Physics 224

**Discoveries and Inventions of Modern Physics** 

## Fall 2002

due 11:00 am Tuesday Oct. 15

## PROBLEM SET 2

Oct. 10 Colloquium: "Dynamic Contrast Magnetic Resonance Imaging in Cancer and Neuro Studies"

Professor Lydia Su, UCI

3:30 pm, 101 Rowland Hall

- 1. Consider a nonrelativistic free particle in a cubic container of edge length L and volume  $V = L^3$ . Assume that the particle is confined in the container so that the potential is zero inside the container and infinite outside.
  - (a) Each quantum state s of this particle has a corresponding kinetic energy  $\varepsilon_s$  which depends on V. What is  $\varepsilon_s(V)$ ?
  - (b) Find the contribution to the gas pressure  $p_s = -(\partial \varepsilon_s / \partial V)$  of a particle in this state in terms of  $\varepsilon_s$  and V.
  - (c) Use this result to show that the mean pressure  $\langle p \rangle$  of any ideal gas of particles is always related to its mean total kinetic energy  $\langle E \rangle$  by  $\langle p \rangle = \frac{2}{3} \langle E \rangle /V$ .
- 2. Eisberg and Resnick: 1.16
- 3. Eisberg and Resnick: 11.3 (Note that in terms of the notation used in class  $\varepsilon_F = \mu$ .)
- 4. Eisberg and Resnick: 11.5 (Note that in terms of the notation used in class  $\alpha = -\beta \mu$ .)
- 5. Plot the blackbody distribution spectrum  $\rho_T(\eta)$  versus  $\eta = \hbar \omega / kT$  at T=3 K.
- 6. Eisberg and Resnick: 1.19 (Hint: Use the result of the previous problem and the result stated in problem 1.18.)
- 7. Eisberg and Resnick: 1.12