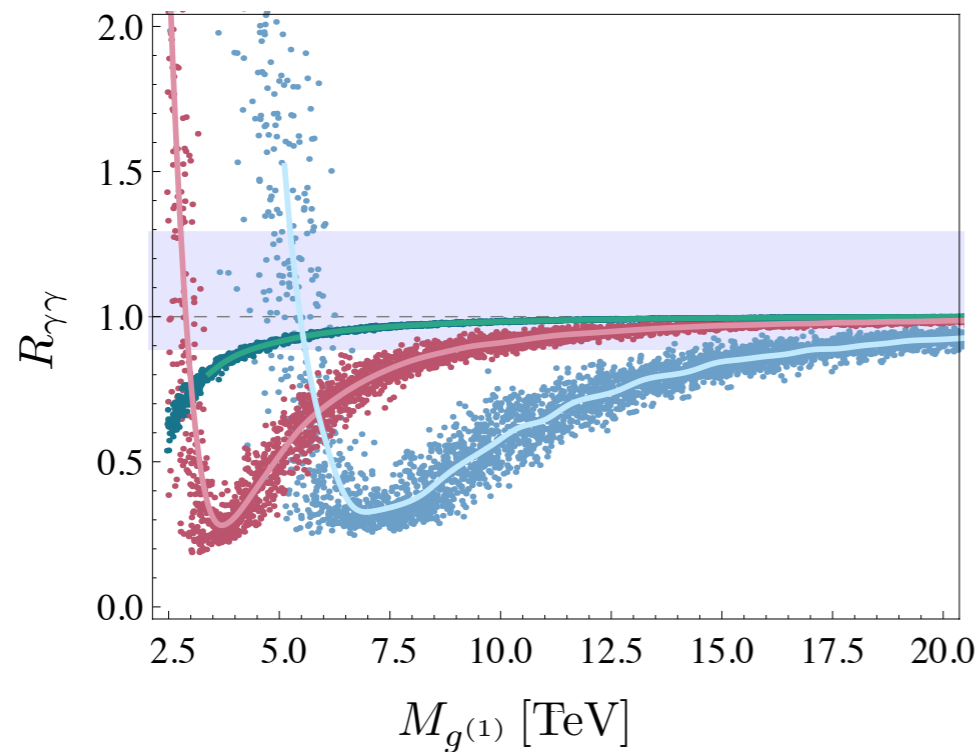
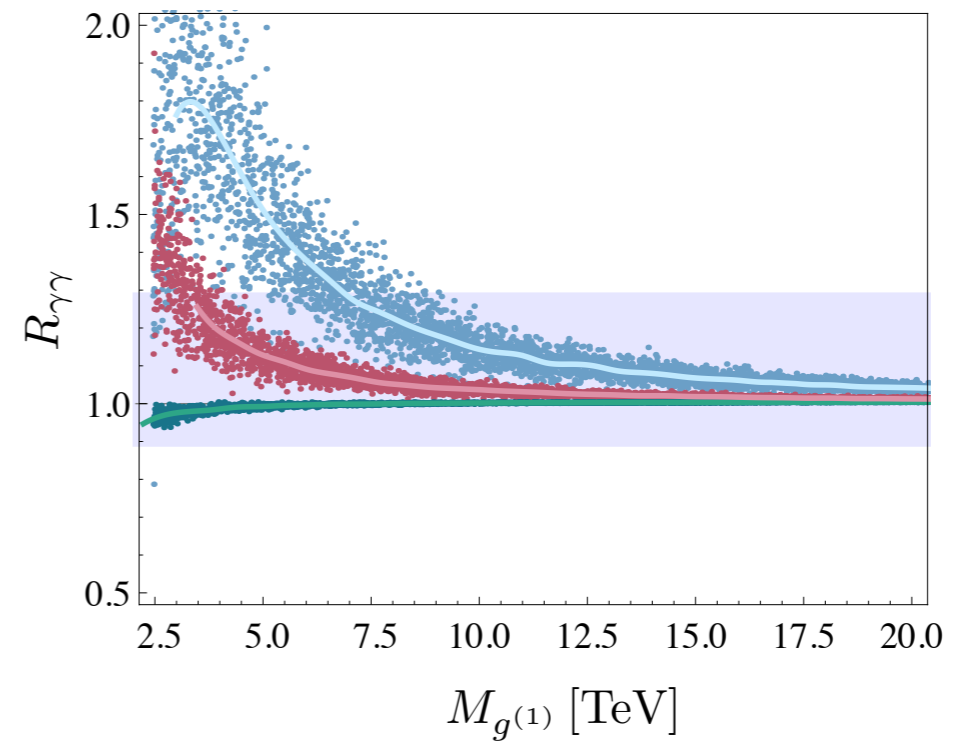
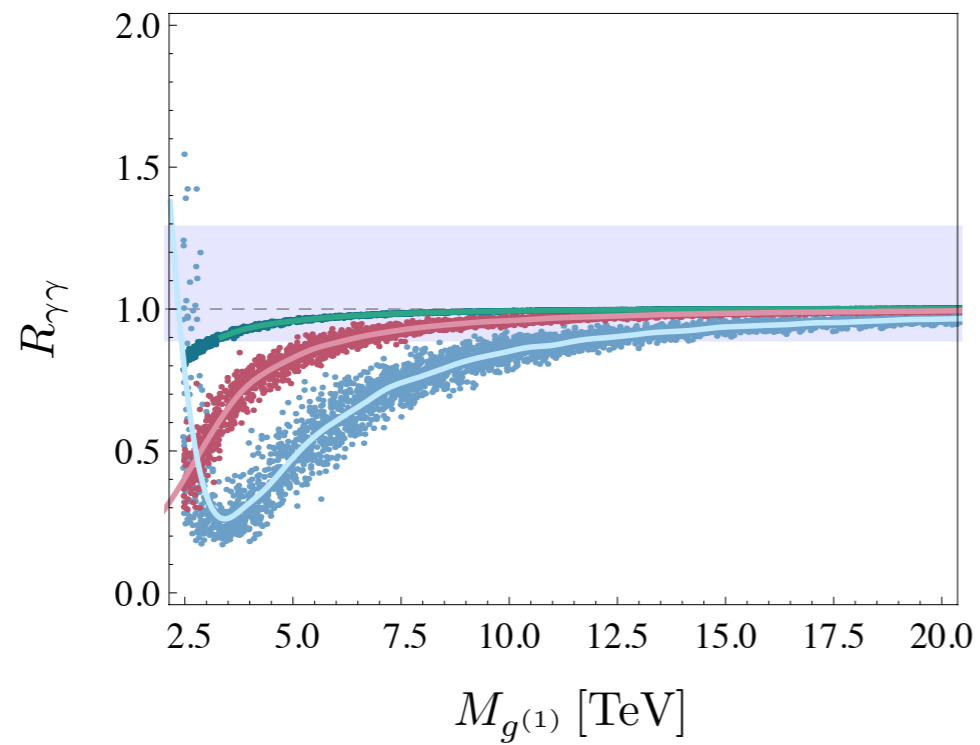
ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005



Backup: RS predictions for $pp \rightarrow h \rightarrow \gamma\gamma$

ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005

$y_* = 3$
 $y_* = 1.5$
 $y_* = 0.5$



Backup: RS predictions for $pp \rightarrow h \rightarrow \gamma\gamma$

Exclusion plots

ATLAS: hep-ex/1307.1427
CMS: CMS-PAS-HIG-13-005

