

### PROBLEM SET 7

*November 8 Colloquium:* “Domain coarsening in a pattern: how do stripes grow?”

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3:30 pm, 101 Rowland Hall

1. Name the topic of your report (try to be specific) and list the reference(s) you will use for your final report.
2. **AC Josephson Effect** When a static DC voltage  $V$  is applied across a Josephson junction, an AC current results. To see how this comes about, notice that an electron pair experiences a potential energy difference  $qV$  on passing across the junction, where  $q = -2e$ . We can say that a pair on one side is at potential  $-eV$  and a pair on the other side is at  $+eV$ . Thus the equations of motion become

$$i\hbar \frac{\partial \psi_1}{\partial t} = \hbar T \psi_2 - eV \psi_1 \quad i\hbar \frac{\partial \psi_2}{\partial t} = \hbar T \psi_1 + eV \psi_2 \quad (1)$$

where  $\psi_1$  is the superconducting order parameter on side 1:

$$\psi_1 = \sqrt{n_1} e^{i\theta_1} \quad (2)$$

$n_1$  is the density of superconducting pairs on side 1. Similarly

$$\psi_2 = \sqrt{n_2} e^{i\theta_2} \quad (3)$$

Assume that the superconductors are identical. Find the current density  $J$  as a function of time and of the phase difference  $\delta(0)$ .  $\delta(0) = \theta_2 - \theta_1$  is the phase difference at  $V = 0$ . What is the angular frequency  $\omega$  at which the current oscillates when a voltage  $V$  is applied?

3. Eisberg and Resnick Problem 13.18.

4. Eisberg and Resnick Problem 13.24.

5. Eisberg and Resnick Problem 13.30 (n-p-n transistor).