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**PROBLEM SET 9**

Reading: Handout on NMR

**1. Thermodynamics of a Simple System of Spin-1/2 Particles**

Consider a solid with  $N$  weakly interacting spin-1/2 particles, each with magnetic moment of magnitude  $\mu_B$ . The solid is in a uniform external magnetic field  $\vec{H}$  pointing along the z-axis. The solid is in contact with a heat bath at temperature  $T$ . The Hamiltonian  $\mathcal{H}$  is

$$\mathcal{H} = -\vec{\mu} \cdot \vec{H} \quad (1)$$

where  $\vec{\mu}$  is the magnetic moment. Find, as a function of temperature,

- (a) the magnetization  $M$
- (b) the susceptibility  $\chi$ . Plot or sketch the susceptibility vs.  $T$ . (This is called the Curie susceptibility.)
- (c) the specific heat at constant volume  $C_V$ . Plot or sketch the  $C_V$  vs.  $T$ . (This is called the Schottky specific heat.)