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**PROBLEM SET 7**

Reading: AM Chapter 34 or Marder (2nd Ed) Chapter 27 or Kittel (8th Ed) Chapter 10

**1. Josephson Inductance** Starting from

$$I = I_c \sin \delta \quad (1)$$

show that the nonlinear inductance  $L_J$  of a Josephson junction is given by

$$L_J = \frac{\phi_o}{2\pi} \frac{1}{I_c \cos \delta} \quad (2)$$

where  $\phi_o$  is the flux quantum given by

$$\phi_o = \frac{2\pi\hbar c}{2e} \quad (3)$$

Remember that the inductance is positive.

**2. Ginzburg-Landau Equation and the Proximity Effect** When a normal metal is placed in contact with a superconductor, the superconducting wave function can leak into the metal and make the metallic region near the interface superconducting. This is known as the proximity effect.

Consider a metal (in the half-space  $x > 0$ ) in contact with a superconductor (occupying a region  $x < 0$ ). Assuming that the normal metal can be described by a Ginzburg-Landau model but with  $a > 0$ , show that the superconducting order parameter  $\psi(x)$  induced in the metal by the contact with the superconductor is approximately

$$\psi(x) = \psi(0)e^{-x/\xi(T)} \quad (4)$$

where

$$\frac{\hbar^2}{4m\xi(T)^2} = a > 0 \quad (5)$$

and  $\psi(0)$  is the order parameter of the superconductor at the interface.

*Hint:* Start from the Ginzburg-Landau equation

$$-\frac{\hbar^2}{4m}\nabla^2\psi + a\psi + b|\psi|^2\psi = 0 \tag{6}$$